## SUSY-phenomenology-based models of Higgs inflation

Shinsuke Kawai

Sungkyunkwan University, South Korea

Based on [1512.05861] [1411.5188] [1404.1450] [1212.6828] [1107.4767] [1112.2391] Collaborators: Nobuchika Okada (Alabama), Jinsu Kim (KIAS), Masato Arai (Yamagata)

18 Feb 2016 @HIP

# What is the particle physics behind inflation?

### String theory



#### Particle phenomenology

### Standard Model of particle physics



or, beyond the Standard Model (+singlets, SUSY, etc.)

# Inflaton: origin of everything

- A scalar field where is it from?
- Right handed scalar neutrino?

m ~10<sup>13</sup> GeV chaotic inflation [Murayama Suzuki Yanagida Yokoyama 1992]

Higgs field?

SM Higgs boson: mass  $\approx 125$  GeV,  $\lambda \approx O(1)$ Chaotic inflation: m  $\approx 10^{13}$  GeV or  $\lambda \approx 10^{-12}$ 



- Nonminimal coupling to gravity [Cervantes-Cota, Dehnen 1995] [Bezrukov Shaposhnikov 2008]

- Non canonical kinetic term [Nakayama Takahashi] [Germani Kehagias] [others]
- Curvaton scenario [Langlois Vernizzi] [others]
- RG criticality, ad-hoc modification beyond cutoff [Hamada et al.]

### m<sup>2</sup>φ<sup>2</sup> chaotic inflation (RHN)



Planck 2015 [1502.02114v1]

**Nonminimal Higgs inflation** 

# Confidence level (CL)

1σ: 68% 2σ: 95% 3σ: 99.7% 4σ: 99.994% 5σ: 99.99994%

in collider physics

 $5\sigma \approx 50\%$ in cosmology





- Particle phenomenology-based approach to cosmic inflation: Higgs inflation
- Supersymmetric Higgs inflation
  - Supersymmetric Higgs-lepton inflation
  - Supersymmetric SU(5) GUT inflation
- Summary

### Higgs inflation

[Bezrukov Shaposhnikov, PLB 659 (2008) 703]

• Higgs potential:  $V = \frac{\lambda}{4}(\phi^2 - v^2)^2$ 

$$\mathcal{L} = \mathcal{L}_{\rm SM} - \frac{M_P^2}{2}R - \xi H^{\dagger} H R$$

• During inflation  $\langle \phi \rangle \gg v$ 

$$S = \int d^4x \sqrt{-g} \left( -\frac{M_P^2 + \xi \phi^2}{2} R + \frac{1}{2} (\partial_\mu \phi)^2 - \frac{\lambda}{4} \phi^4 \right)$$

• This is in the Jordan frame. Go to the Einstein frame:

$$\hat{g}_{\mu\nu} = \Omega^2 g_{\mu\nu}, \qquad \Omega^2 = 1 + \frac{\xi \phi^2}{M_{\rm P}^2}$$



• In the Einstein frame,

$$S_{E} = \int dx^{4} \sqrt{-\hat{g}} \left( -\frac{M_{P}^{2}}{2} \hat{R} + \frac{1}{2} (\partial_{\mu} \hat{\phi})^{2} - U(\hat{\phi}) \right)$$

$$\frac{d\hat{\phi}}{d\phi} = \Omega^{-2} \sqrt{\Omega^{2} + 6\xi^{2} \phi^{2} M_{P}^{-2}}$$

$$U(\hat{\phi}) = \frac{\lambda}{4} \frac{(\phi^{2} - v^{2})^{2}}{\Omega^{4}}$$

$$U(\hat{\phi})$$

$$\cdot \text{ Inflaton potential}$$

$$\phi \ll M/\xi \Longrightarrow \hat{\phi} \approx \phi$$

$$M/\xi \ll \phi \ll M/\sqrt{\xi} \Longrightarrow \hat{\phi} \approx \sqrt{3/2}\xi \phi^{2}$$

$$\phi \gg M/\sqrt{\xi} \Longrightarrow \hat{\phi} \approx \sqrt{6} \ln \phi$$

$$\lambda M^{4} \xi^{2}/16$$

$$\int_{0}^{\sqrt{\lambda} end} \frac{\lambda \sqrt{4/4}}{\sqrt{\lambda} e^{-\frac{1}{2}}} \hat{\phi}$$

• Inflation at  $\phi \gg M/\sqrt{\xi}$ 

$$\epsilon \equiv \frac{1}{2} \left( \frac{\partial_{\hat{\phi}} U}{U} \right)^2 \approx \frac{4}{3} \frac{M^4}{\xi^2 \phi^4}$$
$$\eta \equiv \frac{\partial_{\hat{\phi}}^2 U}{U} \approx -\frac{4}{3} \frac{M^2}{\xi \phi^2}$$

Curvature perturbation



 $U(\hat{\phi})$ 

### Summary: Higgs inflation





Inflaton identified with a known particle field

Predicted CMB spectrum fits well with the present data



Higgs potential unstable against radiative corrections

GO SUSY!



Nonminimal coupling  $\xi \sim 10000.$  This is insanely large

#### Supersymmetric extension

SM is good, but not perfect

- No good candidate of DM
- Difficulty in baryogenesis
- Hierarchy problem

Supersymmetric extension of the SM

- Gauge coupling unification favours SUSY
- UV completion, e.g. string theory
- SUSY Higgs inflation?

### The $\eta$ -problem

Supergravity with

Canonical Kähler potential

Generic superpotential W

F-term SUSY breaking

gives slow-roll parameter  $\eta \sim O(1)$ 

• Slow roll inflation in supergravity is known to be difficult.

To circumvent the  $\eta$ -problem?



"Compensator formalism" in the Jordan frame e.g. [Ferrara Kallosh Linde Marrani Van Proeyen 2010, 2011]

*K*, *W*, *fab* and  $\phi$  logically redundant, but useful in practice

#### Constructing Supersymmetric Higgs inflation



 $G_{IJ}, V(\phi^{I})$ : complicated

### Models of SUSY Higgs inflation

- Nonminimally coupled Higgs inflation not possible in MSSM
- NMSSM [Einhorn Jones 2009] [Ferrara Kallosh Linde Marrani Van Proeyen 2010]
- Pati-Salam [Pallis Toumbas 2011]
- SUSY seesaw [Arai SK Odaka 2011]
- SUSY GUT [Arai SK Odaka 2011]

focus on these example

### **SUSY Higgs inflation: generic features**

- Noncanonical K\u00e4hler potential
   nonminimal coupling

   (unlike A-term MSSM inflation
   or F-term hybrid inflation)
- Nonminimal coupling not necessarily large
- Tachyonic instability in the singlet direction, removed by further modification of Kähler [Ferrara Kallosh Linde Marrani Van Proeyen]
- Multifield dynamics not studied so far





# Single field vs. multi field

|  | SINGLE FIELD INFLATION                          | MULTI FIELD INFLATION                                  |
|--|---|--|
| BACKGROUND<br>EVOLUTION                      | Straight trajectory                             | Curved trajectory in n-<br>dimensional space           |
| DOF OF<br>FLUCTUATIONS                       | Scalar 1(=2+1-2)<br>Vector 2<br>Tensor 2        | Scalar n (=2+n-2)<br>Vector 2<br>Tensor 2              |
| EVOLUTION OF<br>FLUCTUATIONS                 | Adiabatic, freeze outside<br>the Hubble horizon | Adiabatic (curvature)<br>and<br>entropy (isocurvature) |
| NON-GAUSSIANITY<br>OF SCALAR<br>FLUCTUATIONS | Small   | Sou<br>Can be large                                    |

# Primordial density fluctuations

- Power spectrum  $\langle \zeta_{\vec{k}_1} \zeta_{\vec{k}_2} \rangle = (2\pi)^3 \delta^3 (\vec{k}_1 + \vec{k}_2) P_{\zeta}(k_1)$
- = Bispectrum  $\langle \zeta_{\vec{k}_1} \zeta_{\vec{k}_2} \zeta_{\vec{k}_3} \rangle = (2\pi)^3 \delta^3 (\vec{k}_1 + \vec{k}_2 + \vec{k}_3) B_{\zeta}(k_1, k_2, k_3)$
- Trispectrum  $\langle \zeta_{\vec{k}_1} \zeta_{\vec{k}_2} \zeta_{\vec{k}_3} \zeta_{\vec{k}_4} \rangle$ =  $(2\pi)^3 \delta^3 (\vec{k}_1 + \vec{k}_2 + \vec{k}_3 + \vec{k}_4) T_{\zeta} (k_1, k_2, k_3, k_4)$ 
  - Translational invariance  $\rightarrow \delta^3(\sum \vec{k_i})$
  - Rotational invariance  $\rightarrow P_{\zeta}(k_1), B_{\zeta}(k_1, k_2, k_3), B_{\zeta}(k_1, k_2, k_3, k_4), \text{etc.}$

 $K_1$ 

 $k_4$ 

 $k_2$ 

'Shape' of non-Gaussianities

# Non-Gaussianities (bispectrum)

- Different profiles corresponding to different shapes
  - Local:

 $B_{\zeta}^{\text{local}}(k_1, k_2, k_3) = \frac{6}{5} f_{\text{NL}}^{\text{local}} \Big[ P_{\zeta}(k_1) P_{\zeta}(k_2) + P_{\zeta}(k_2) P_{\zeta}(k_3) + P_{\zeta}(k_3) P_{\zeta}(k_1) \Big]$ generated at superhorizon in multifield inflation models

- Equilateral
- Orthogonal
- Other types (warm, flat, etc.)  $f_{\rm NL}^{\rm local} = 0.8 \pm 5.0, \quad f_{\rm NL}^{\rm equil} = -4 \pm 43, \quad f_{\rm NL}^{\rm ortho} = -26 \pm 21$ [Planck (2015)]

### **Constructing SUSY Higgs inflation**

(example in SUSY seesaw [Arai, SK, Okada, arXiv:1112.2391, 1212.6828]) Superpotential

 $W = \mu H_u H_d + y_u u^c Q H_u + y_d d^c Q H_d + y_e e^c L H_d + y_D N_R^c L H_u + M N_R^c N_R^c$ 

MSSM

**D**-flat direction

$$L = \frac{1}{\sqrt{2}} \begin{pmatrix} \varphi \\ 0 \end{pmatrix}, H_u = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \varphi \end{pmatrix}.$$

Kähler potential

 $K = -3 \ln \Phi, \qquad \text{nonminimal coupling } \xi R \varphi^2, \xi = \gamma/4 - \frac{1}{6}$   $\Phi = 1 - \frac{1}{3} (|N_R^c|^2 + |\varphi|^2) + \frac{1}{4} \gamma(\varphi^2 + c.c.) + \frac{1}{3} v |N_R^c|^4$ 

Seesaw relation

controls tachyonic instability

$$m_{\nu} = \frac{y_D^2 \langle H_u \rangle^2}{M}$$

 $m_{\nu}^2 \approx \Delta_{32}^2 = 2.43 \times 10^{-3} \text{eV}^2 \quad \langle H_u \rangle \approx 174 GeV$ 

Large enough  $v \Rightarrow$  single field inflation



yd can be naturally small

#### Constructing Supersymmetric Higgs inflation



Economist World politics Business & finance Economic

### Cosmology **BICEP** unflexed

ore from The Economist My Subscription

The

One of last year's most talked-about scien Feb 7th 2015 | From the print edition



OW many astronomers does it take to nail a coffin shut? entists—one the masters of Planck, an orbiting telescop ace Agency; the other the team bobind Diorne



Weath

### Prediction in the single-field limit & Planck/BICEP2 (2014)



### Noncanonical (quartic) term in Kähler $\Rightarrow$ N<sub>R</sub> =0 $\Rightarrow$ Single-field inflation

#### **Purpose:**

investigate how the multi-field effects (e.g. non-Gaussianity) restricts Kähler potential of the underlying supergravity theory

$$\Phi = 1 - \frac{1}{3}(|N_R^c|^2 + |\varphi|^2) + \frac{1}{4}\gamma(\varphi^2 + c.c.) + \frac{1}{3}v|N_R^c|^4$$

# Inflaton trajectories

#### (2-field SUSY Higgs inflation in SUSY seesaw)



red: Sinit =0, yellow: Sinit = 1.617×10<sup>-11</sup>, orange: Sinit = 10<sup>-5</sup> quantum fluctuations sinit =0 in all cases  $\langle (\Delta s)^2 \rangle \approx \frac{H^2}{\langle \Omega \rangle}$ 

- Seesaw mass M =1TeV, e-folding number N =60
- *h*<sub>init</sub> set by N = 60 in the single field limit
- Trajectory dep on the parameter *v* and the init cond (sinit, sinit)
- Once trajectory is fixed, observables can be computed

(we used the backward  $\delta N$  [Yokoyama Suyama Tanaka])

### Scalar power spectrum As



 $A_s \times 10^9 = 2.23 \pm 0.16$  (Planck)

$$k_0 = 0.05 \,\mathrm{Mpc}^{-1}$$

Quantum fluctuations give  $\langle \Delta s \rangle \approx \frac{H}{2\pi} \sim 10^{-5} M_{\rm Pl}$ 

for the seesaw mass M = 1 TeV, e-folding number N = 60



## **Non-Gaussianity (nonlinearity)** *f*<sub>NL</sub>

20

15

10

5

0

 $f_{\rm NL}^{(4)}$ 

 $\langle \zeta_{\boldsymbol{k}_1} \zeta_{\boldsymbol{k}_2} \zeta_{\boldsymbol{k}_3} \rangle = (2\pi)^3 \delta^3 \left( \boldsymbol{k}_1 + \boldsymbol{k}_2 + \boldsymbol{k}_3 \right) B_{\zeta}(k_1, k_2, k_3)$ 

$$B_{\zeta}(k_1, k_2, k_3) = \frac{6}{5} f_{NL}^{\text{local}} \left\{ P_{\zeta}(k_1) P_{\zeta}(k_2) + 2 \text{ perms} \right\}$$

**Observation (Planck 2013):** 

 $f_{\rm NL}^{\rm local} = 2.7 \pm 5.8$ 

(68% C.L.)



### Scalar spectral index ns

$$\mathcal{P}_S = A_s \left(\frac{k}{k_0}\right)^{n_s - 1 + \frac{1}{2}\frac{dn_s}{d\ln k}\ln\frac{k}{k_0} + \cdots}$$

**Observation (Planck 2013):** 

 $n_s = 0.9603 \pm 0.0073$  (68% C.L.)





### Tensor amplitude At and tilt nt

- No effects of multi-field on the tensor mode
- This is expected: tensor mode generated quantum mechanically at subhorizon, decouple from scalar mode
- Gravitational waves are same as in the single-field case



### Tensor/scalar ratio r = At/As

- Multi-field: As enhanced, whereas At stays constant
- The ratio r = At /As suppressed by the multifield effects





Sinit

### As, fNL and ns

• Planck (2013):

| $A_s = (2.23 \pm 0.16) \times 10^{-9}$ | (68% C.L.),  |
|--|--------------|
| $n_s = 0.9603 \pm 0.0073$              | (68%  C.L.), |
| r < 0.12                               | (95% C.L.),  |
| $f_{ m NL}^{ m local} = 2.7 \pm 5.8$   | (68% C.L.).  |

 Recall: quantum fluctuation gives Δs ~ 10<sup>-5</sup>



 $4.5 \times 10^{-9}$ 

 $4. \times 10^{-9}$ 

 $3.5 \times 10^{-9}$ 

 $2.5 \times 10^{-9}$ 

 $2. \times 10^{-9}$ 

 $1.5 \times 10^{-9}$  L \_ \_ \_ \_ \_ \_ 0.060

20

15

10

5

 $f_{\rm NL}^{(4)}$ 

0.062 0.064

0.066 0.068

υ

₹ 3.×10<sup>-9</sup>

 $s_{\text{init}}=0$ 

-  $s_{init} = 10^{-7}$ 

-  $s_{\text{init}} = 10^{-6}$ 

 $s_{init} = 10^{-5}$ 

0.070 0.072 0.074

 $s_{\text{init}}=0$ 

 $s_{\text{init}}=10^{-7}$ 

 $- s_{init} = 10^{-6}$ 

•  $s_{\text{init}} = 10^{-5}$ 

# Inflation in SUSY-seesaw

- Multi-field dynamics potentially important
- Planck constraints on non-Gaussianities restricts Kähler potential of supergravity
- NMSSM inflation model is similar

### Higgs inflation in GUT

- Inflation ~ GUT scale  $\gg$  SM (EW) scale
- Hierarchy problem, gauge coupling unification ⇒ super GUT
- Simplest: SU(5)
- This is a revival of inflation models in the 80s, now with nonminimal coupling
- Enough e-folding number? Spectral index? Scalar-tensor ratio?
- SM after the inflation? Phenomenological consistency (DM, baryogenesis, gravitino problem...)?

#### SU(5) grand unification

Gauge field

$$\begin{array}{cccc} \mathbf{24} = (\mathbf{8}, \mathbf{1}, 0) + (\mathbf{1}, \mathbf{3}, 0) + (\mathbf{1}, \mathbf{1}, 0) + (\mathbf{3}, \mathbf{2}, \frac{5}{3}) + (\overline{\mathbf{3}}, \mathbf{2}, -\frac{5}{3}) \\ g & A^a_\mu \to W^a_\mu & B_\mu & X_{\alpha\mu}, Y_{\alpha\mu} & \overline{X}_{\alpha\mu}, \overline{Y}_{\alpha\mu} \end{array}$$

• Fermion fields

$$\begin{array}{c|c} \mathbf{10} = (\mathbf{1}, \mathbf{1}) + (\mathbf{\bar{3}}, \mathbf{1}) + (\mathbf{3}, \mathbf{2}) \\ \hline e & \overline{u} & Q = (u_L, d_L) \\ \hline \mathbf{\bar{5}} = (\mathbf{\bar{3}}, \mathbf{1}) + (\mathbf{1}, \mathbf{2}) \\ \hline d & L = (e, \nu_e) \\ \hline \cdot \text{ Scalar fields} \end{array}$$

 $\begin{array}{lll} \textbf{24} & \text{GUT Higgs} & SU(5) \rightarrow SU(3) \times SU(2) \times U(1) \\ \textbf{5} = (\textbf{3}, \textbf{1}, -\frac{2}{3}) + (\textbf{1}, \textbf{2}, 1) & \text{Colour Higgs} + \text{SM Higgs} \end{array}$ 

#### Minimal SUSY SU(5) model

• Vector multiplet

#### **24** of SU(5)

Chiral multiplets





### Higgs inflation of minimal SUSY SU(5) GUT

• The superpotential

$$W = \overline{H} \left( \mu + \rho \Sigma \right) H + \frac{m}{2} \operatorname{Tr}(\Sigma^2) + \frac{\lambda}{3} \operatorname{Tr}(\Sigma^3)$$

The Kähler potential

$$\Phi = 1 - \frac{1}{3} \left( \operatorname{Tr} \Sigma^{\dagger} \Sigma + |H|^{2} + |\overline{H}|^{2} \right) - \frac{\gamma}{2} \left( \overline{H}H + H^{\dagger} \overline{H}^{\dagger} \right)$$
$$+ \frac{\tilde{\omega}}{3} \left( \operatorname{Tr} \Sigma^{\dagger} \Sigma^{2} + \operatorname{Tr} \Sigma^{\dagger 2} \Sigma \right) + \frac{\zeta}{3} \left( \operatorname{Tr} \Sigma^{\dagger} \Sigma \right)^{2}$$

#### Phenomenological constraints

Gauge symmetry broken to SU(3) x SU(2) x U(1)

$$\Sigma = \sqrt{\frac{2}{15}} S \operatorname{diag}\left(1, 1, 1, -\frac{3}{2}, -\frac{3}{2}\right)$$

• The superpotential is

Colour unbroken  $\Rightarrow \langle H_c \rangle = \langle \overline{H}_c \rangle = 0$ 

$$M_{H_u}, M_{H_d} \ll M_{\rm GUT} \Rightarrow \mu = \sqrt{\frac{3}{10}} \rho \langle S \rangle$$

 $\sqrt{30}$ 

$$W = \left(\mu + \sqrt{\frac{2}{15}}\rho S\right)\overline{H}_cH_c + \left(\mu - \sqrt{\frac{3}{10}}\rho S\right)H_uH_d + \frac{m}{2}S^2 - \frac{\lambda}{3\sqrt{30}}S^3.$$

 $\delta S$ 

SU(5) broken  $\Rightarrow \langle S \rangle \equiv v = 2 \times 10^{16} \text{ GeV}$ 

### The SU(5) super GUT model [M.Arai, S.K. N.Okada 2011]

- Cubic + quartic terms in Kähler necessary
- Stable trajectory, SM vacuum
- No cosmological constant problem





# Prediction of the SU(5) GUT Higgs inflation



### SU(5) GUT Higgs inflation

... is identical to the single-field case. No large non-Gaussianities

# Why the SU(5) case different?

- Multifield effects (non-Gaussianity, isocurvature modes) arise from nontrivial nonlinear dynamics outside the horizon
- This is possible only when the inflaton trajectory stays on a ridge for long enough e-folds and then swerve off
- The potential of the SU(5) model needs to be asymmetric and such a trajectory is unlikely, even with fine-tuned initial conditions







- It's good time to think about the origin of the inflaton within "beyond the Standard Model" physics.
- Higgs inflation interesting. SUSY Higgs inflation perhaps more interesting.
- Avoid the η problem: non-canonical Kähler potential
- Multi-field signatures (e.g. non-Gaussianities) may be a clue to understand supergravity embedding of BSM.
- Analysed a concrete model based on SUSY seesaw & SU(5) GUT

# Summary

- It seems that that symmetries of the inflaton potential are crucial for the multifield effects
- In generic multifield inflation (e.g. in string landscape), no particular symmetries are expected, thus a single-field analysis is likely to be sufficient.



Thank you for your attention.