



Simplified Models for DM searches

M33 rotation curve

Thomas Jacques

arXiv:1502.05721, Nordstrom, TDJ

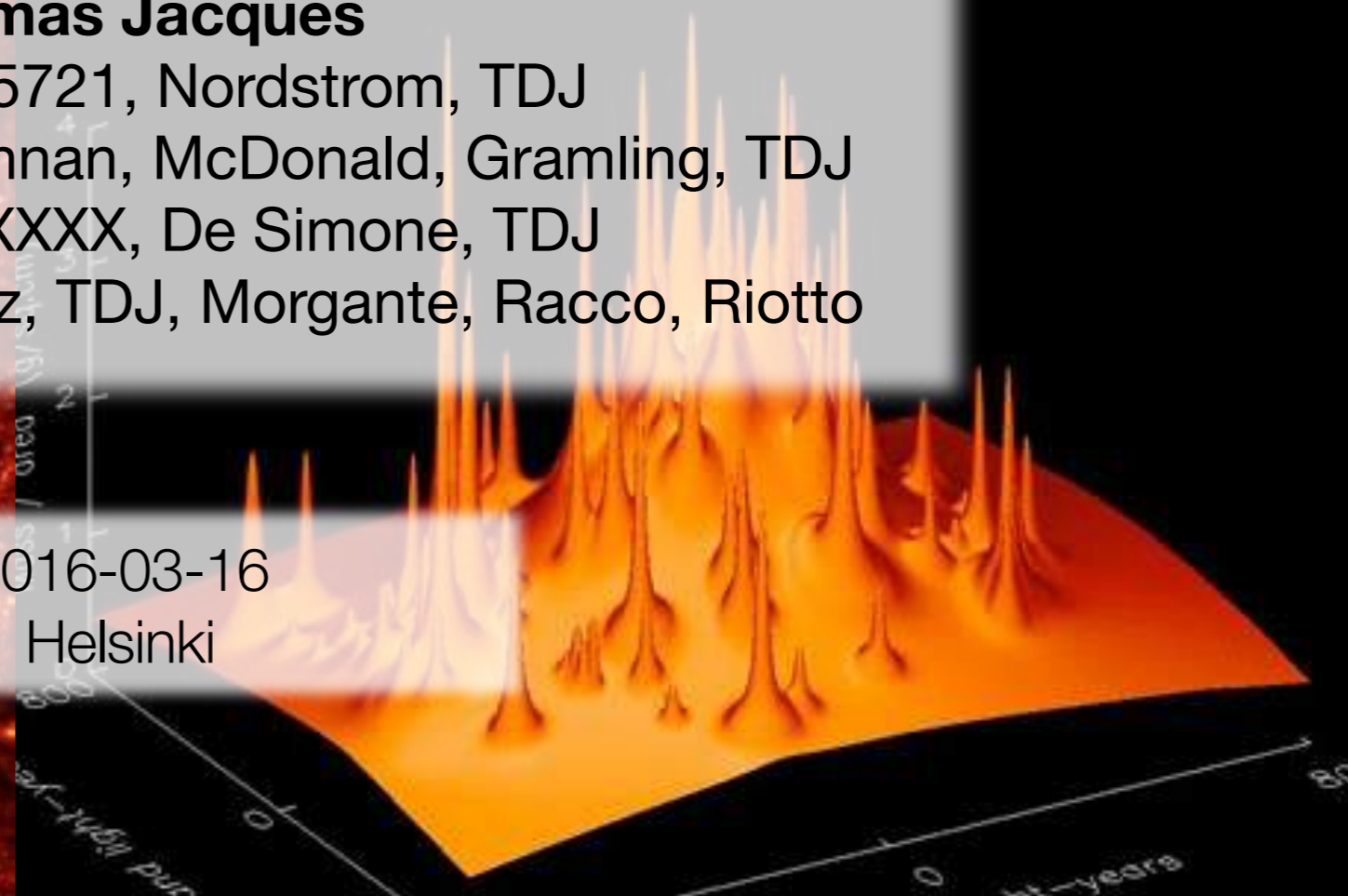
arXiv:1603.01366, Brennan, McDonald, Gramling, TDJ

arXiv:1603.XXXXX, De Simone, TDJ

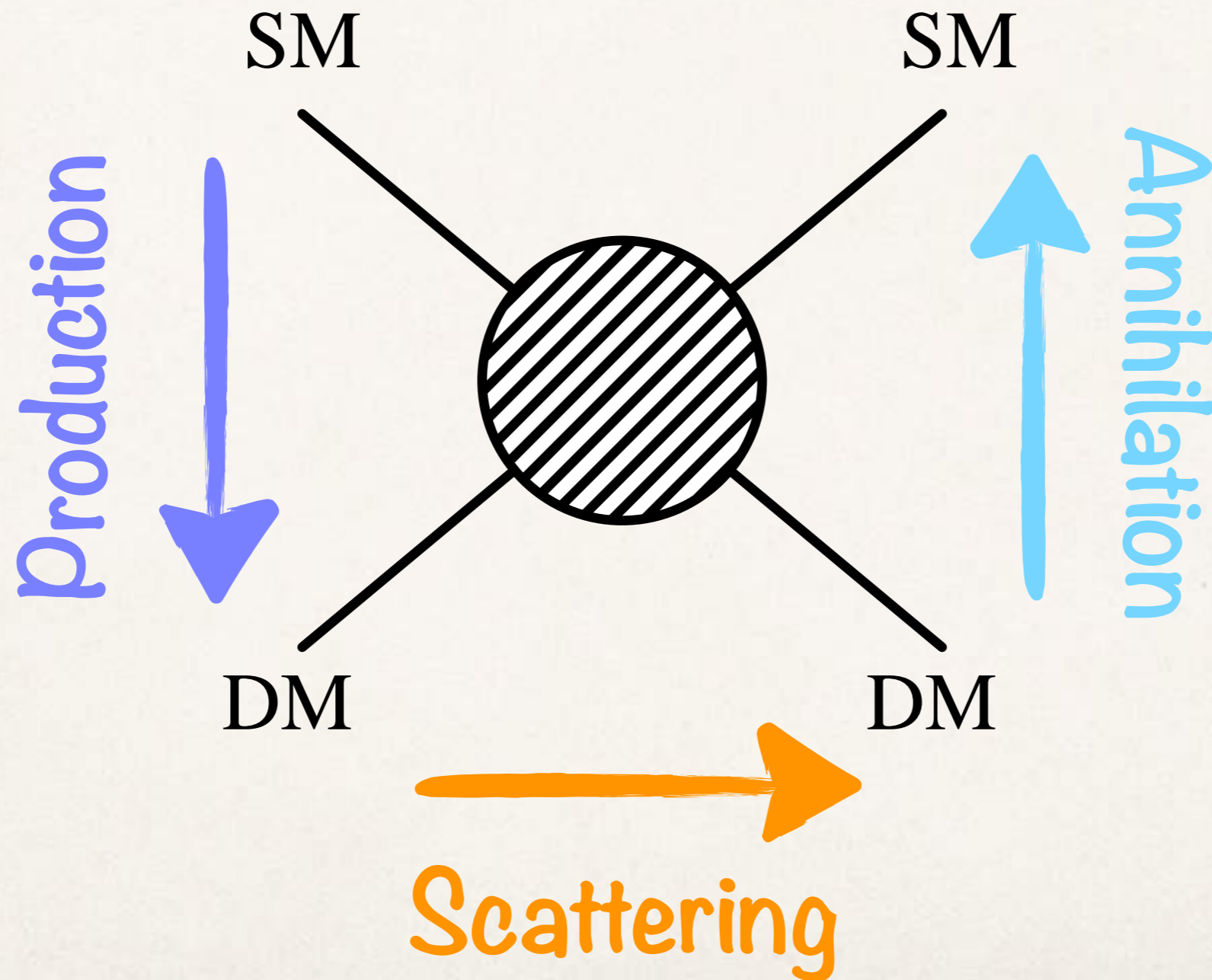
arXiv:160X.XXXXX, Katz, TDJ, Morgante, Racco, Riotto

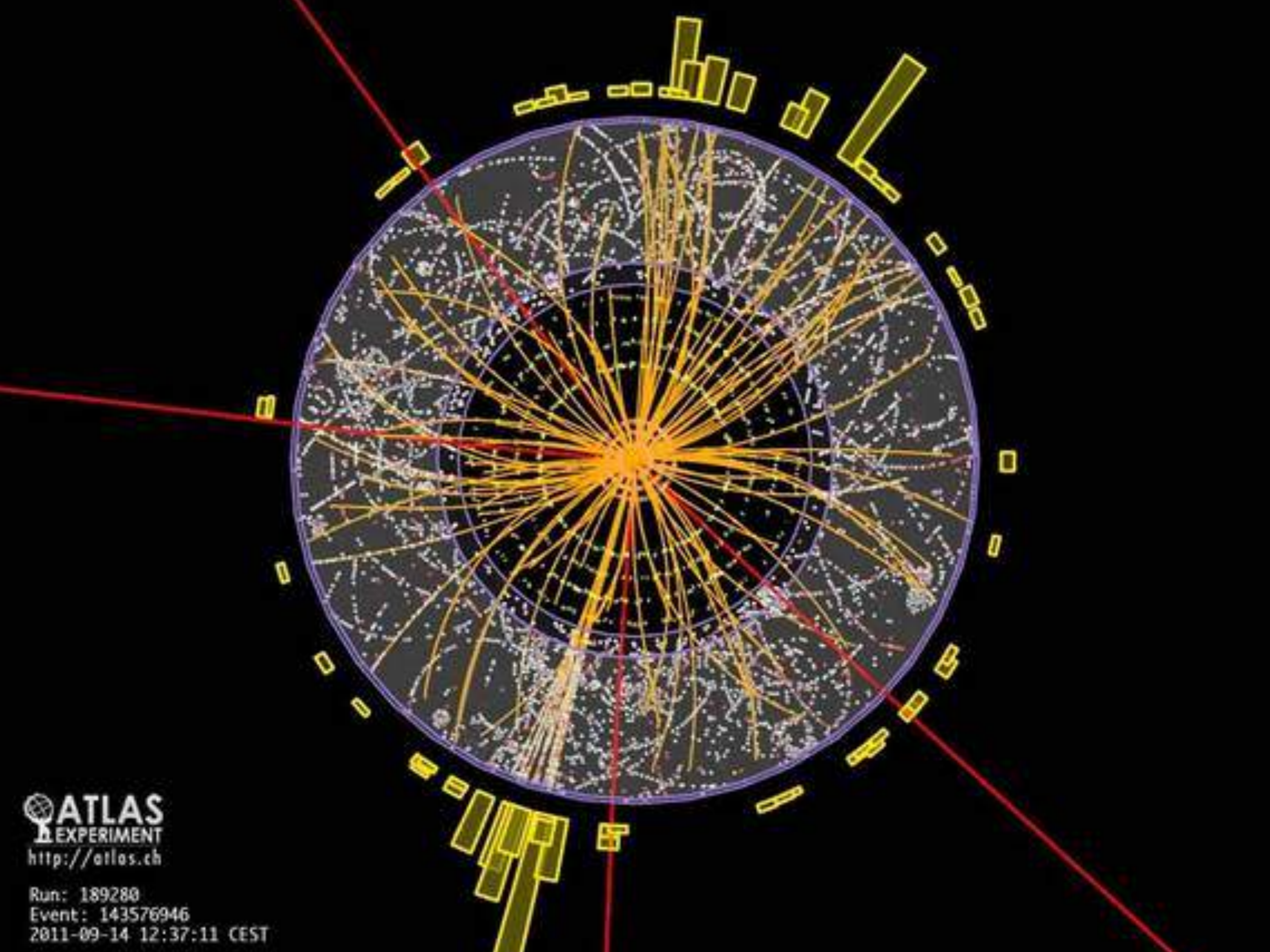
2016-03-16

Helsinki



Dark matter searches





ATLAS
EXPERIMENT
<http://atlas.ch>

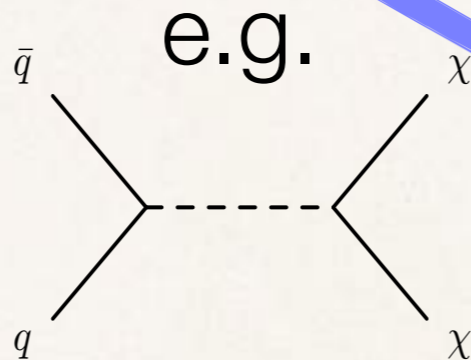
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What exactly are we constraining?

Effective operators

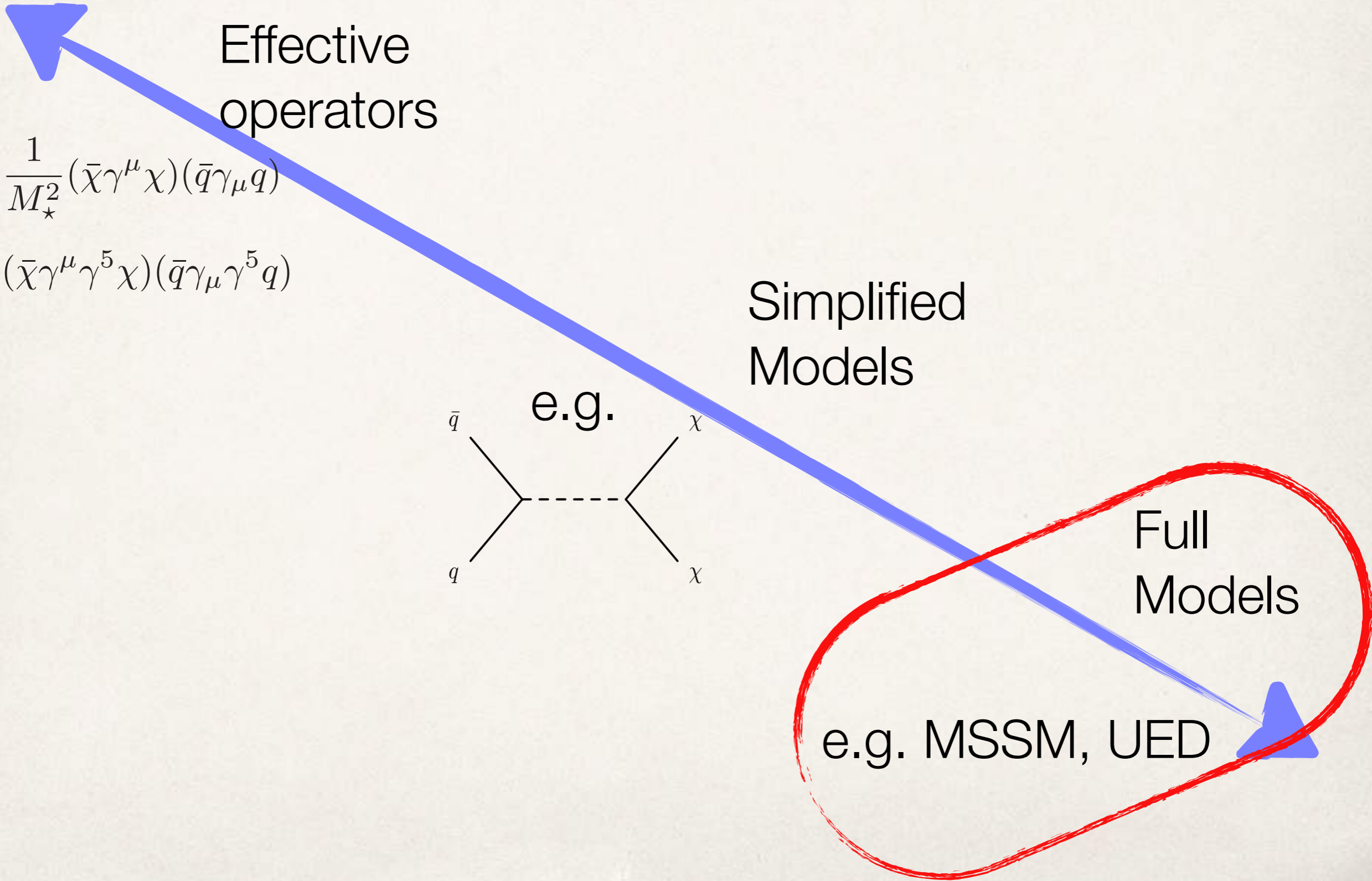
e.g. $\frac{1}{M_*^2} (\bar{\chi} \gamma^\mu \chi) (\bar{q} \gamma_\mu q)$
 $\frac{1}{M_*^2} (\bar{\chi} \gamma^\mu \gamma^5 \chi) (\bar{q} \gamma_\mu \gamma^5 q)$

Simplified Models



Full Models

e.g. MSSM, UED

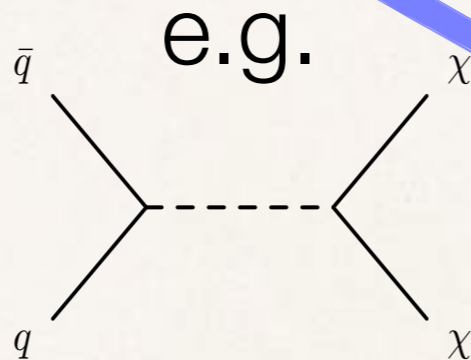


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Simplified Models



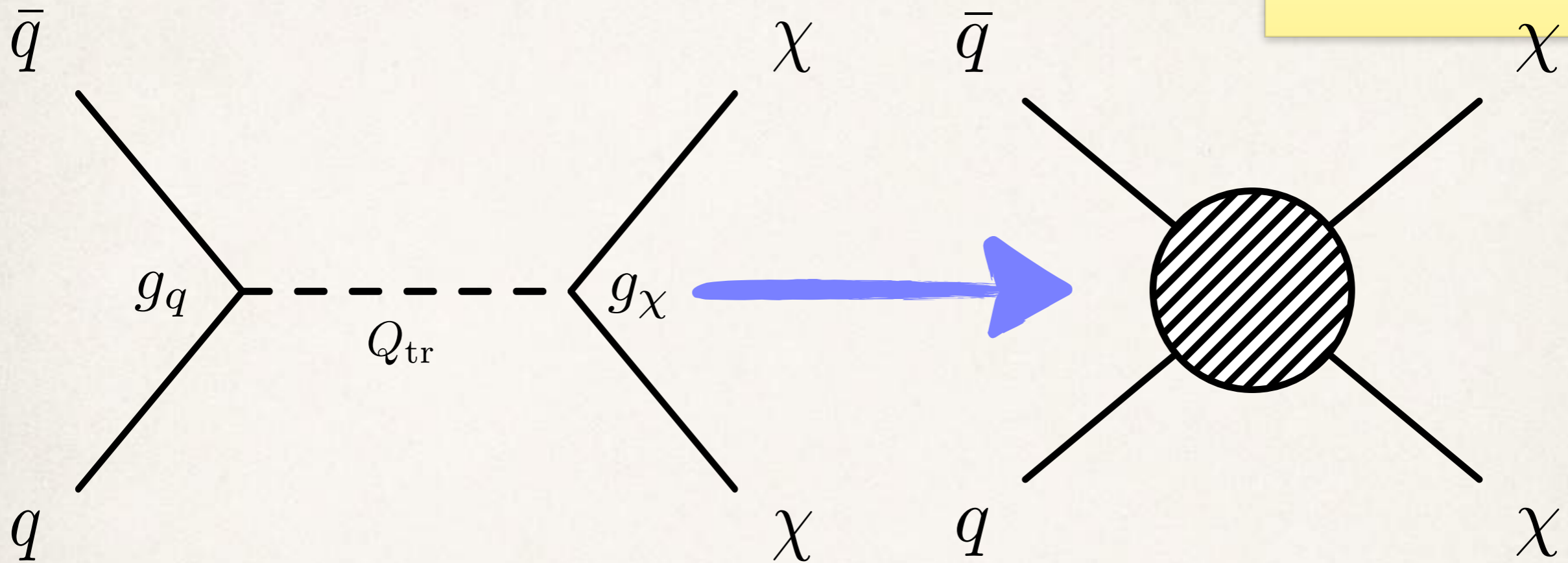
Full Models

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Effective operators

List of DD operators...



$$\frac{g_q g_\chi}{M^2 - Q_{\text{tr}}^2} \simeq \frac{g_q g_\chi}{M^2} \equiv \frac{1}{M_\star^2}$$

- Integrate out the mediator
- Reduce parameters to m_χ , M_\star for each operator

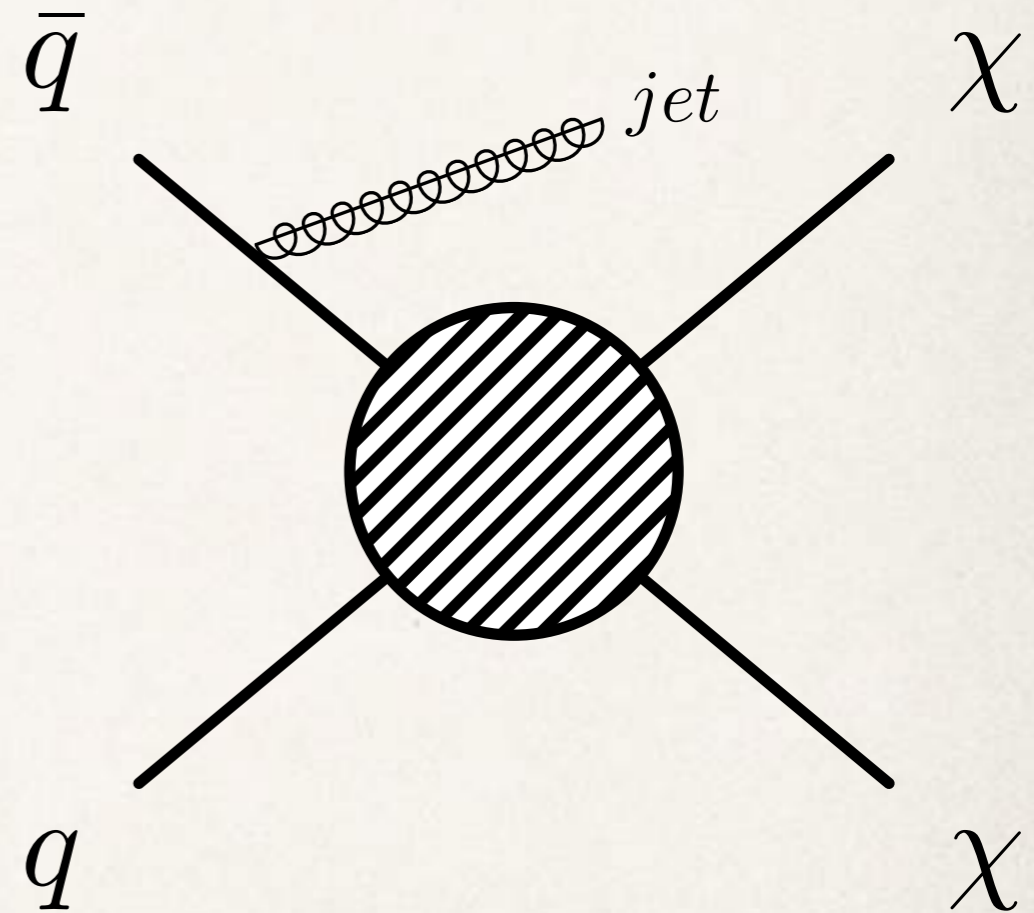
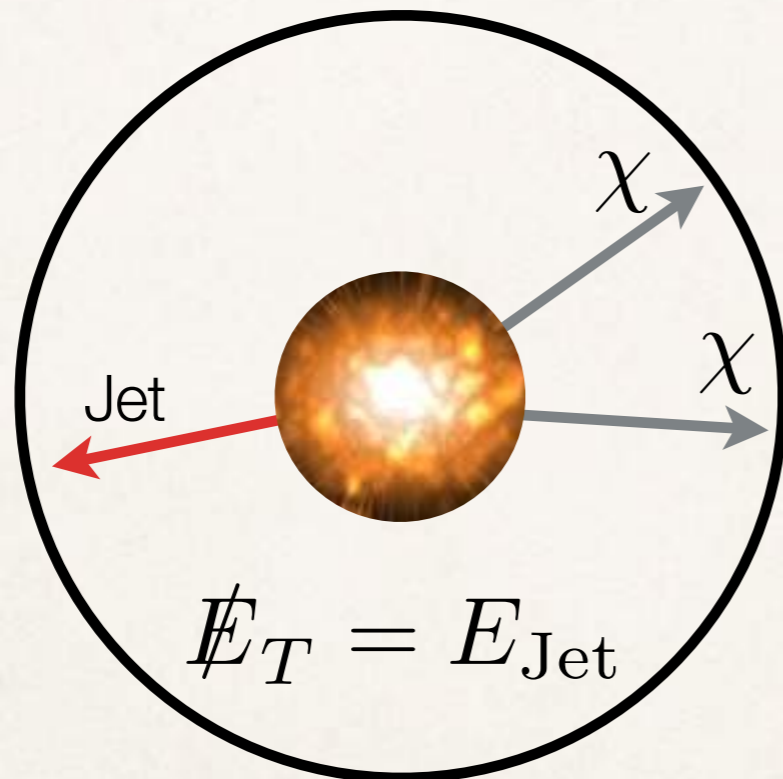
Effective operators

- Left with a small ‘basis’ set of operators
- Most common operators are for Dirac fermion WIMPs:

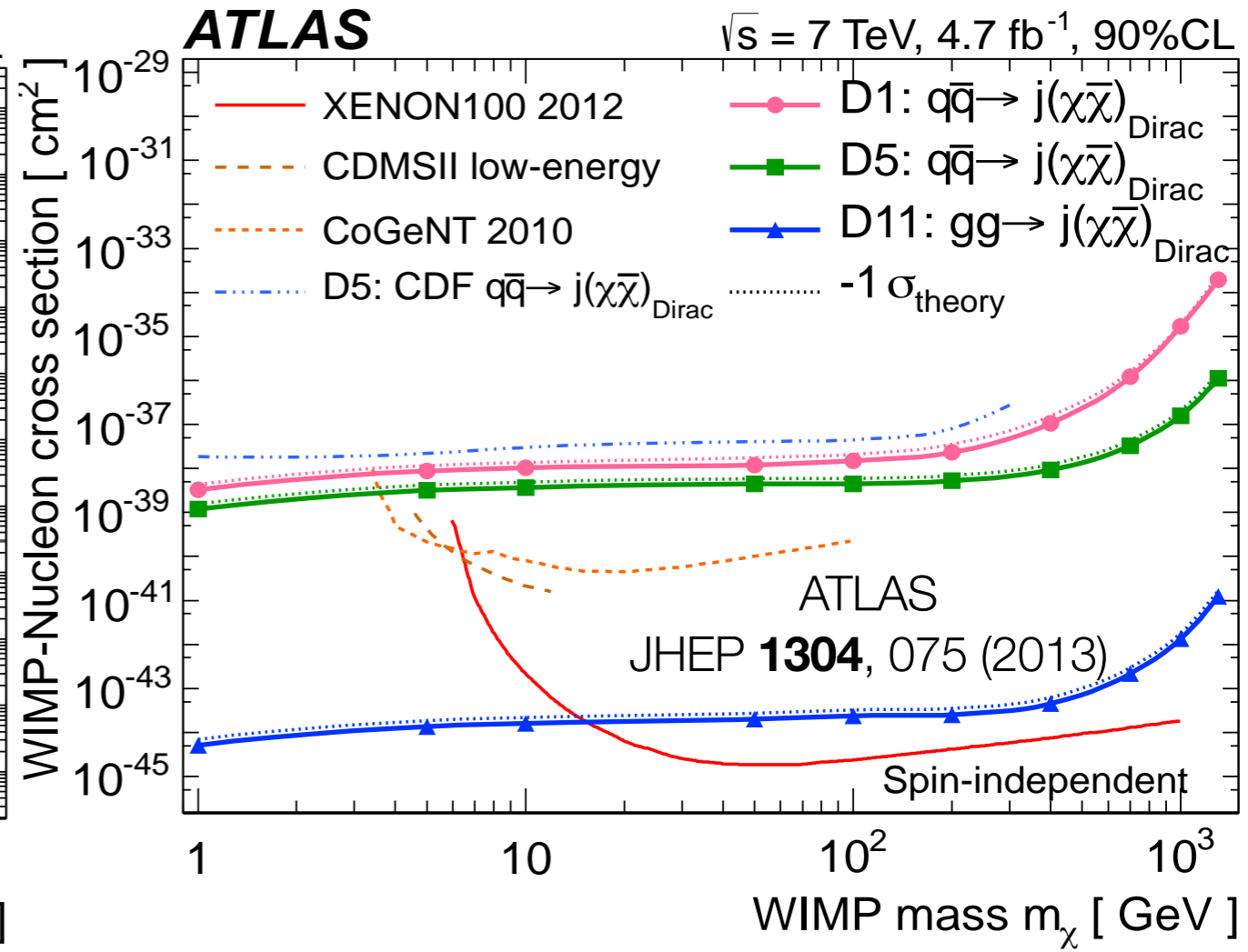
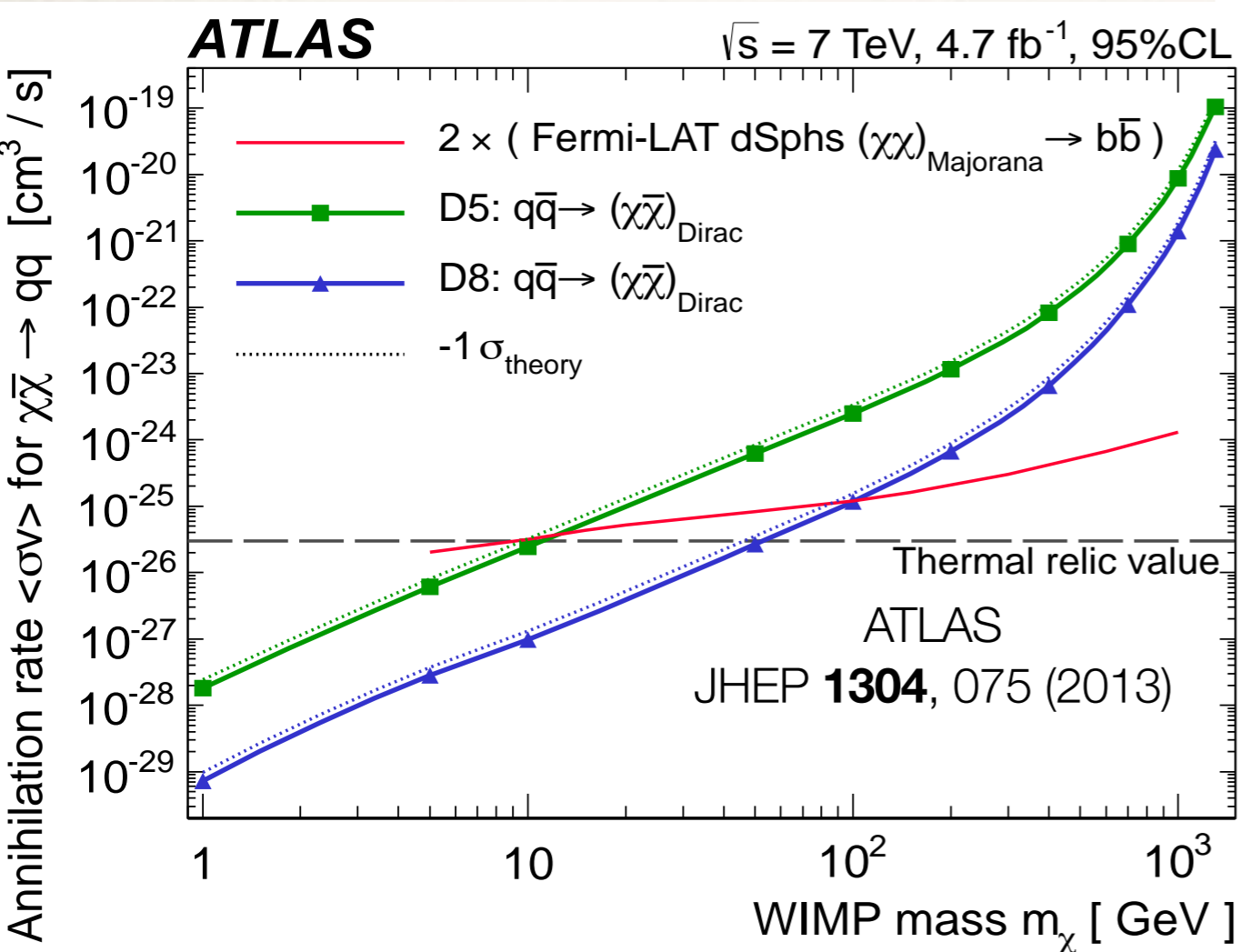
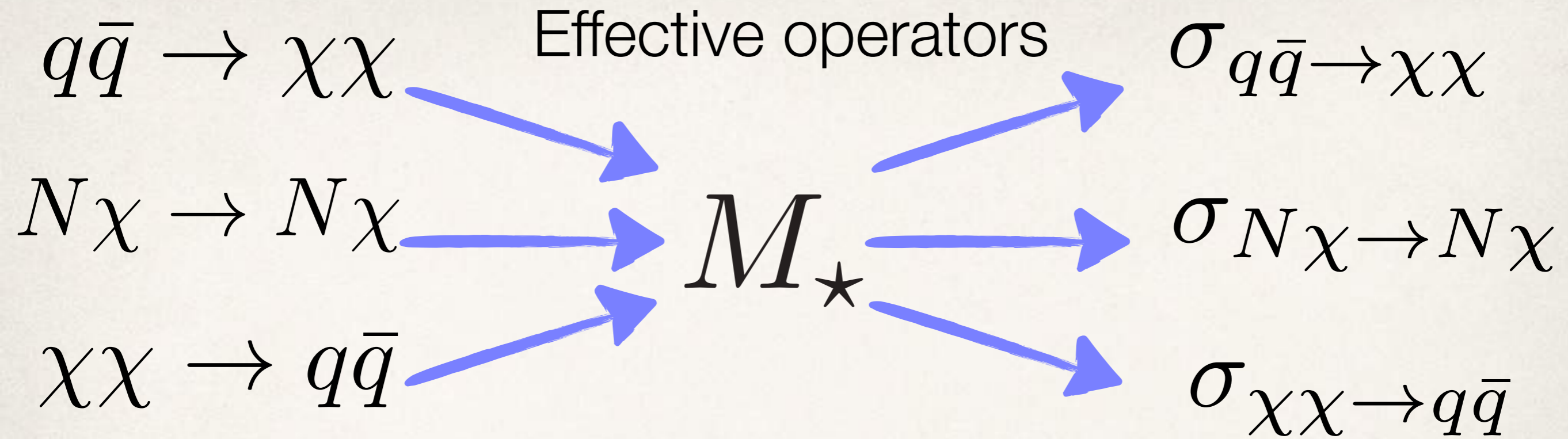
- scalar mediator-like coupling $D1 = \frac{m_q}{M_\star^3} (\bar{\chi}\chi)(\bar{q}q)$
- vector coupling $D5 = \frac{1}{M_\star^2} (\bar{\chi}\gamma^\mu\chi)(\bar{q}\gamma_\mu q)$
- axial-vector coupling $D8 = \frac{1}{M_\star^2} (\bar{\chi}\gamma^\mu\gamma^5\chi)(\bar{q}\gamma_\mu\gamma^5 q)$
- gluon initial state $D11 = \frac{i\alpha_S}{4M_\star^3} (\bar{\chi}\chi)(G_{\mu\nu}\tilde{G}^{\mu\nu})$

Search channels

- The most generic search channel is missing energy + jet(s): DM production inferred by non-zero transverse momentum sum



- Other channels can be important but they are more model-dependent

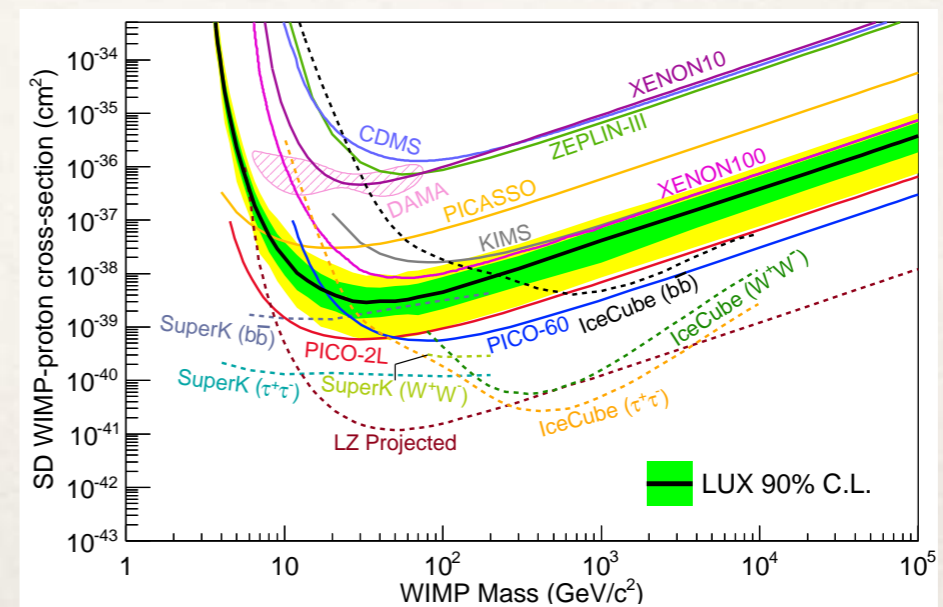
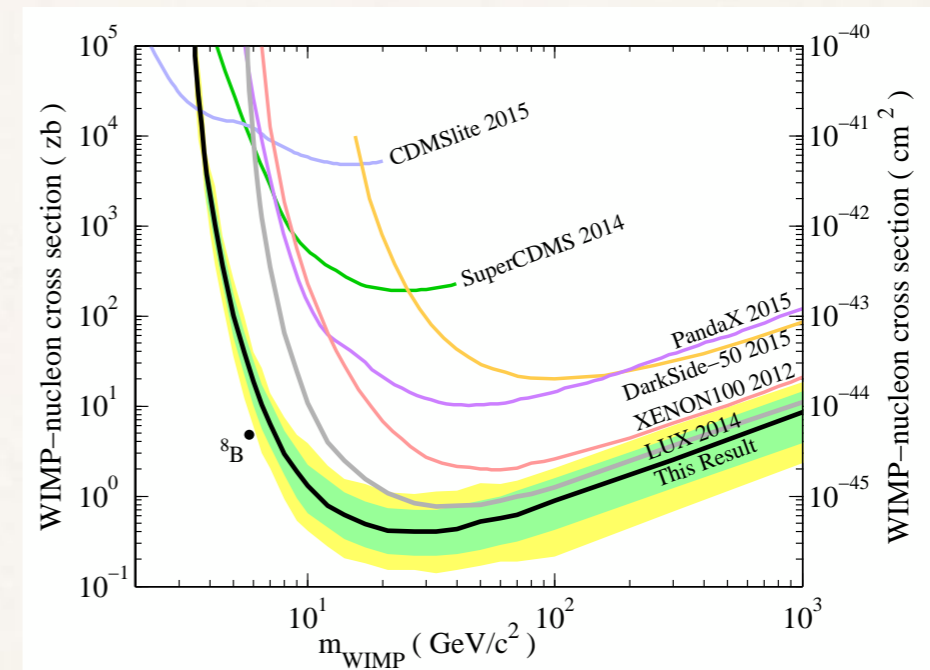


Effective operators for direct detection

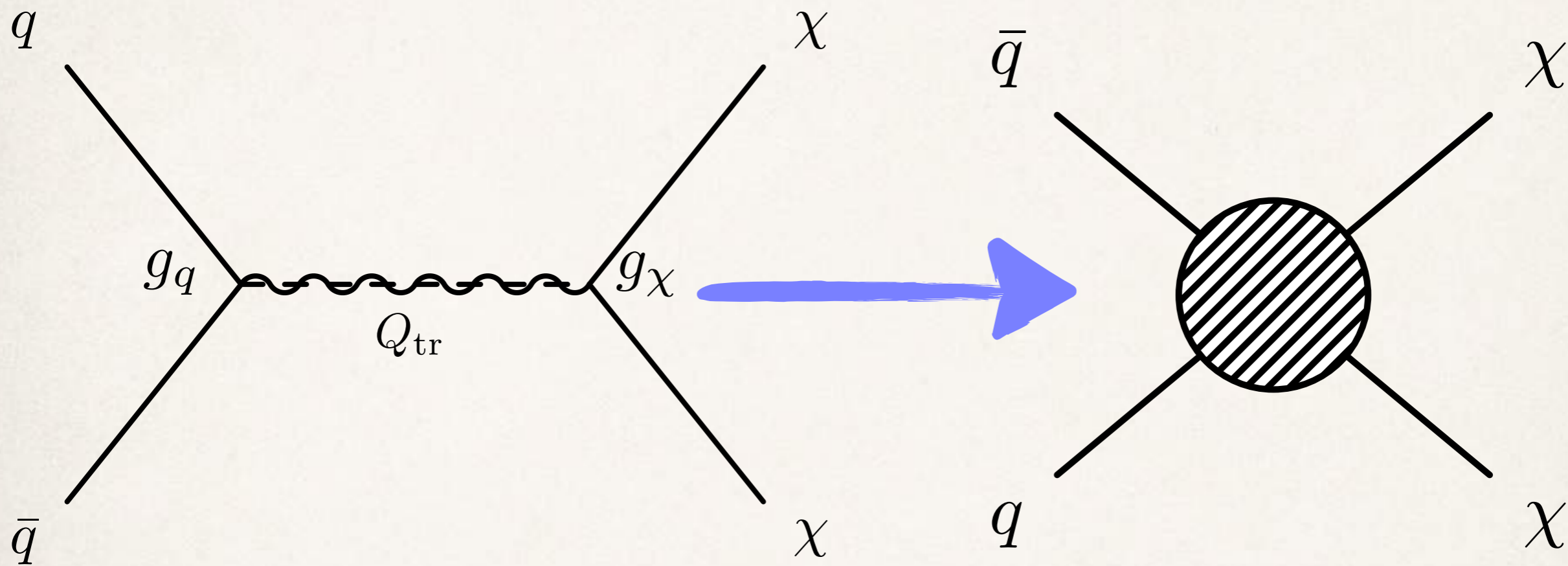
- Note that the ‘usual’ direct detection constraints on σ_{SI} and σ_{SD} are a constraint on some, not all effective operators

$$\left. \begin{array}{l} (\bar{\chi}\chi)(\bar{q}q) \\ (\bar{\chi}\gamma^\mu\chi)(\bar{q}\gamma_\mu q) \\ (\bar{\chi}\chi)(G_{\mu\nu}^a G_{\mu\nu}^a) \\ (\phi^*\phi)(\bar{q}q) \\ (\phi^*\overset{\leftrightarrow}{\partial}_\mu\phi)(\bar{q}\gamma^\mu q) \\ (\phi^*\phi)(G_{\mu\nu}^a G_{\mu\nu}^a) \end{array} \right\} \longleftrightarrow \sigma_{SI}$$

$$\left. \begin{array}{l} (\bar{\chi}\gamma^\mu\gamma^5\chi)(\bar{q}\gamma_\mu\gamma^5q) \\ (\bar{\chi}\sigma^{\mu\nu}\chi)(\bar{q}\sigma_{\mu\nu}q) \end{array} \right\} \longleftrightarrow \sigma_{SD}$$



Effective operators



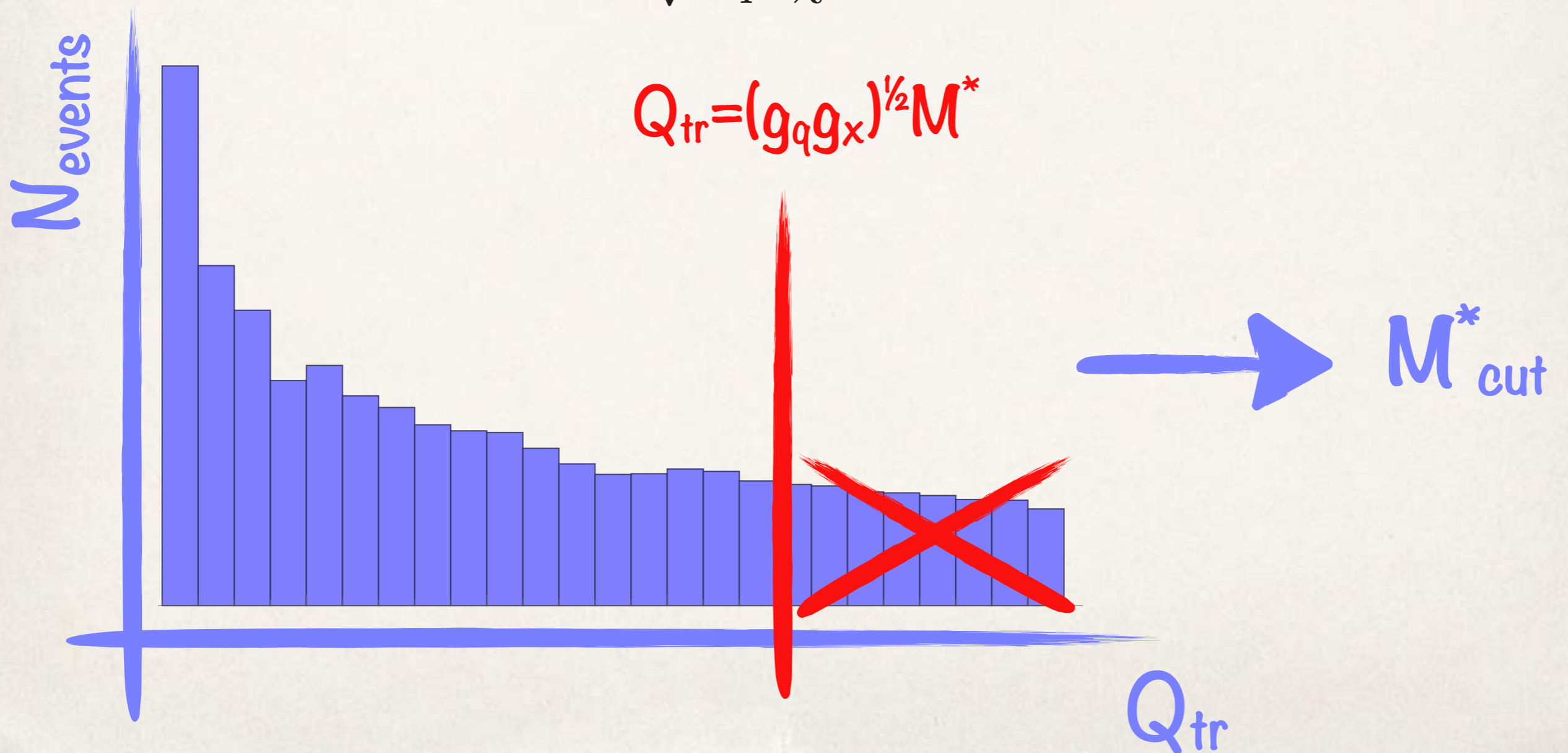
$$\frac{g_q g_\chi}{M^2 - Q_{\text{tr}}^2} \simeq \frac{g_q g_\chi}{M^2} \equiv \frac{1}{M_\star^2}$$

$$Q_{\text{tr}} < M \equiv \sqrt{g_q g_\chi} M_\star$$

Rescaling operator constraints

- For a given choice of $\sqrt{g_q g_\chi}$, only use events that satisfy

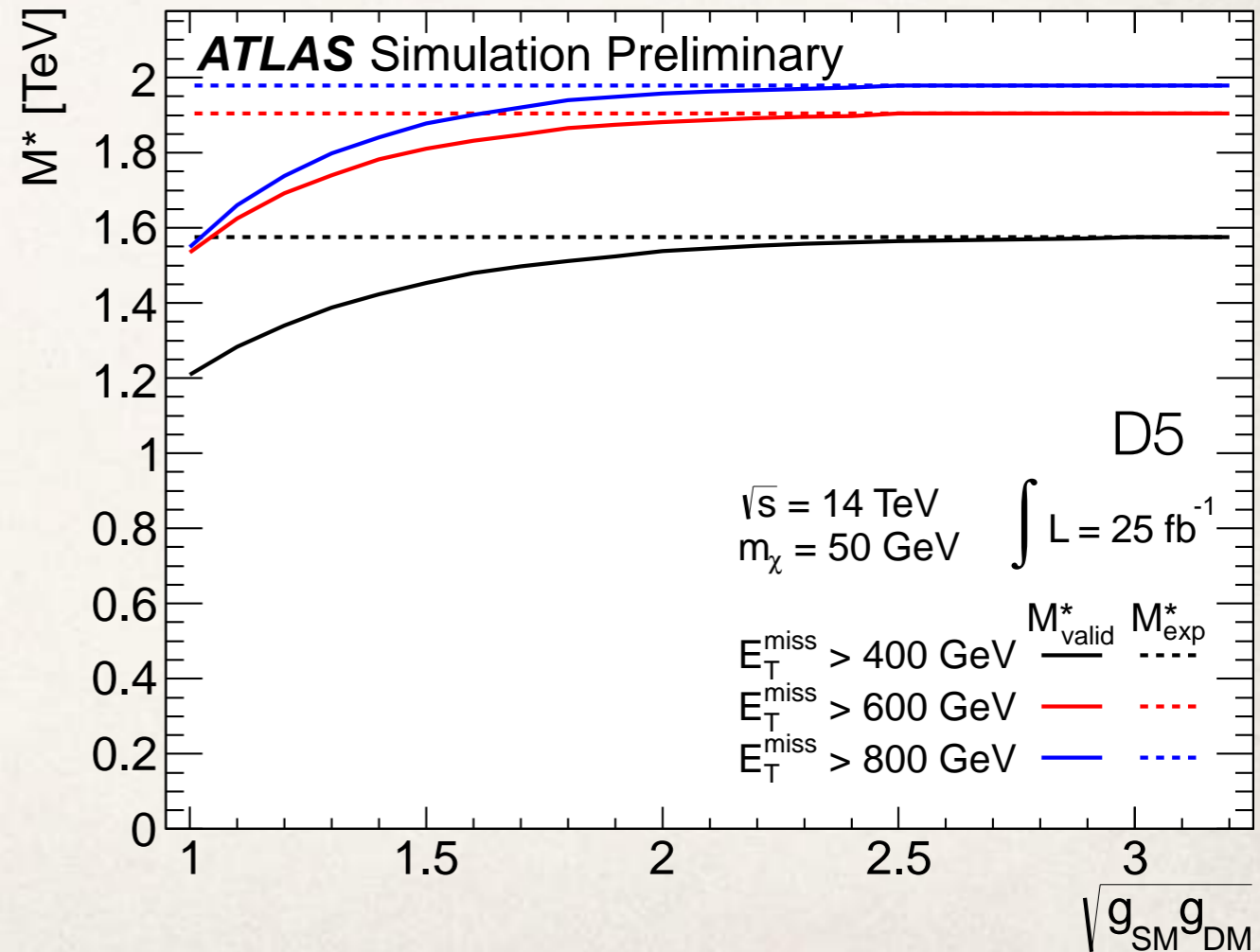
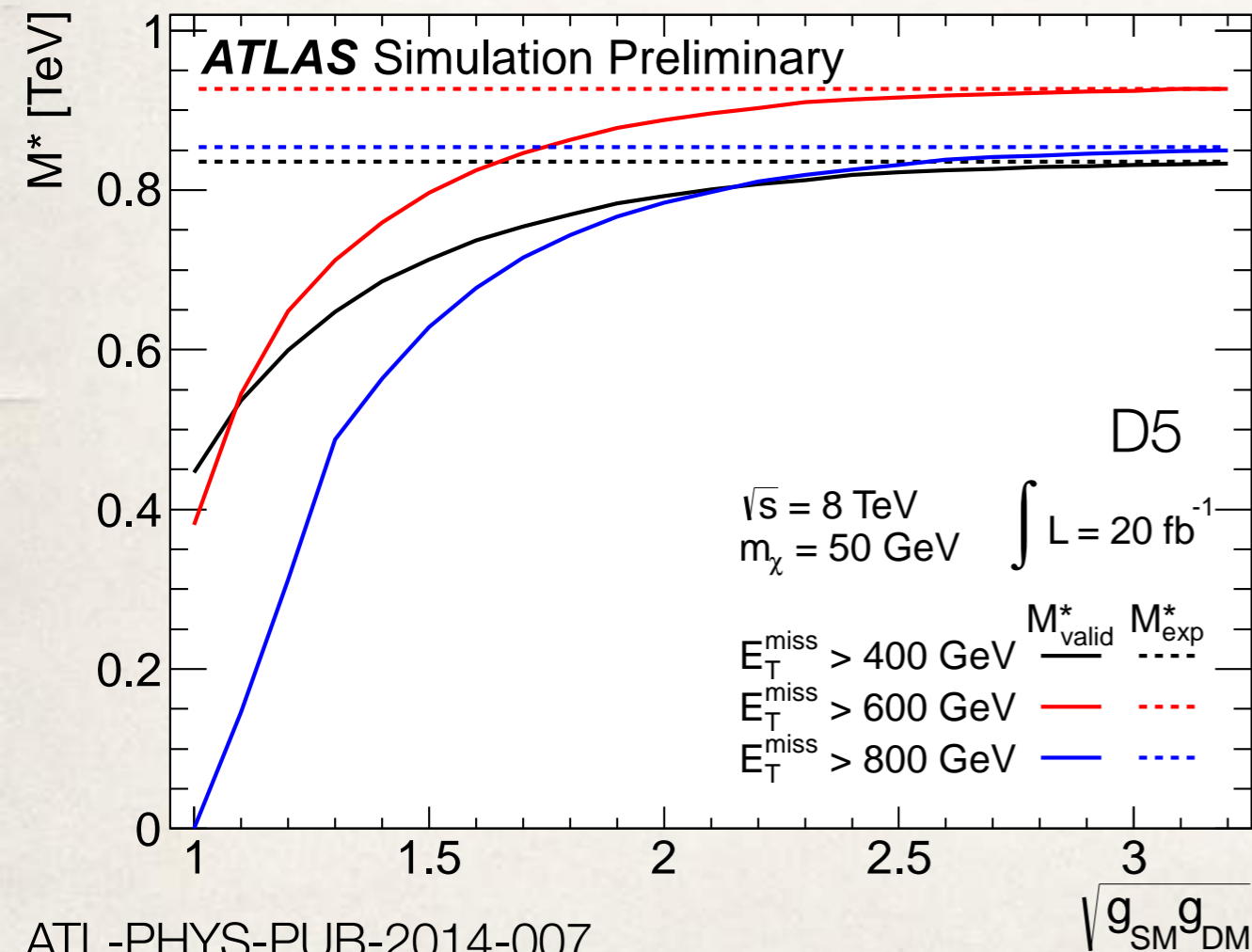
$$M \equiv \sqrt{g_q g_\chi} M^* \geq Q_{\text{tr}}$$



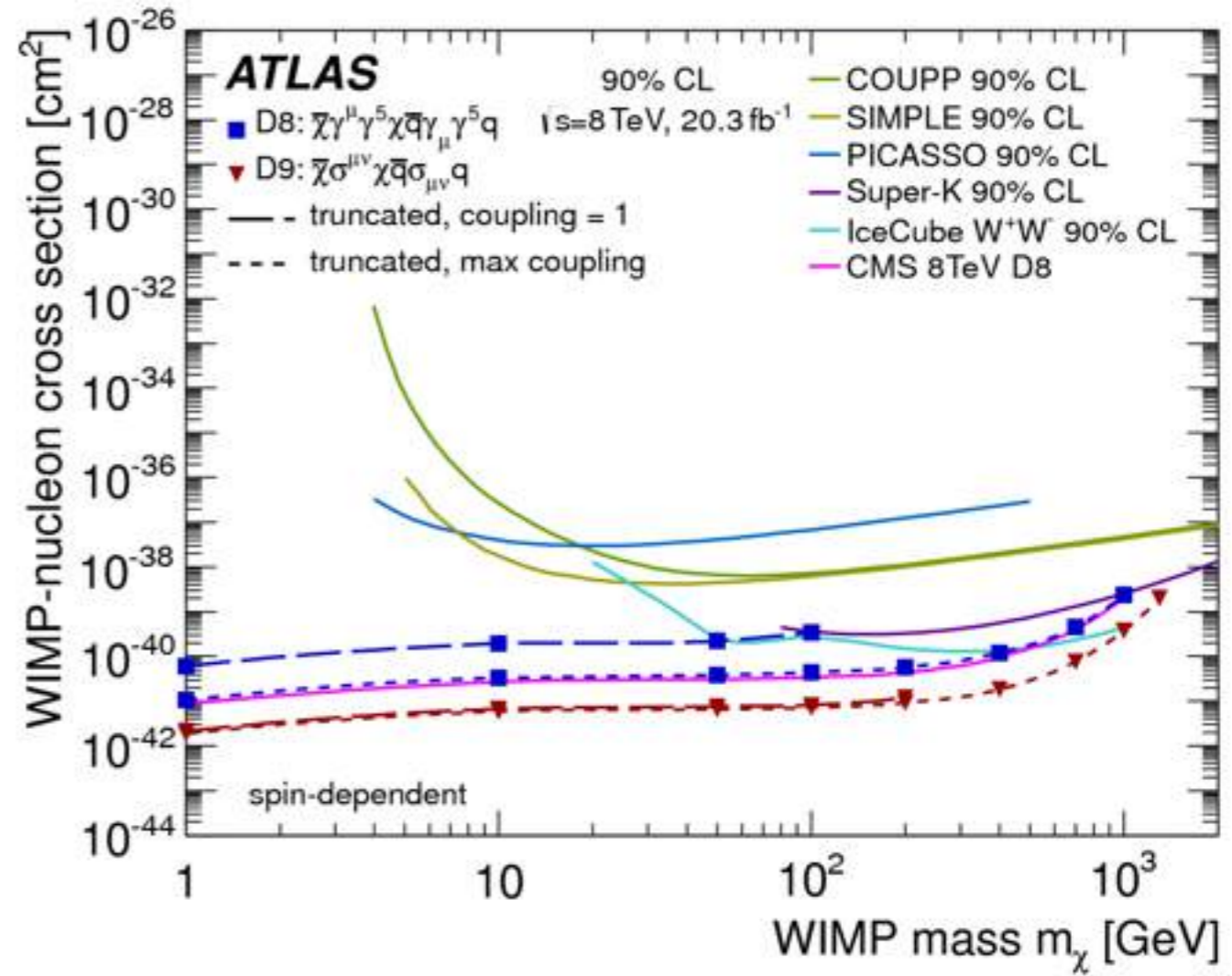
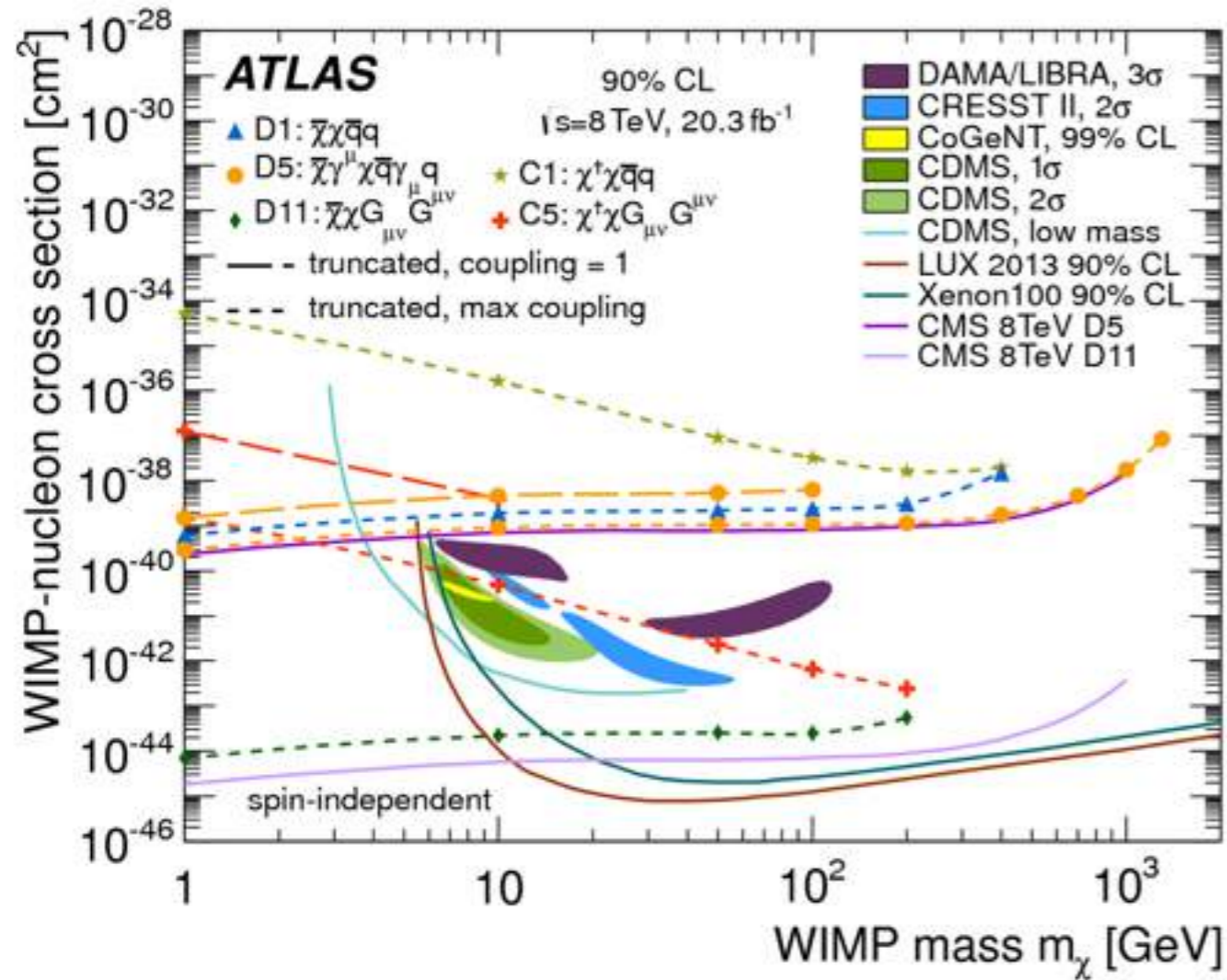
Rescaling operator constraints

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$$M \equiv \sqrt{g_q g_\chi} M^* \geq Q_{\text{tr}}$$



Rescaling operator constraints



Eur. Phys. J. C (2015) 75:299

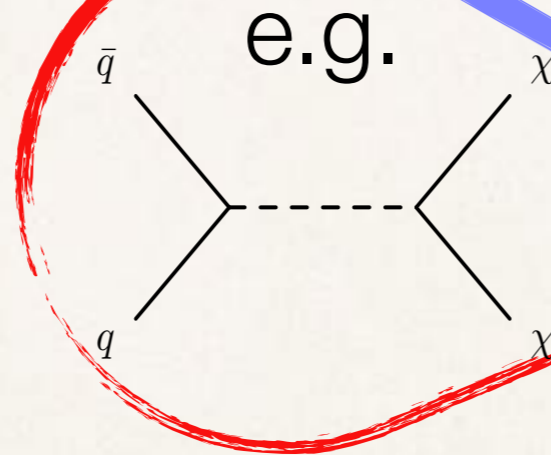
ATLAS + Busoni, De Simone, TDJ, Morgante, Riotto

So what now?

Effective operators

e.g. $\frac{1}{M_*^2} (\bar{\chi} \gamma^\mu \chi) (\bar{q} \gamma_\mu q)$
 $\frac{1}{M_*^2} (\bar{\chi} \gamma^\mu \gamma^5 \chi) (\bar{q} \gamma_\mu \gamma^5 q)$

Simplified Models



Full Models

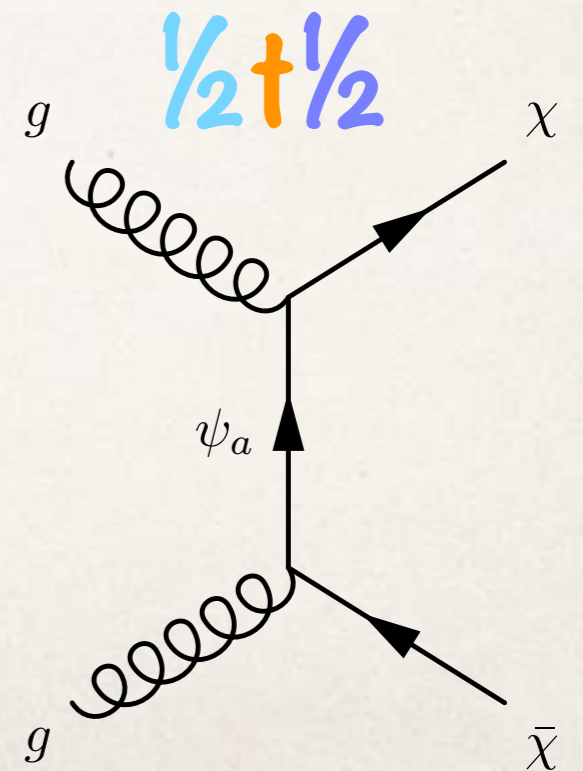
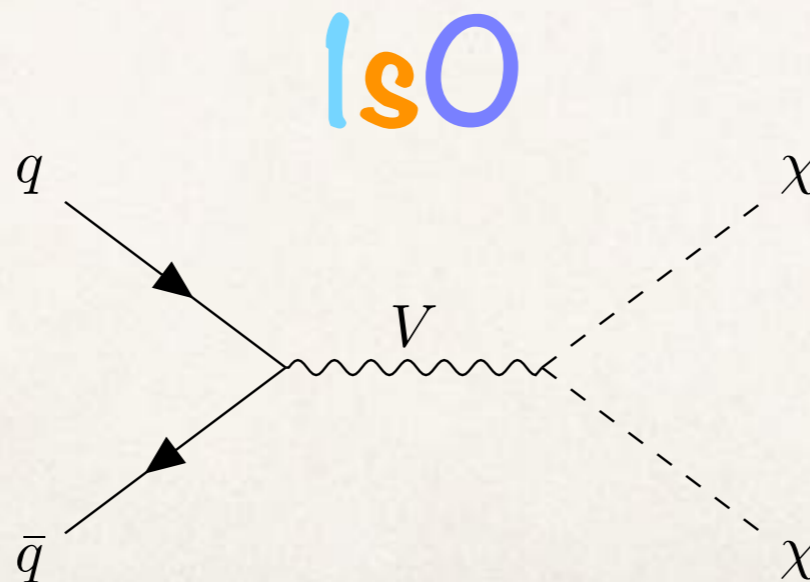
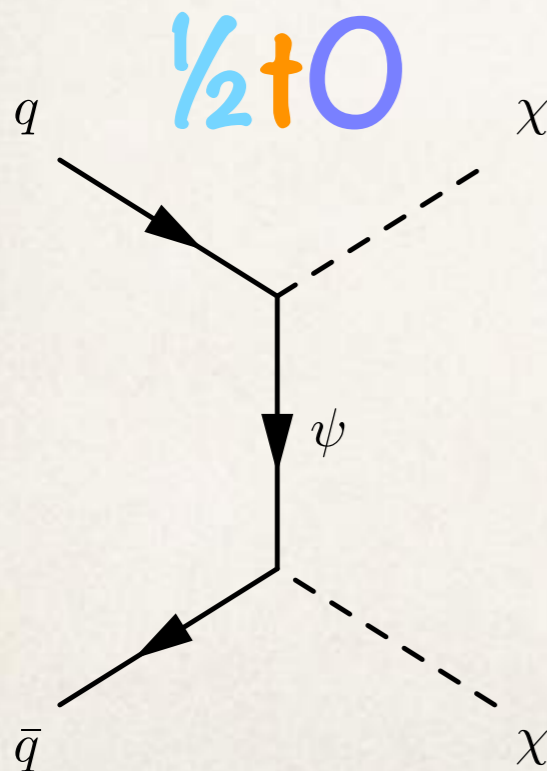
e.g. MSSM, UED

Classification of simplified models

- There are many simplified models to choose from and they can be organized in a logical way. The most important features are

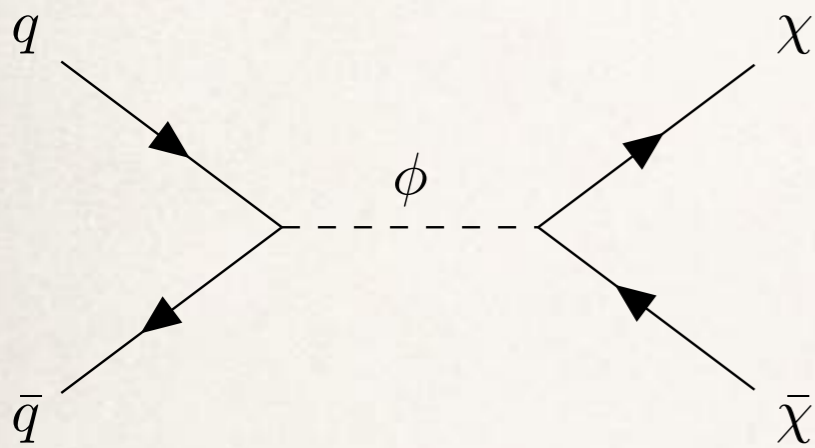
Mediator spin **Geometry of diagram** **DM spin**

- If DM is neutral, this defines most features of the model



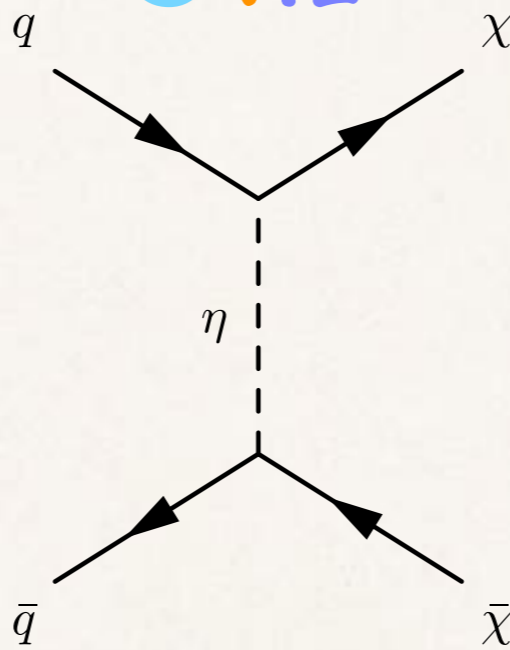
The usual suspects

$O_{S^{\frac{1}{2}}}$



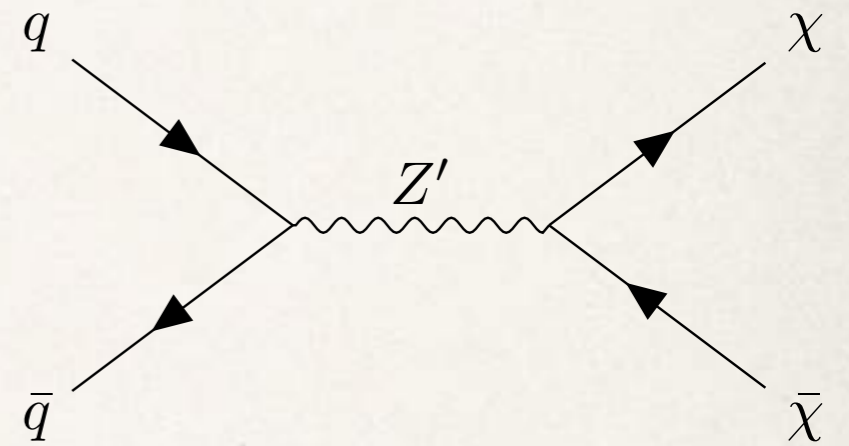
“Higgs portal”

$O_{t^{\frac{1}{2}}}$



“Squark-like”

$I_{S^{\frac{1}{2}}}$



“Z-prime”

- Each is associated with a particular UV-completion

Simplicity

- Even then there are choices to make - for example, for $1s^{1/2}$, there is a choice of vector or axial-vector couplings

$$\begin{aligned}\mathcal{L} \supset & g_\chi Z'_\mu (c_V^\chi \bar{\chi} \gamma^\mu \chi + c_A^\chi \bar{\chi} \gamma^\mu \gamma^5 \chi) \\ & + \sum_q g_q Z'_\mu (c_V^q \bar{q} \gamma^\mu q + c_A^q \bar{q} \gamma^\mu \gamma^5 q) \\ & + \sum_l g_l Z'_\mu (\underbrace{c_V^l \bar{l} \gamma^\mu l}_{\text{Vector}} + \underbrace{c_A^l \bar{l} \gamma^\mu \gamma^5 l}_{\text{Axial-vector}})\end{aligned}$$

- Including couplings to both quarks and leptons, up to 28 free parameters, even in such a simple model!
- Necessary to make simplifying assumptions to keep the number of parameters small

Simplicity

For $1s^{1/2}$ (Z'):

I. Direct detection constraints: $c^q_V = c^{\chi}_V = 0$

II. Dilepton constraints: $g_1 = 0$

III. Minimal Flavor Violation:

g_q equal for each quark

$$\begin{aligned} \mathcal{L} \supset & g_\chi Z'_\mu (\cancel{c^{\chi}_V \bar{\chi} \gamma^\mu \chi} + c^{\chi}_A \bar{\chi} \gamma^\mu \gamma^5 \chi) \\ & + \sum_q g_q Z'_\mu (\cancel{c^q_V \bar{q} \gamma^\mu q} + c^q_A \bar{q} \gamma^\mu \gamma^5 q) \\ & + \sum_l g_l Z'_\mu (\cancel{c^l_V \bar{l} \gamma^\mu l} + c^l_A \bar{l} \gamma^\mu \gamma^5 l) \end{aligned}$$

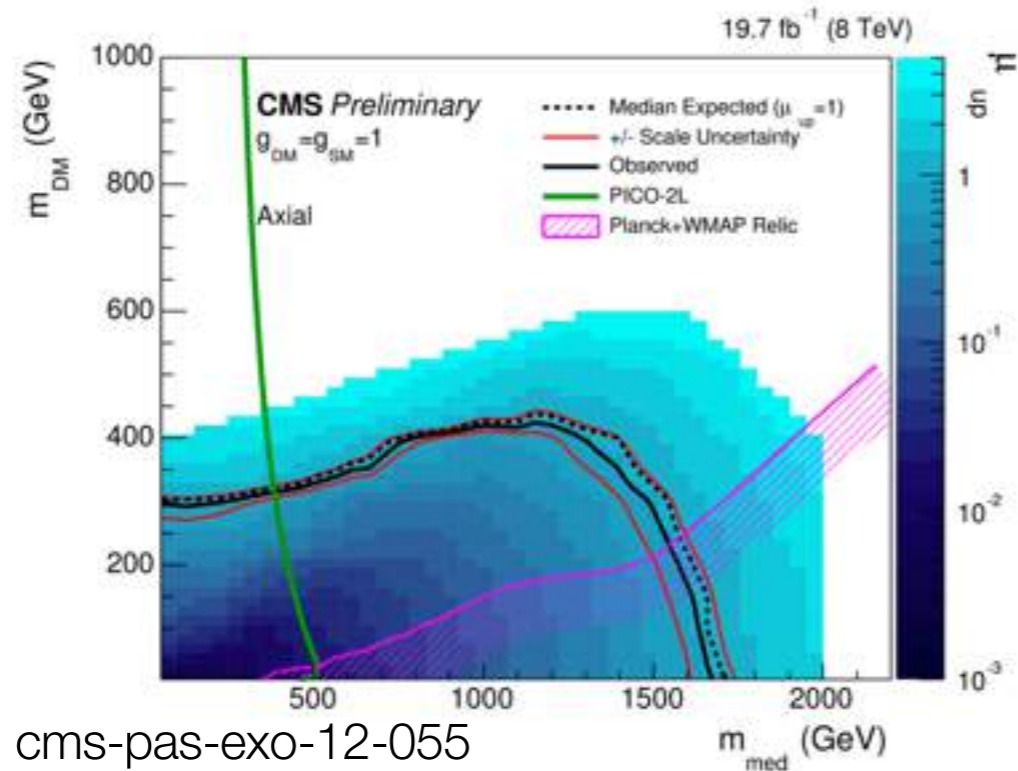
Vector Axial-vector

$$\left\{ m_{\text{DM}}, M_{\text{med}}, g_{\text{DM}}, g_{\text{SM}} \right\} \rightarrow \left\{ m_{\text{DM}}, M_{\text{med}}, g_{\text{DM}} \cdot g_{\text{SM}}, g_{\text{DM}} / g_{\text{SM}} \right\}$$

Even with these simplifying assumptions, a full scan over the 4D parameter space can be computationally prohibitive

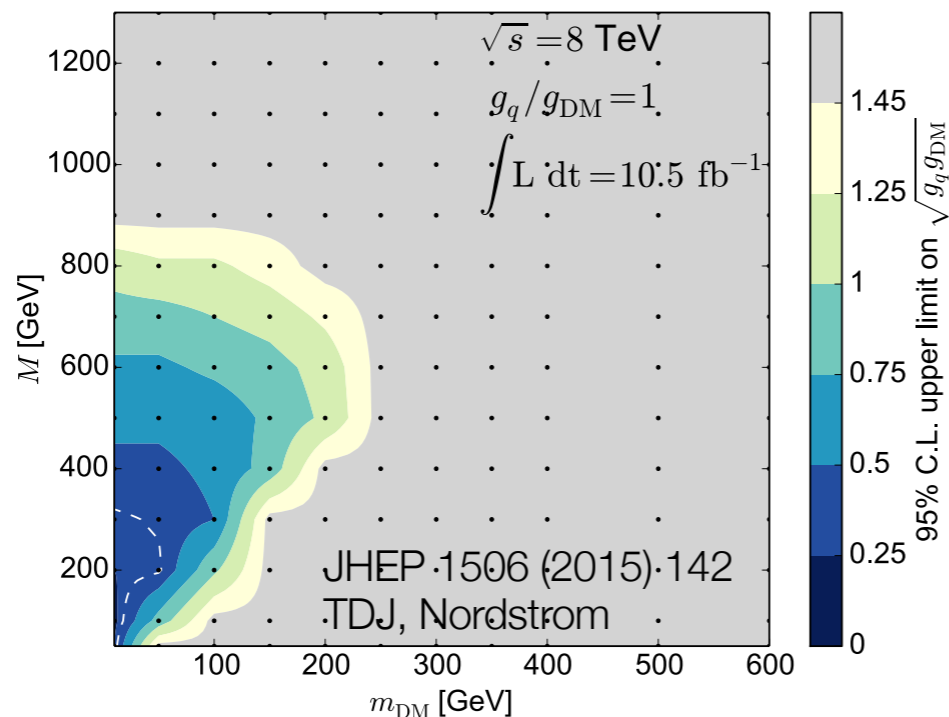
Parameter space

Benchmark
coupling



- ✓ Only 2 parameters to scan
- ✓ Easier comparison between experiments
- ✗ Semi-arbitrary choice of coupling
- ✗ Less comprehensive: Difficult to translate to other couplings

3-D scan



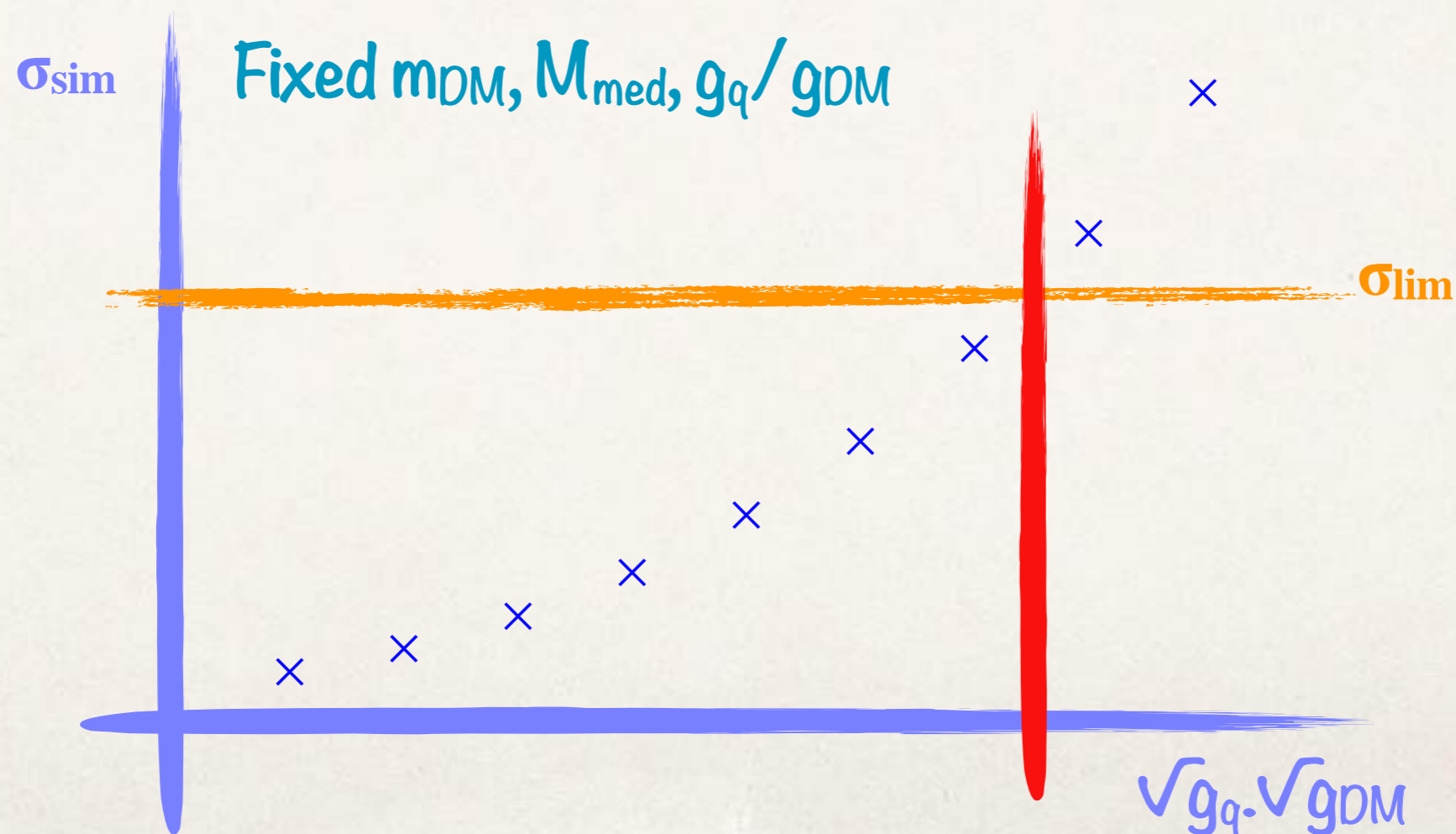
- ✓ Easy to interpret
- ✓ More comprehensive
- ✗ Approximations become necessary - important to avoid regions where these break down
- ✗ Difficult to compare results

Rescaling relations

$$\left\{ m_{\text{DM}}, M_{\text{med}}, g_{\text{DM}}, g_{\text{SM}} \right\} \rightarrow \left\{ m_{\text{DM}}, M_{\text{med}}, g_{\text{DM}} \cdot g_{\text{SM}}, g_{\text{DM}} / g_{\text{SM}} \right\}$$

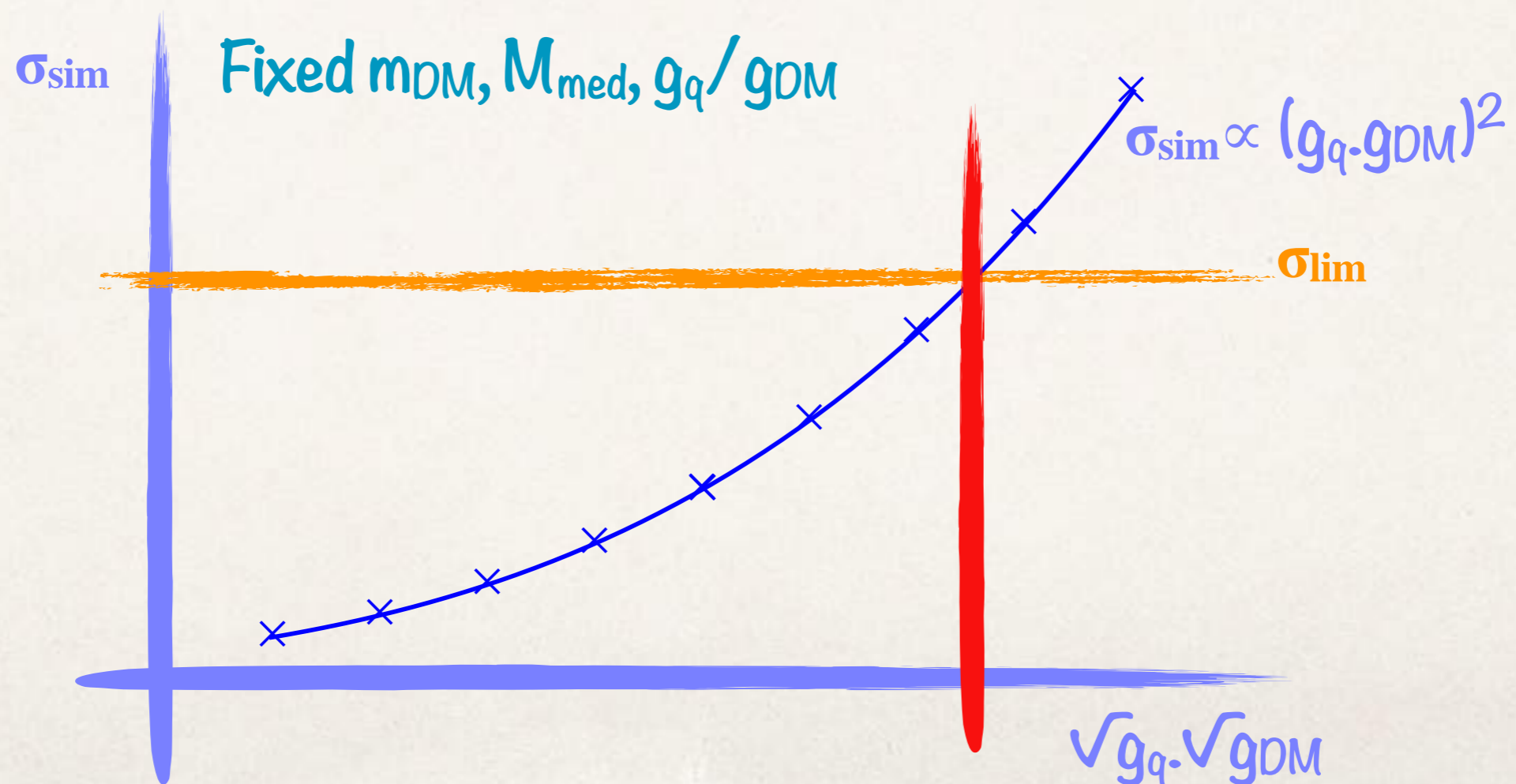
For each $\{m_{\text{DM}}, M_{\text{med}}, g_{\text{q}}/g_{\text{DM}}\}$, simulate signal cross section σ_{sim} for a range of $g_{\text{q}} \cdot g_{\text{DM}}$, compare with the experimental limit σ_{lim} .

Value of $g_{\text{q}} \cdot g_{\text{DM}}$ where $\sigma_{\text{sim}} = \sigma_{\text{lim}}$ defines the constraint on $g_{\text{q}} \cdot g_{\text{DM}}$.



Rescaling relations

If we know how σ_{sim} varies with $g_q \cdot g_{\text{DM}}$, we can simulate for one value of $g_q \cdot g_{\text{DM}}$, avoiding the full scan



Rescaling relations

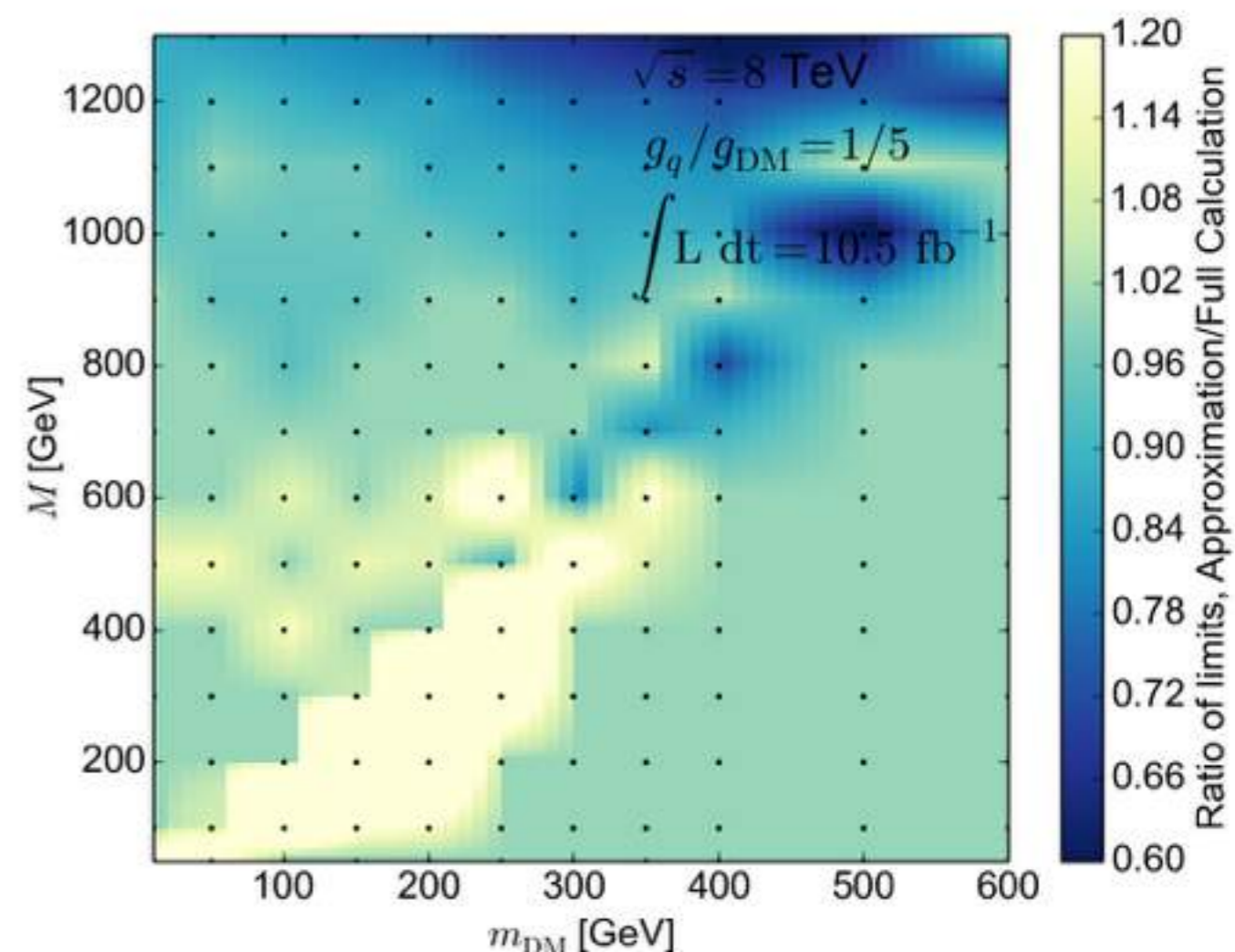
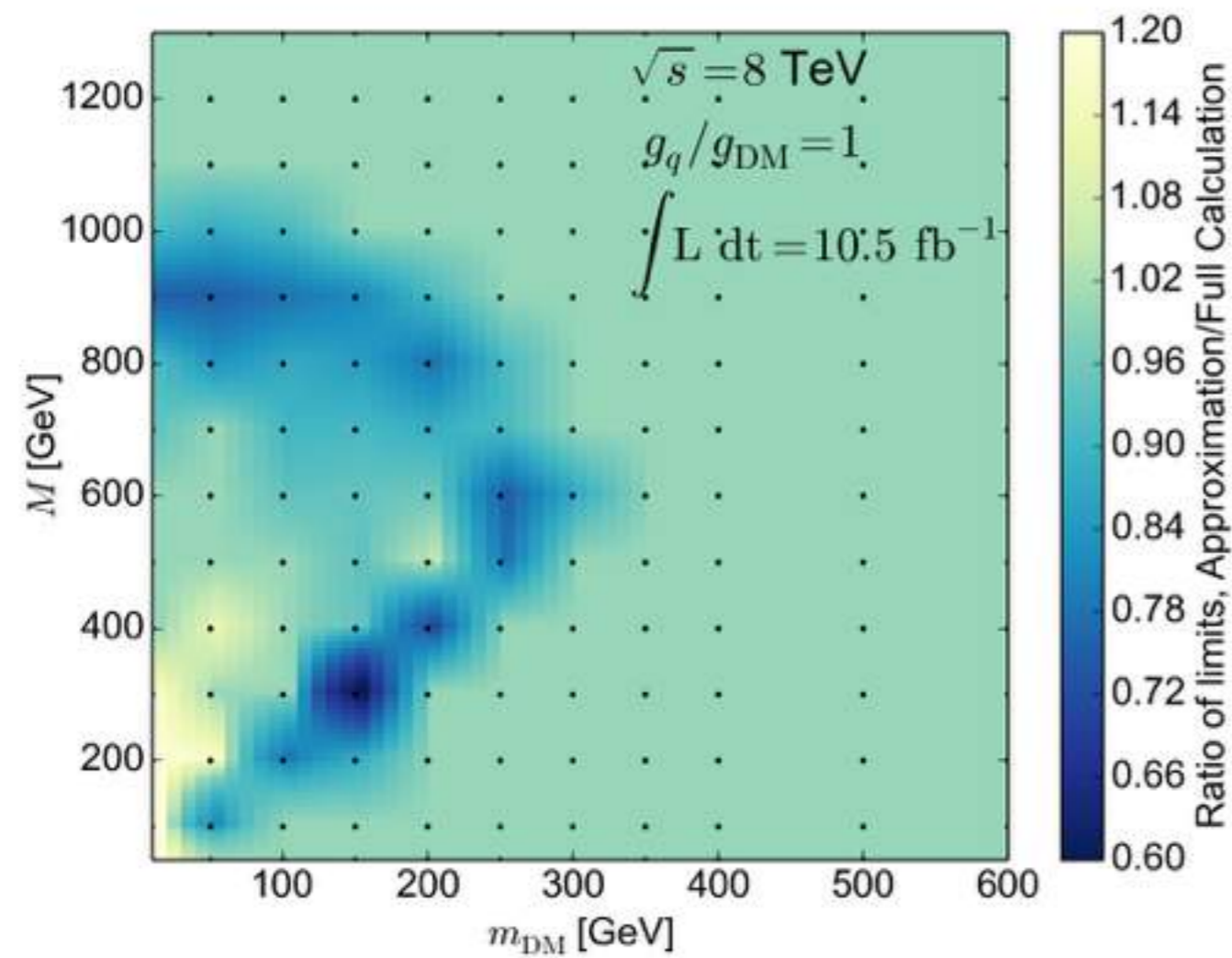
$$\sigma \propto \begin{cases} g_q^2 g_{\text{DM}}^2 / \Gamma_{\text{OS}} & \text{if } M > 2m_{\text{DM}} \\ g_q^2 g_{\text{DM}}^2 & \text{if } M < 2m_{\text{DM}} \end{cases}$$

How well does this approximation hold?

1s^{1/2}

JHEP 1506 (2015) 142

TDJ, Nordstrom

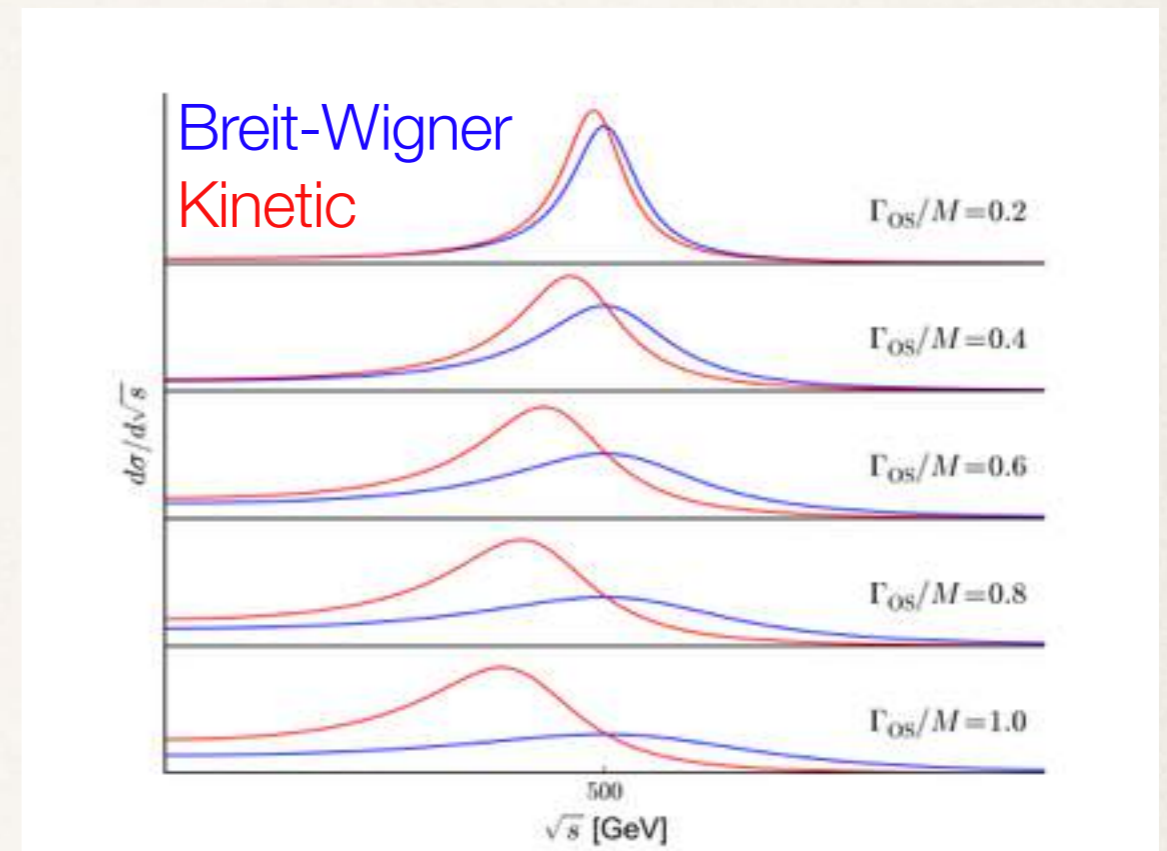


Problems with the width

- The standard Breit-Wigner propagator with on-shell width,

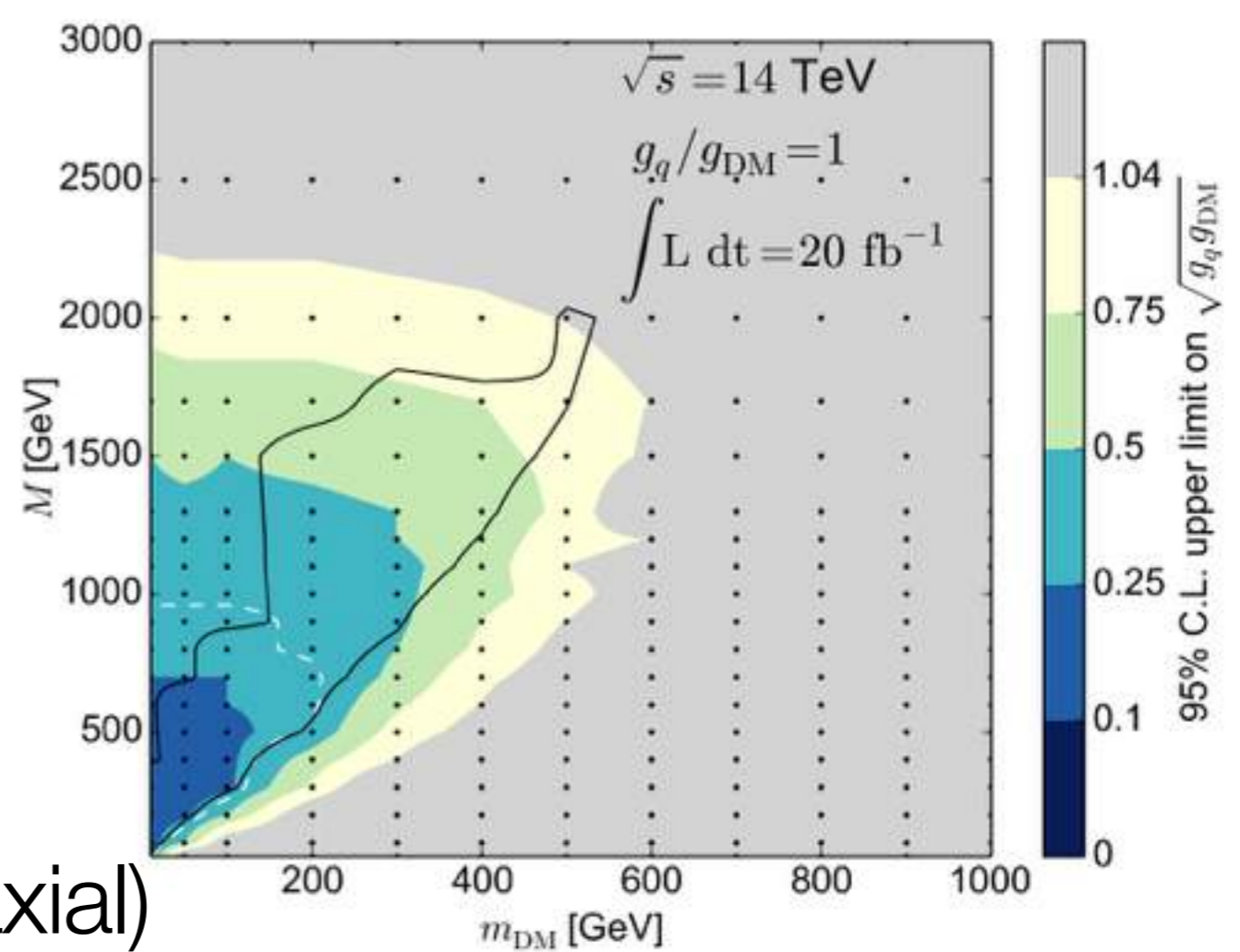
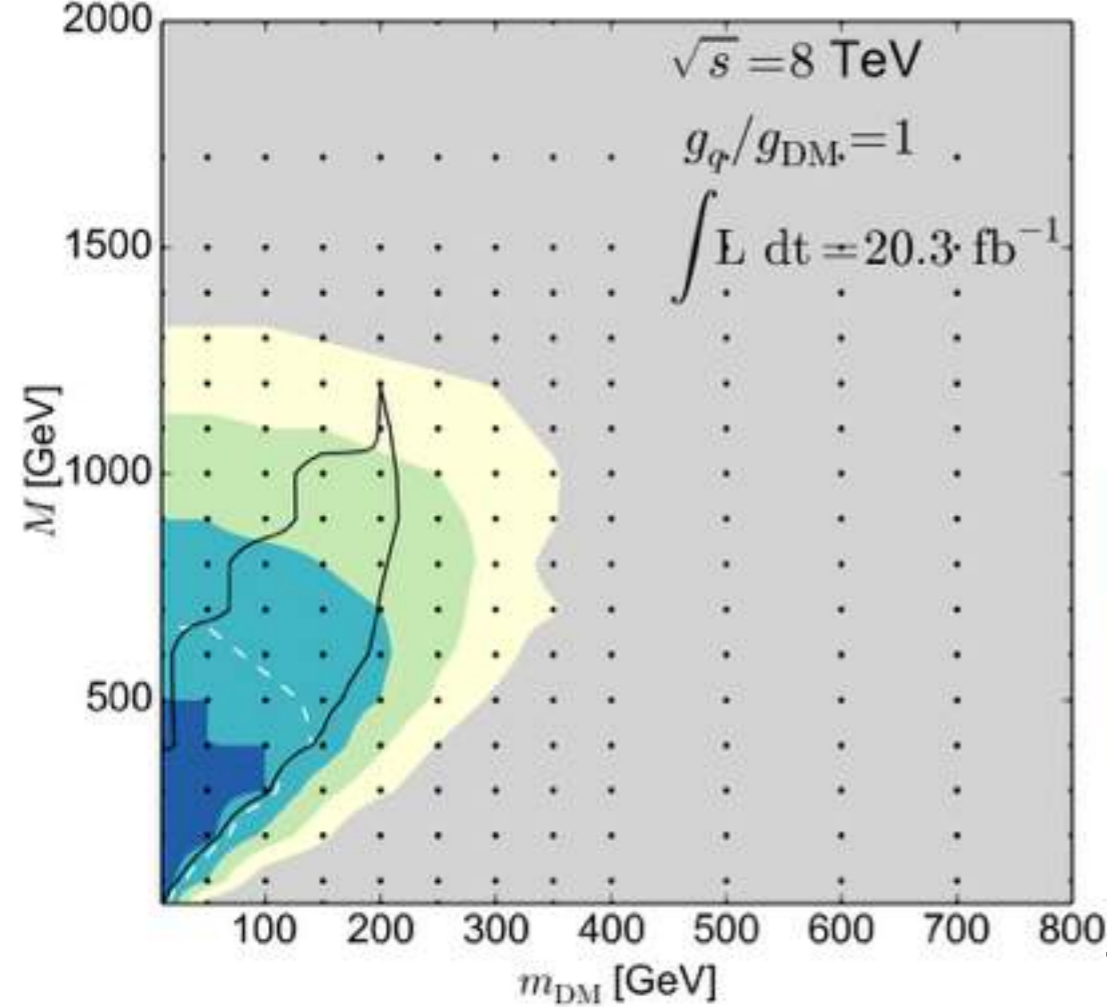
$$\Delta_{BW} = \frac{1}{s - M^2 + iM\Gamma_{OS}}$$

as used by generators, only valid for $\Gamma \ll M$.

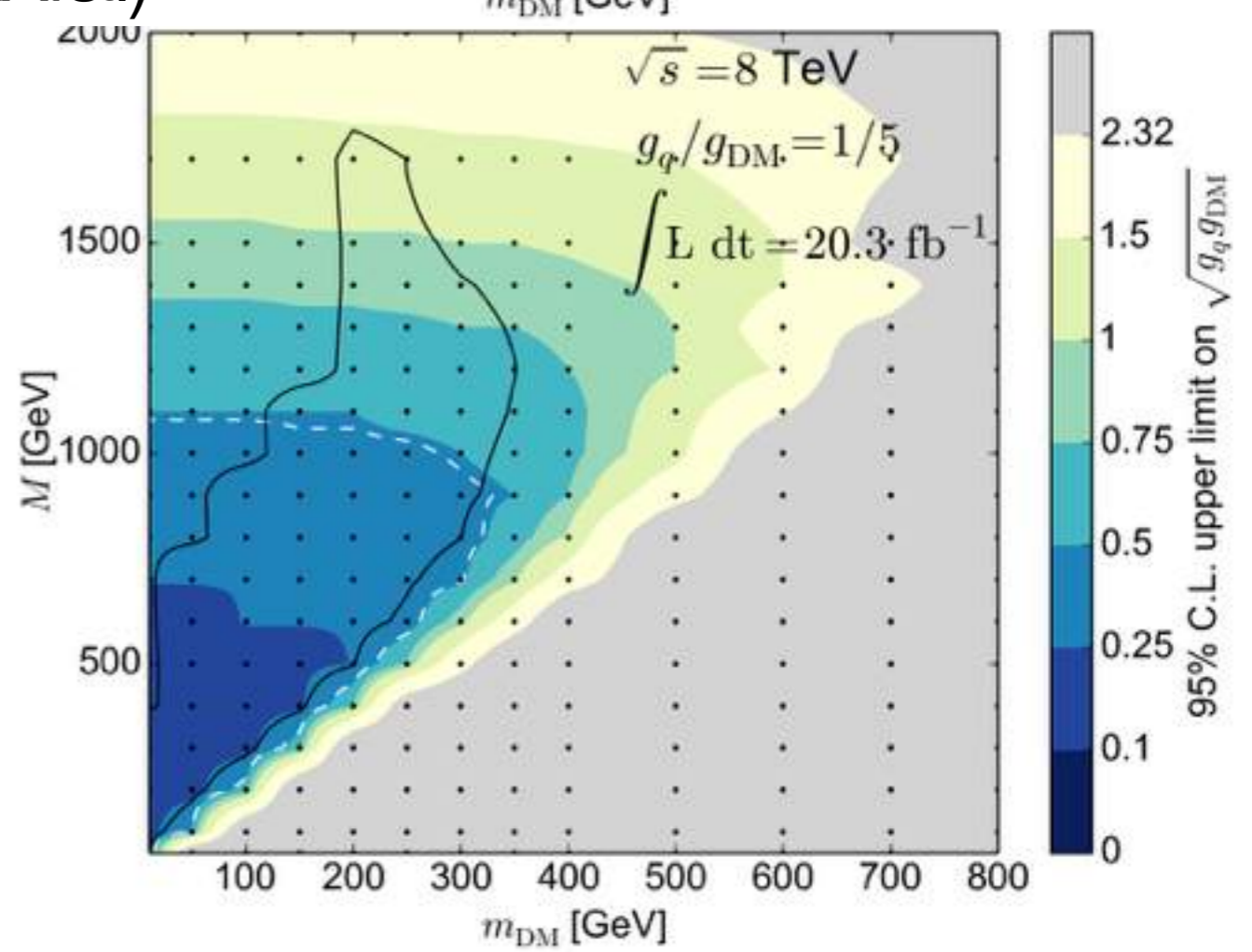
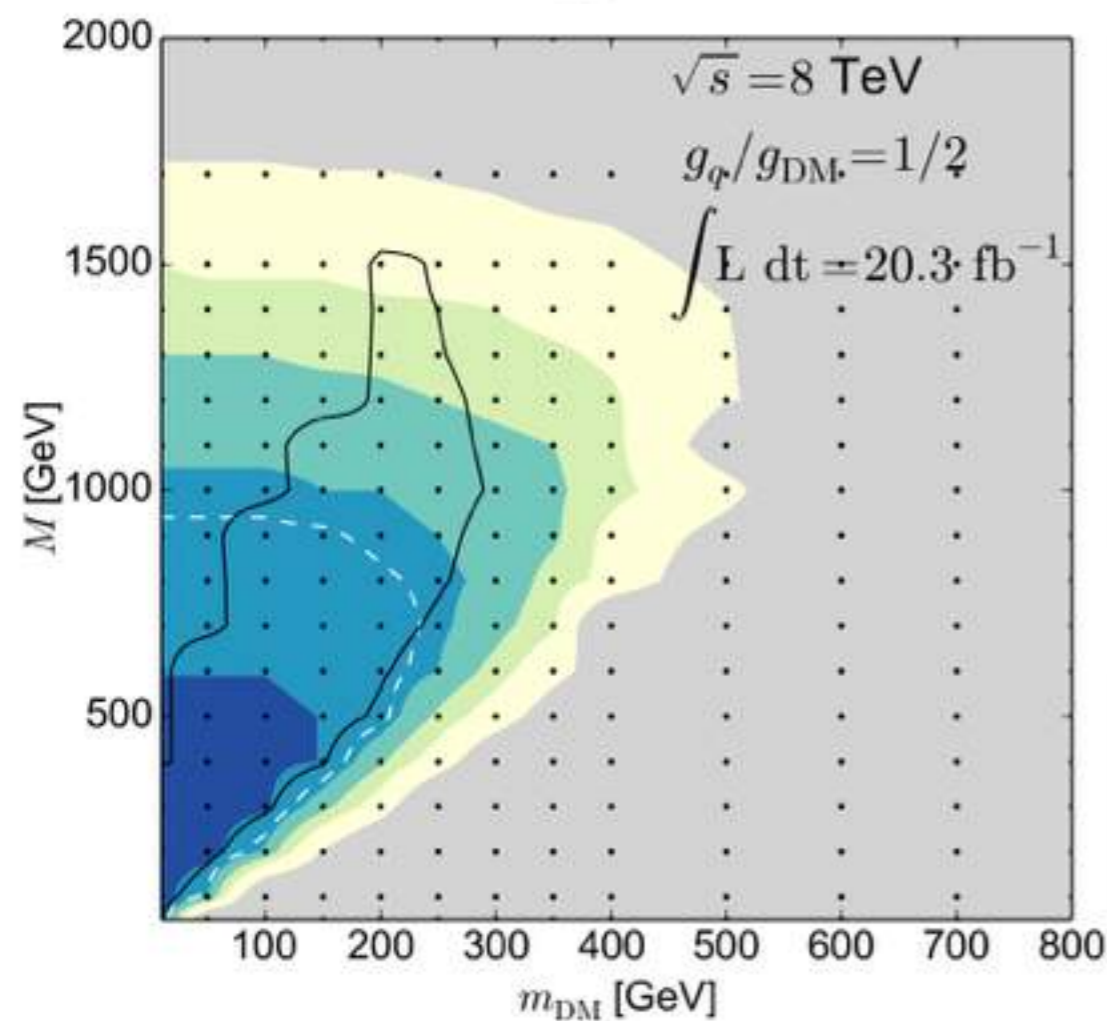


- Restrict parameter space to regions where $\Gamma < M$.
Current strength of constraints give $\Gamma/M \sim 0.5$;
In the transition region, rescale by the ratio of the BW and kinetic propagators after convolution with the PDF

$$\frac{\int_{x_1, x_2} \text{PDF} \times \Delta_{\text{Kinetic}}}{\int_{x_1, x_2} \text{PDF} \times \Delta_{BW}}$$

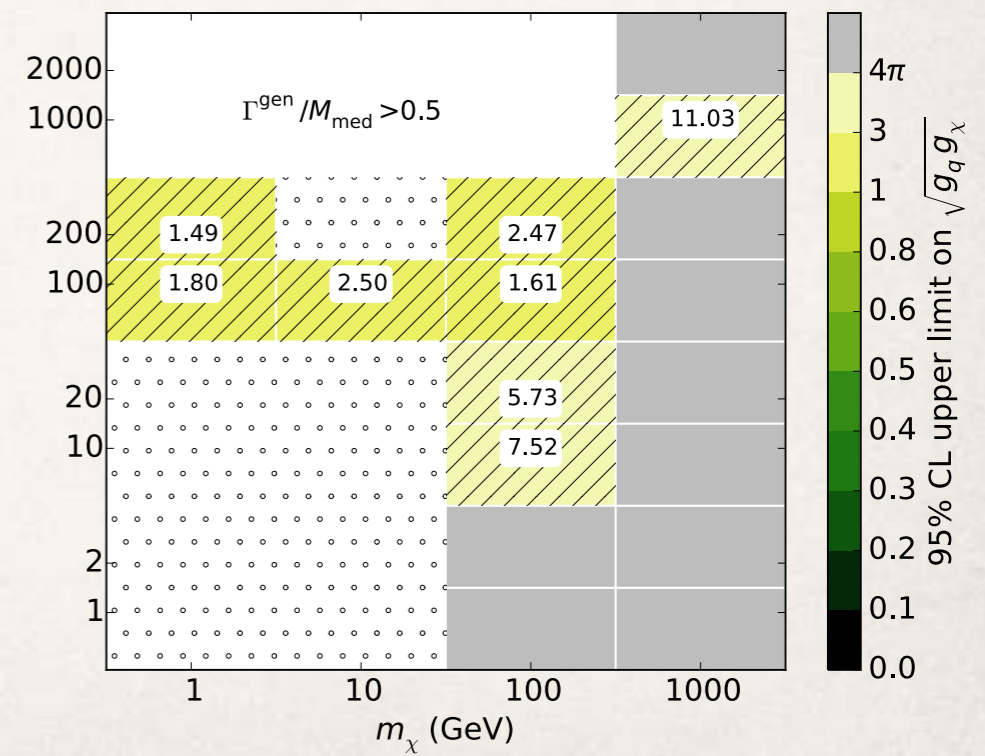
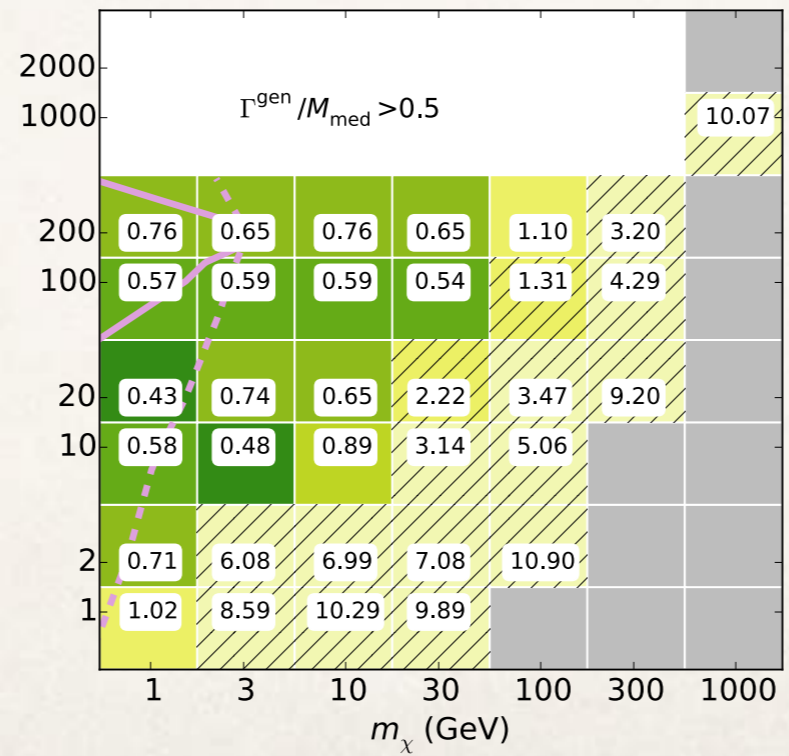
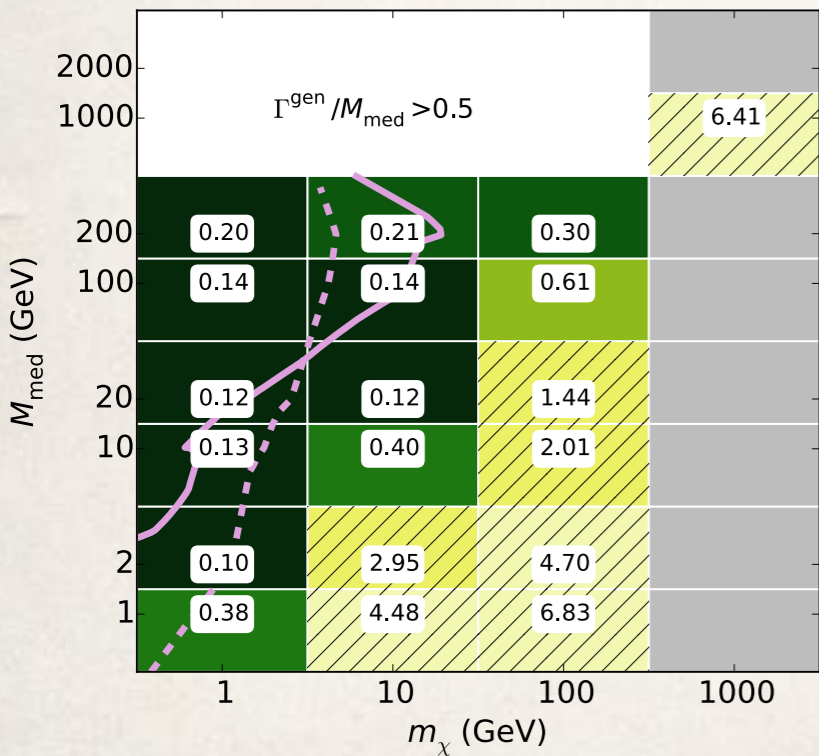
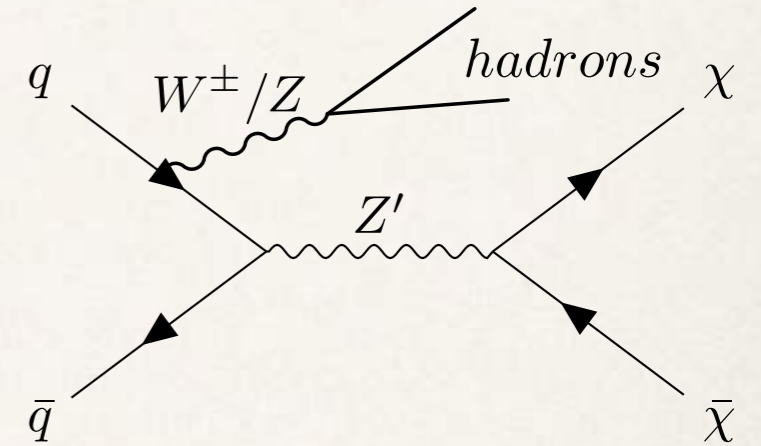
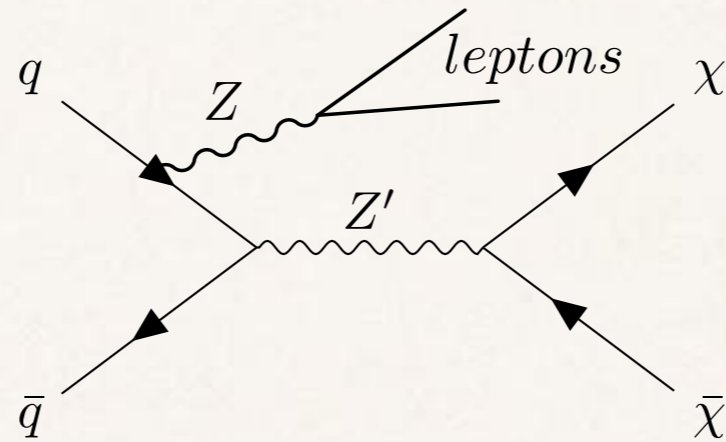
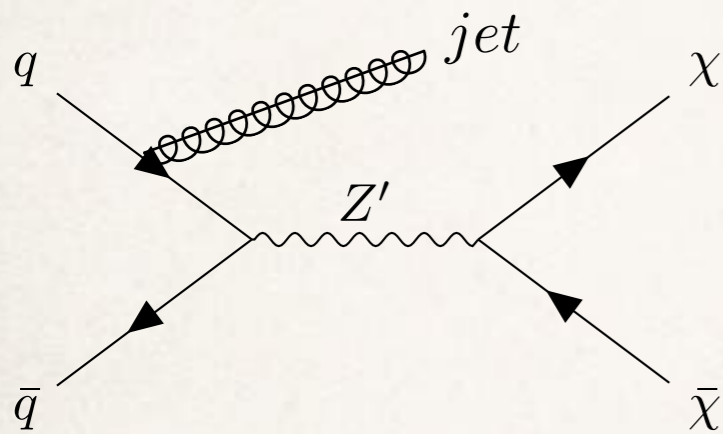


1 s^{1/2} (axial)



Search channels

- To be comprehensive, study other search channels



1s^{1/2} (axial) - Similar results for 1s^{1/2} (vector)

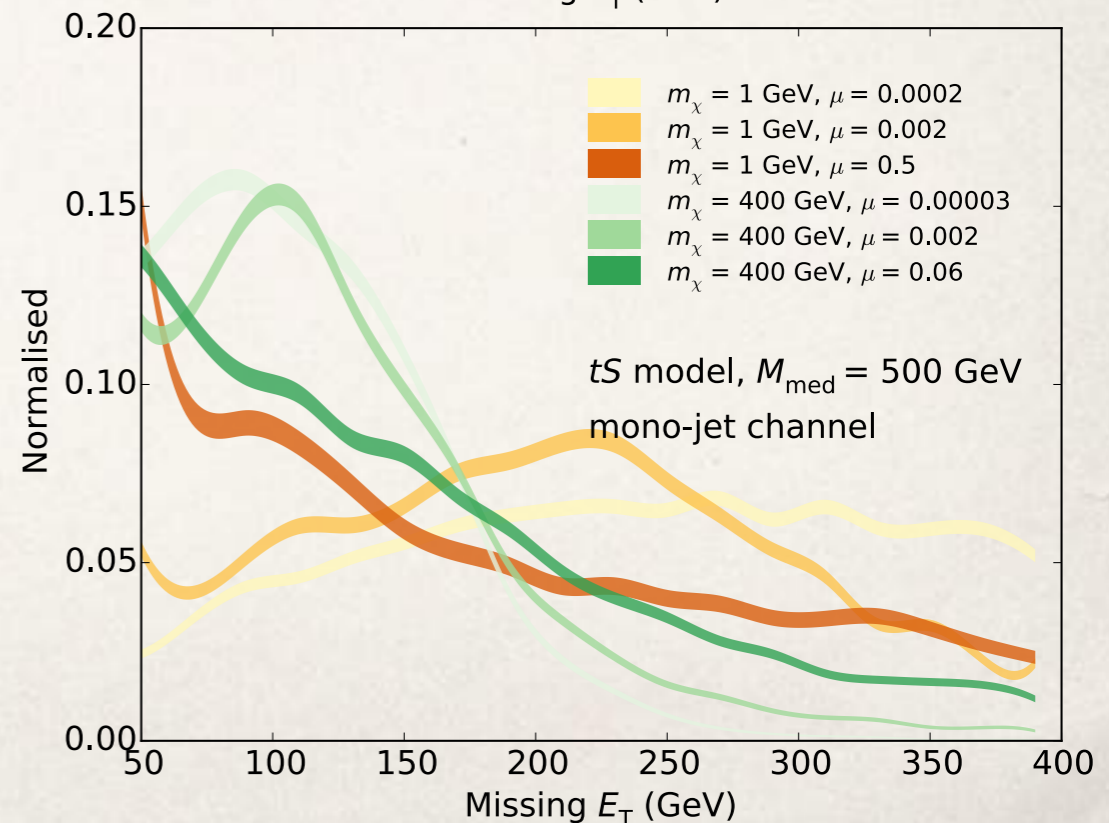
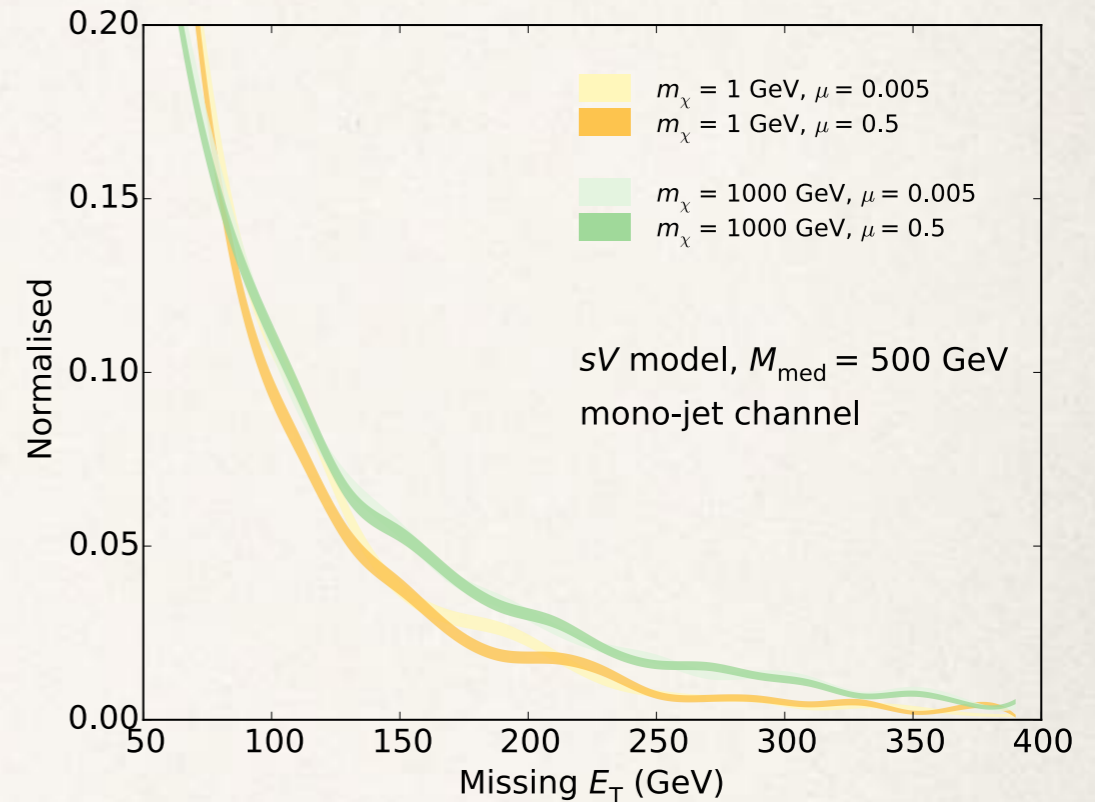
Testing the approximation

- Does the rescaling relation still hold?

$$\sigma \propto \begin{cases} g_q^2 g_{\text{DM}}^2 / \Gamma_{\text{OS}} & \text{if } M > 2m_{\text{DM}} \\ g_q^2 g_{\text{DM}}^2 & \text{if } M < 2m_{\text{DM}} \end{cases}$$

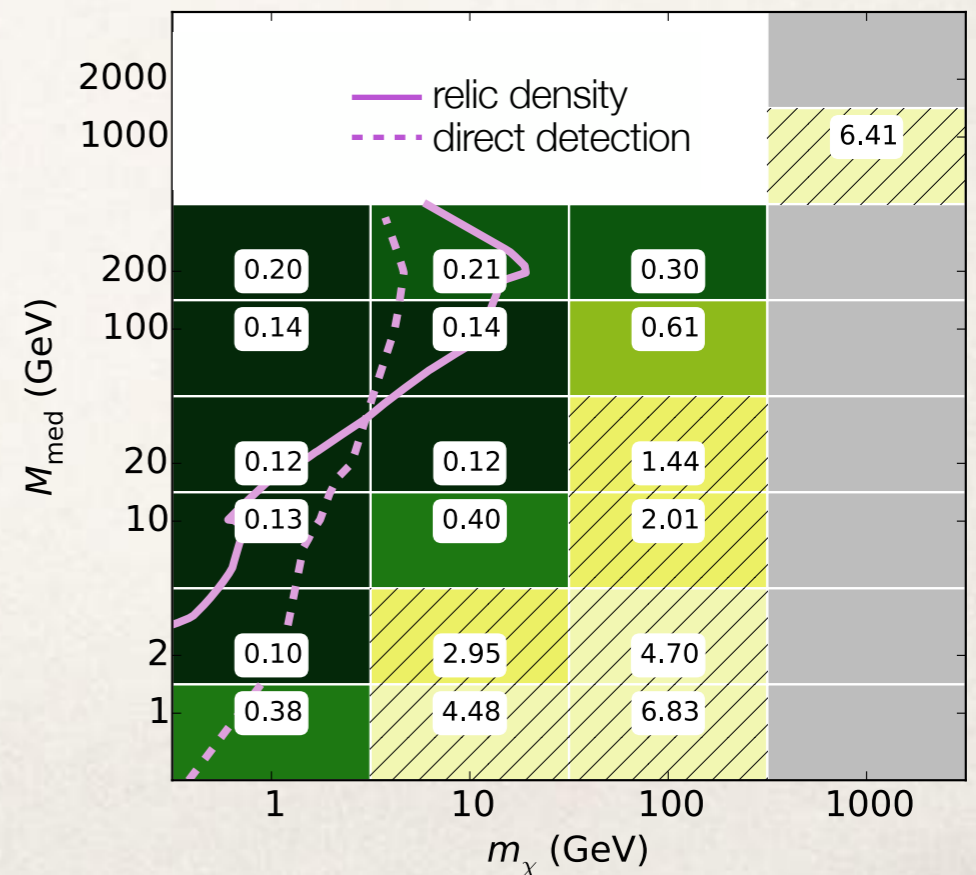
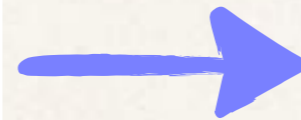
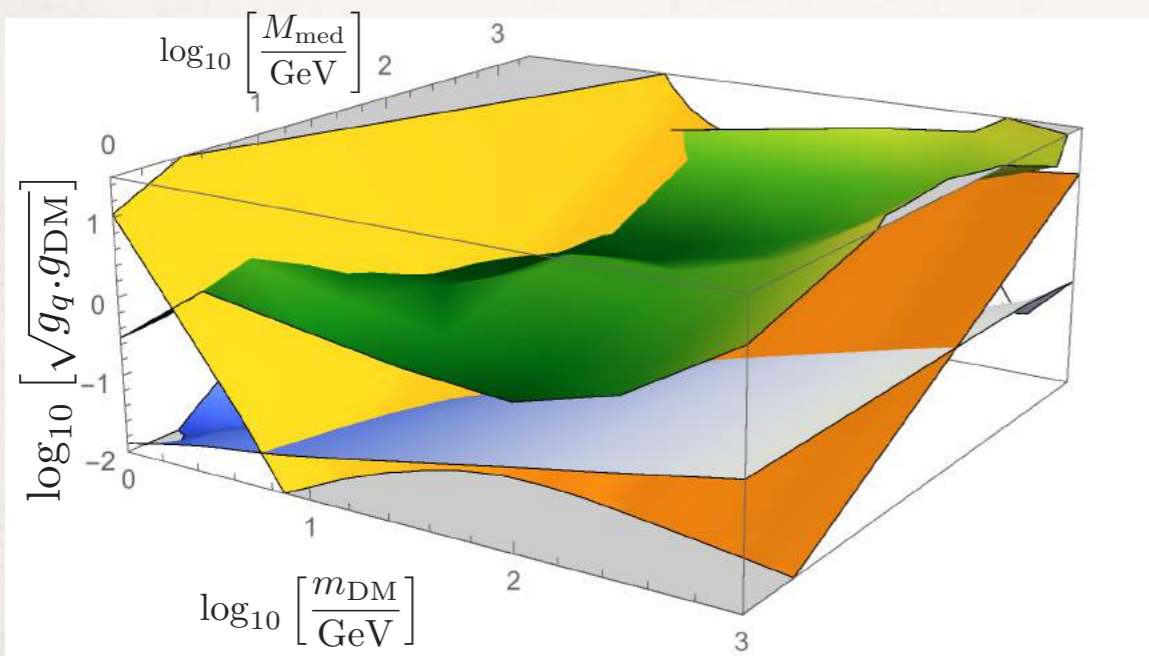
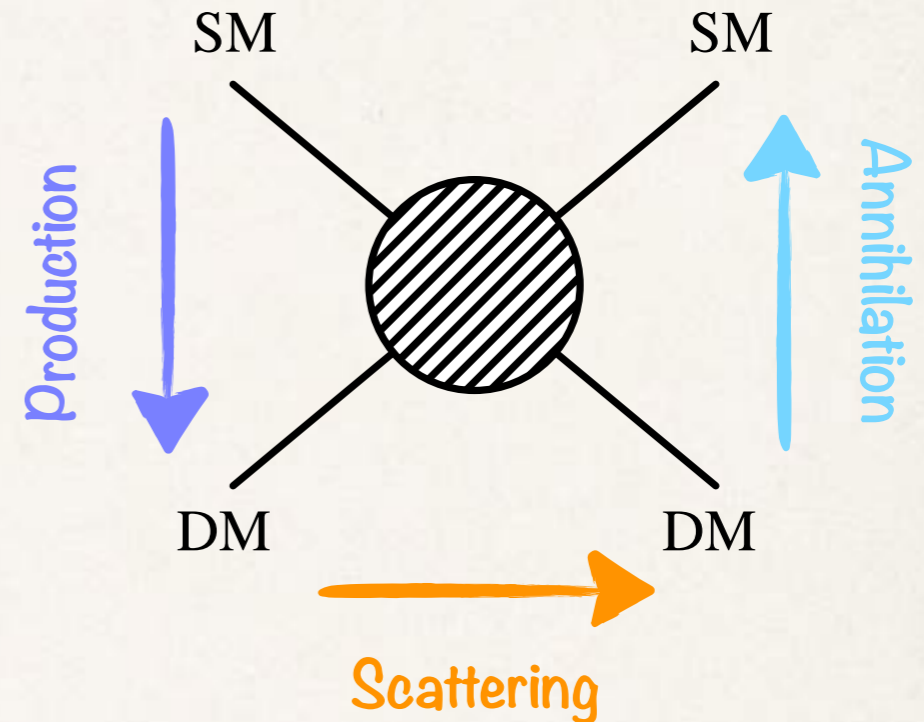
- Only if the kinematic distribution of missing energy is independent of the width

$$\sigma \propto \frac{g_{\text{DM}}^2 g_q^2}{(s - M^2)^2 + M^2 \Gamma^2},$$



Comparing to other constraints

- Difficult to compare multiple constraints in 3D parameter space!
- Intercept shows the boundary where one constraint becomes stronger than another, indicating the region where each class of constraints performs best



Comparing to other constraints

- Direct detection assumes a local density and velocity distribution as input

$$\frac{dR}{dE_R} = \frac{\rho_\chi}{m_{\text{DM}} m_N} \int_{|\vec{v}| > v_{\text{min}}} d^3\vec{v} |\vec{v}| f(\vec{v}) \frac{d\sigma_{\chi N}}{dE_R}$$

- Relic density constraints assume DM is a thermal relic sensitive to number of annihilation channels and relative contribution to total relic density

$$\langle \sigma v \rangle_{\text{total}} \simeq \frac{4.8 \times 10^{-10} \text{ GeV}^{-2}}{\Omega_{\text{DM}} h^2}.$$

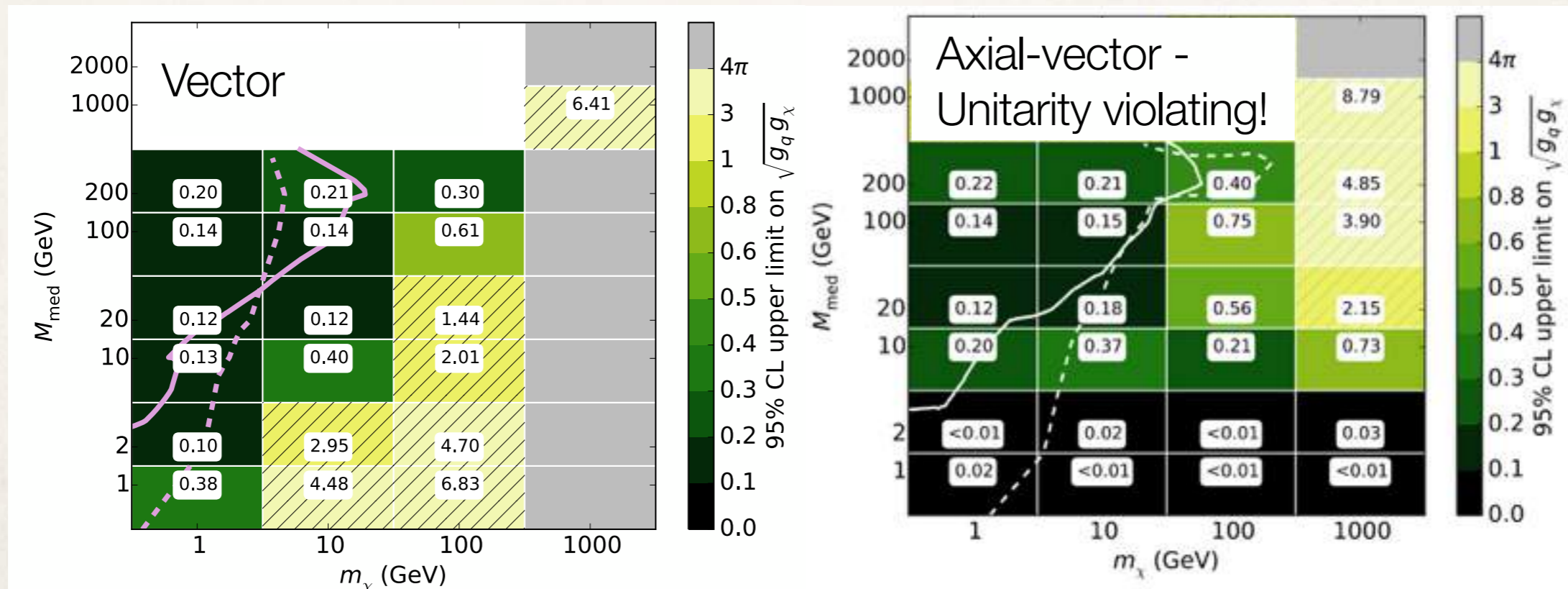
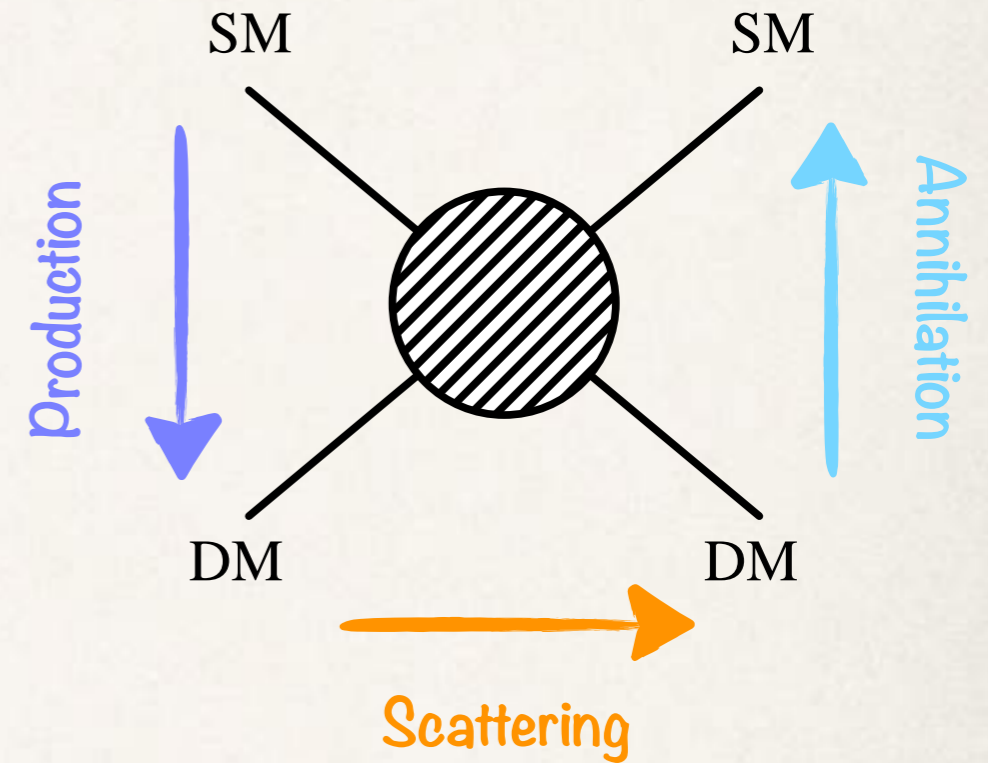
- Each constraint has strengths and weaknesses, so together are complementary, but compare with caution

Consistency

- The simplified models we've been using are not designed to be UV-complete
- Does it matter if the simplified models we're using are physical?
 - Signals and constraints can be *overestimated* if we get this wrong;
 - Some models are not just be *incomplete*, but *wrong*

Consistency

- We focus on axial-vector $1s_{1/2}$ (Z'), because it 'hides' from direct detection
 - Violates unitarity when $m_{\text{DM}} \gg M_{\text{med}}$, greatly enhancing the cross section
 - Suffers anomalies!



Building a natural, consistent axial $1s^{1/2}$ (Z')

- $\cos\theta U(1)_{B-L} + \sin\theta U(1)_Y$ is guaranteed anomaly-free, so use this as our $U(1)'$
- This fixes the charge of the left- and right-handed SM fermions under $U(1)'$

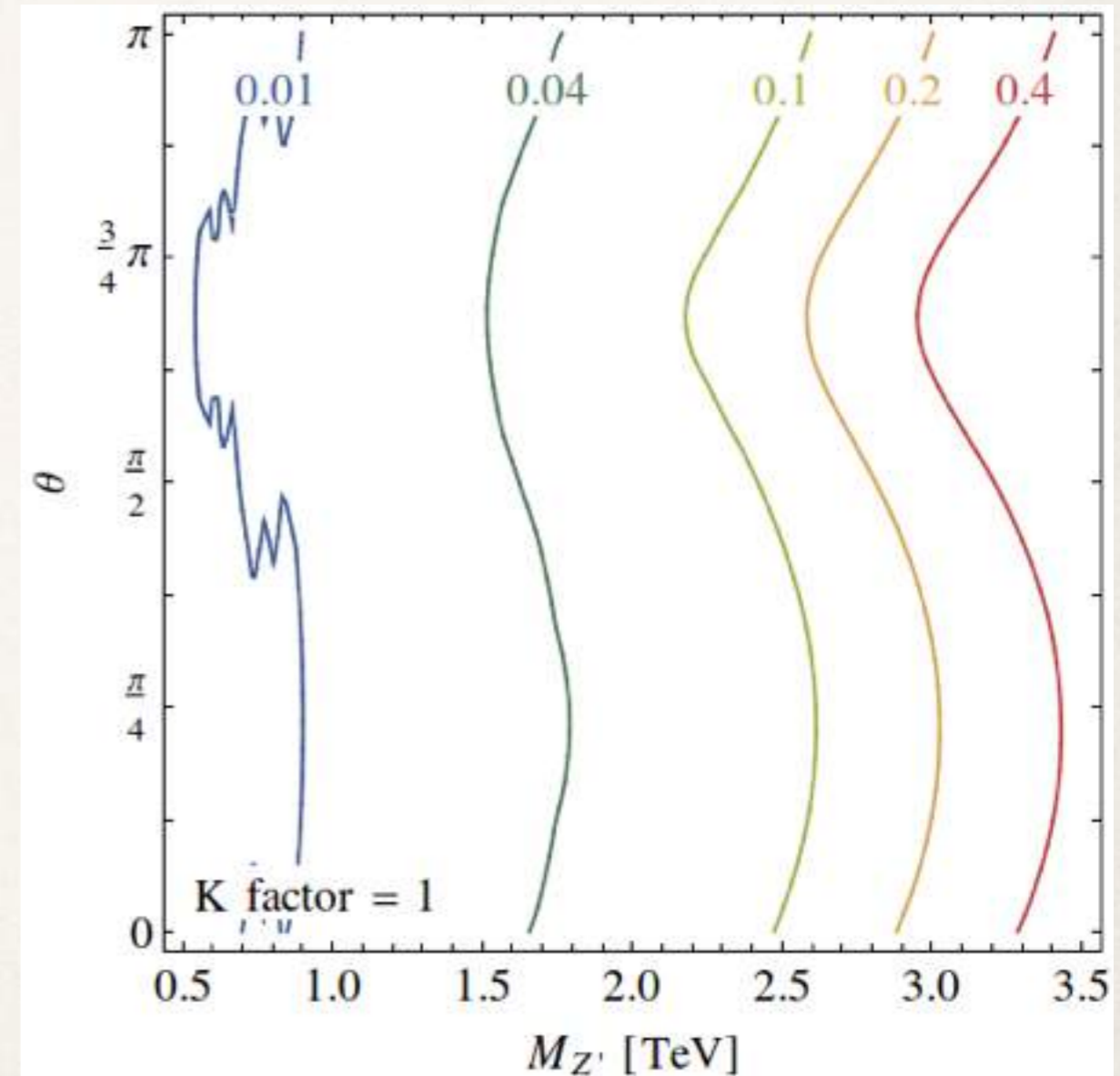
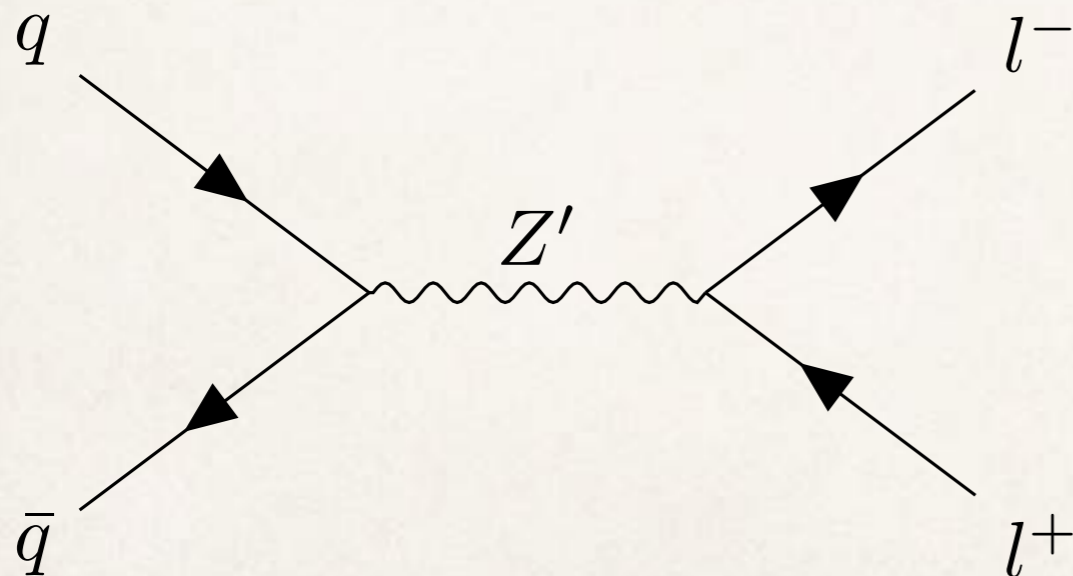
| | $SU(3)$ | $SU(2)$ | $U(1)_Y$ | $U(1)_{B-L}$ | $U(1)'$ |
|---|--------------------|----------|----------------|----------------|--|
| $\begin{pmatrix} \nu_L^i \\ \ell_L^i \end{pmatrix}$ | 1 | 2 | $-\frac{1}{2}$ | -1 | $-\frac{1}{2} \cos \theta - \sin \theta$ |
| $(\ell_R^i)^C$ | 1 | 1 | 1 | $+1$ | $\cos \theta + \sin \theta$ |
| $\begin{pmatrix} u_L^i \\ d_L^i \end{pmatrix}$ | 3 | 2 | $\frac{1}{6}$ | $+\frac{1}{3}$ | $\frac{1}{6} \cos \theta + \frac{1}{3} \sin \theta$ |
| $(u_R^i)^C$ | $\bar{\mathbf{3}}$ | 1 | $-\frac{2}{3}$ | $-\frac{1}{3}$ | $-\frac{2}{3} \cos \theta - \frac{1}{3} \sin \theta$ |
| $(d_R^i)^C$ | $\bar{\mathbf{3}}$ | 1 | $\frac{1}{3}$ | $-\frac{1}{3}$ | $\frac{1}{3} \cos \theta - \frac{1}{3} \sin \theta$ |

- If L and R fermions have different charge,
Higgs must be charged to maintain gauge invariance $y_\ell \bar{L}_L \Phi \ell_R$

| | | | | | |
|---|----------|----------|---------------|-----|---------------------------|
| $\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$ | 1 | 2 | $\frac{1}{2}$ | 0 | $\frac{1}{2} \cos \theta$ |
|---|----------|----------|---------------|-----|---------------------------|

Dilepton constraints

- Induced lepton coupling subjects this model to stringent constraints from Z' decay to dileptons



Building a natural consistent axial Z'

- Mixing results in a mix of terms - no pure axial-vector term!

| SM fermion f | coeff. of $g_{Z'} \bar{f} Z' f$ | coeff. of $g_{Z'} \bar{f} Z' \gamma_5 f$ |
|----------------|---|---|
| leptons | $-\frac{3}{4} \cos \theta - \sin \theta$ | $-\frac{1}{4} \cos \theta$ |
| neutrinos | $-\frac{1}{4} \cos \theta - \frac{1}{2} \sin \theta$ | $\frac{1}{4} \cos \theta + \frac{1}{2} \sin \theta$ |
| up quarks | $\frac{5}{12} \cos \theta + \frac{1}{3} \sin \theta$ | $\frac{1}{4} \cos \theta$ |
| down quarks | $-\frac{1}{12} \cos \theta + \frac{1}{3} \sin \theta$ | $-\frac{1}{4} \cos \theta$ |

$$\mathcal{L} \supset g_\chi Z'_\mu (\cancel{c_V^\chi \bar{\chi} \gamma^\mu \chi} + c_A^\chi \bar{\chi} \gamma^\mu \gamma^5 \chi) + g_q Z'_\mu (\underbrace{c_V^q \bar{q} \gamma^\mu q}_{\text{Vector}} + \underbrace{c_A^q \bar{q} \gamma^\mu \gamma^5 q}_{\text{Axial-vector}})$$

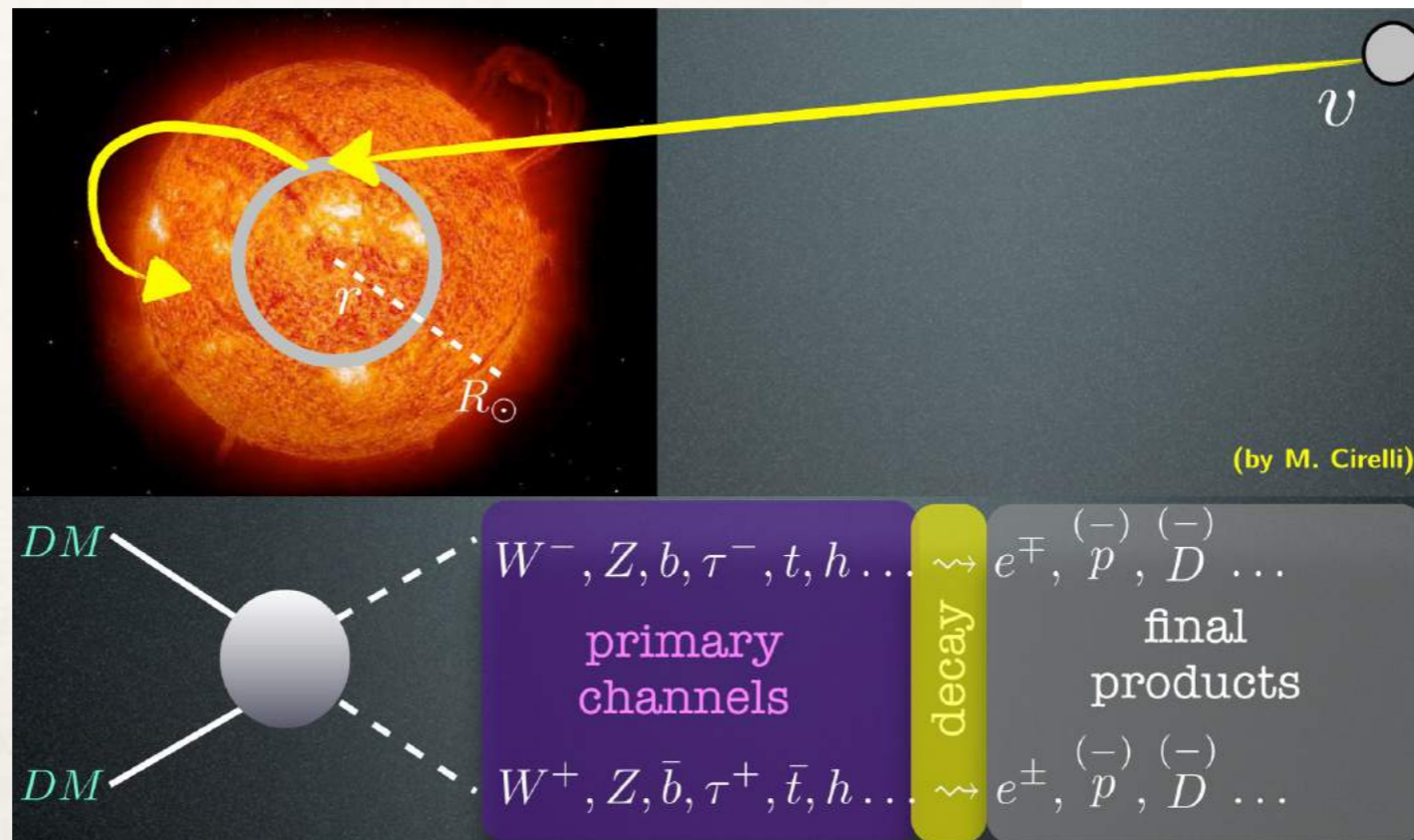
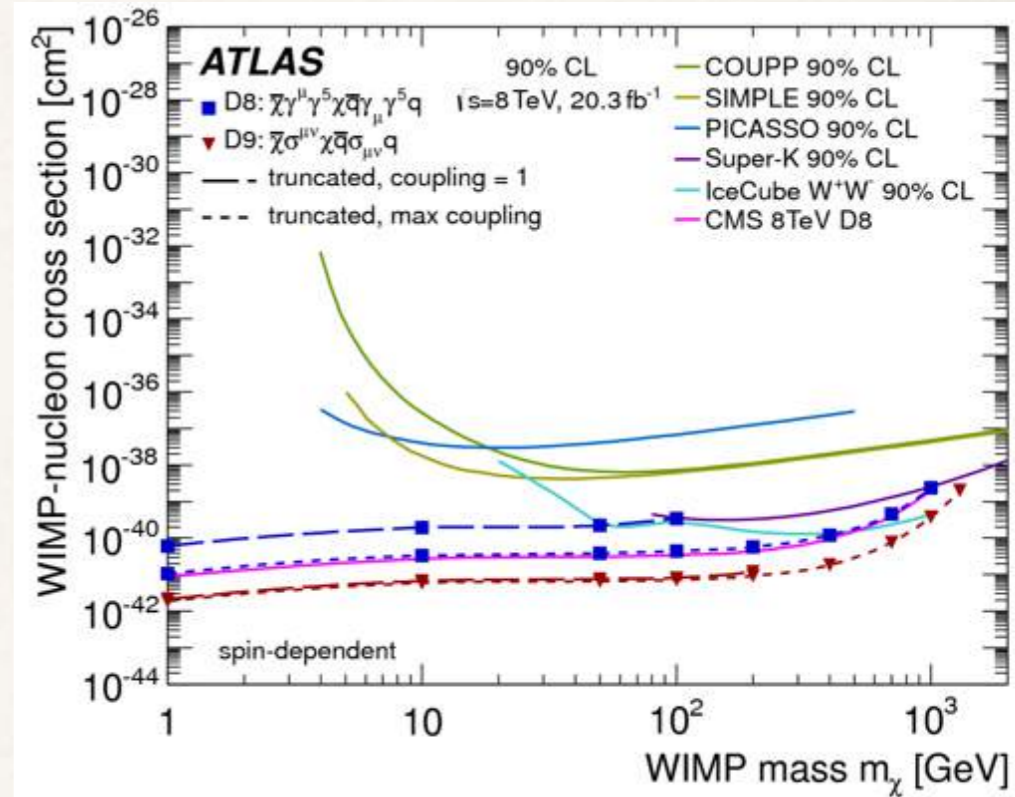
- Induces a range of DM scattering operators, not just the 'usual' σ_{SI} and σ_{SD} .

$$\longrightarrow \underbrace{\vec{s}_\chi \cdot \vec{s}_N}_{\sigma_{SD}}, \quad \underbrace{i \vec{s}_\chi \cdot (\vec{s}_N \times \vec{q})}_{\text{Suppressed, but neither } \sigma_{SI} \text{ nor } \sigma_{SD}}, \quad \vec{s}_\chi \cdot \vec{v}^\perp$$

IceCube: Using annihilation to probe scattering

- It is difficult for DD experiments to compete with LHC constraints on these models
- Solar neutrinos provide a unique window on DM scattering
- DM accumulates in the sun

$$\Gamma_{\text{ann}} \propto \rho^2 \rightarrow \Gamma_{\text{ann}} = \Gamma_{\text{capture}}$$



Conclusion

- Effective operators remain a useful benchmark for DM searches at the LHC if used and interpreted with caution
- Simplified models are the natural next step. The size of the parameter and model space present some challenges which can be overcome with careful application of constraints and approximations
- The consistent use of simplified models is important and presents interesting phenomenology!