

# Gravity at the Horizon: from the cosmic dawn to ultra-large scales

Miguel Zumalacárregui

Nordic Institute for Theoretical Physics

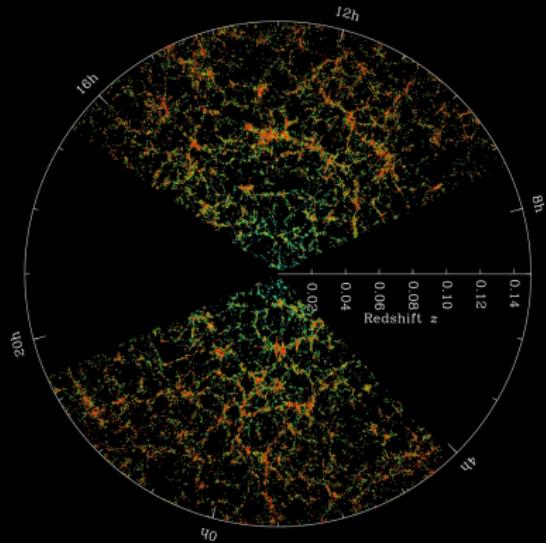
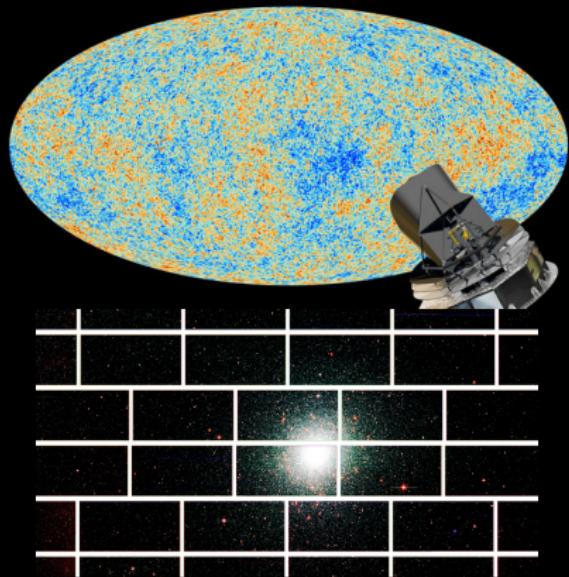


NORDITA

Helsinki - Feb 2016

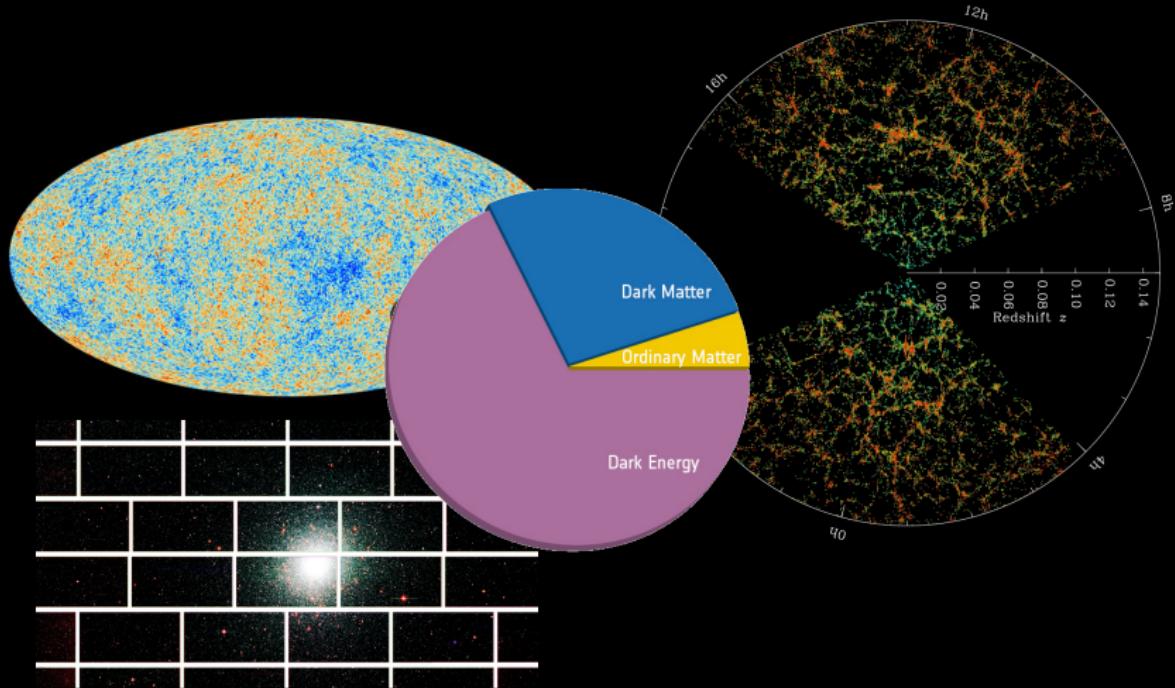
with L. Amendola, E. Bellini, J. Lesgourgues,  
F. Montanari, V. Pettorino, J. Renk

# A Golden Era for Cosmology



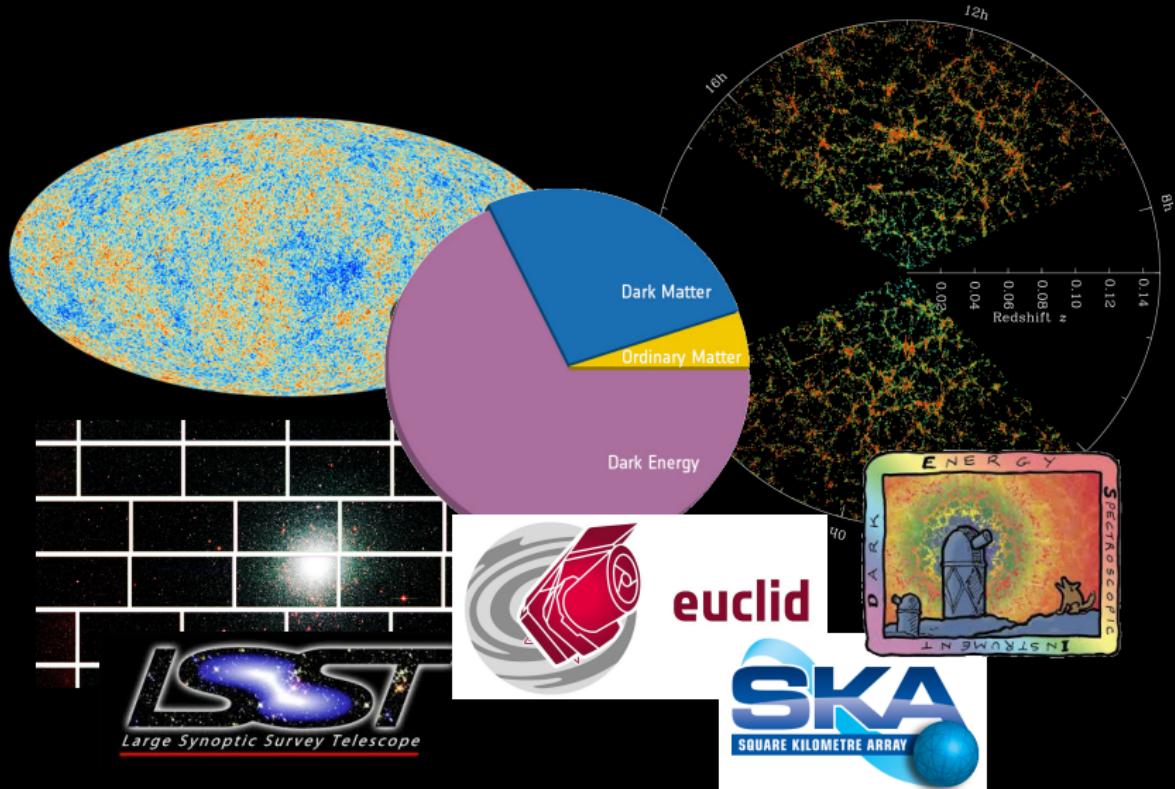
images from Planck , SDSS, Dark Energy Survey

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Gravity at the Horizon:

# Why alternative gravities?

- Alternatives to  $\Lambda$ ?

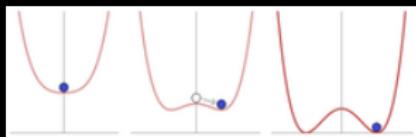
*Inflation again?     $n_s \neq 1$*

- Interesting field-theoretical questions

*proxy for inflation/quantum gravity?*

*viable massive spin-2 particles?*

*cosmological constant problems?*



- Test gravity on cosmological scales

*effects on cosmological scales?*

*model independence of tests?*

# How to modify gravity

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Diet + Exercise → already very hard!

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Lorentz + QM ⇒ restrictions on massless graviton interactions!

(Weinberg '64)

Einstein gravity: only covariant metric theory with 2<sup>nd</sup> order eqs.

(Lovelock '71)

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Need to give up some of the assumptions:

- Add degrees of freedom:
  - Massive gravity: → 5 d.o.f. → very tough!
  - Scalar-tensor: → 2+1 d.o.f.
  - vector-tensor, tensor-vector-scalar (TeVeS), ...
- Lorentz violation, Non-local interactions, ...

# Scalar-Tensor gravity

- ★ Old-School:  $f(\phi)R + K(X, \phi)$   $X \equiv -(\partial\phi)^2/2$
- ▷ quintessence,  $f(R)$ , Brans-Dicke (Jordan '59, Brans & Dicke '61)

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$g_{\mu\nu} + [\phi]$  + Local + 4-D + Lorentz theory with  $2^{nd}$  order Eqs.

$$G_2(X, \phi) - G_3(X, \phi)\square\phi + G_4(\phi, X)R + G_{4,X}\left[(\square\phi)^2 - \phi_{;\mu\nu}\phi^{;\mu\nu}\right] \\ + G_5G_{\mu\nu}\phi^{;\mu\nu} - \frac{G_{5,X}}{6}\left[(\square\phi)^3 - 3(\square\phi)\phi_{;\mu\nu}\phi^{;\mu\nu} + 2\phi_{;\mu}^{;\nu}\phi_{;\nu}^{;\lambda}\phi_{;\lambda}^{;\mu}\right]$$

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## ★ Beyond Horndeski (MZ & Garcia-Bellido '13)

- ▷ General disformal coupling (Bekenstein '92)
- ▷ "Covariantized" galileons (Gleyzes *et al.* '14)

# Cosmology: Horndeski in four words (Bellini & Sawicki JCAP '14)

Background expansion:  $\longrightarrow H(t)$  (or  $\Omega_{\text{de}}$ , or  $w\dots$ )

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- $\alpha_M, \alpha_T \Rightarrow$  Mod. tensor eqs. (Saltas, Sawicki, Amendola, Kunz '14)
- $\alpha_K, \alpha_B \Rightarrow$  Kinetic terms

Theory specific relations:

- Quintessence:  $\alpha_K \propto \Omega_{\text{DE}},$
- JBD:  $\alpha_K, \alpha_B = -\alpha_M,$     Galileon-like:  $\alpha_B + \alpha_M, \alpha_T$

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**BS is no BS**

Horndeski in the Cosmic Linear Anisotropy Solving System

# hi\_class

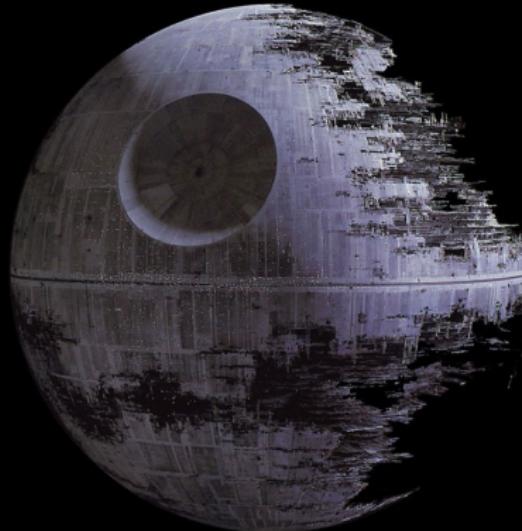
developed with Emilio Bellini, Julien Lesgourgues, Iggy Sawicki

# Horndeski in the Cosmic Linear Anisotropy Solving System

$$\begin{aligned}
 & \bar{R} \sqrt{-g} \mathcal{L}_H \alpha_H \psi \rho p \Phi \Omega \sqrt{-g} \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & G_0 \Phi \alpha_H \psi \rho p \Gamma_{\mu}^{\nu} G_0 \Phi \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & \delta R_H \phi_{\mu\nu} \alpha_H \psi \rho p \Gamma_{\mu}^{\nu} G_0 \Phi \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & H \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & \Phi \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & \Phi \Gamma_{\mu}^{\nu} \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & X \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & \omega \psi^2 X \delta \theta_{\mu\nu} \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & V_0 G_0 \mathbb{D}\phi \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & G_0 \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & \alpha_H \mathbb{D}\phi \theta_{\mu\nu} \psi \rho V_0 G_0 \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & G_0 \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & \delta \psi \alpha_H \psi \rho X \alpha_M \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \\
 & \alpha_B G_0 \psi \rho M_*^2 \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \phi_{\mu\nu} h_z
 \end{aligned}$$

hi\_class

$$\begin{aligned}
 & h_z \psi \rho \bar{R}_{\mu\nu} h_z \\
 & \mathcal{L}_H \alpha_H \psi \rho \mathbb{D}\phi G_0 \alpha_H \psi \rho \bar{R}_{\mu\nu} X \sqrt{-g} \alpha_H \psi \rho \bar{R}_{\mu\nu} h_z \\
 & \mathcal{L}_H \alpha_H \psi \rho \mathbb{D}\phi G_0 \alpha_H \psi \rho \bar{R}_{\mu\nu} \sqrt{-g} \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} h_z \delta \alpha_H \psi \rho \bar{R}_{\mu\nu} M_*^2 \\
 & \mathcal{L}_H \alpha_H \psi \rho \mathbb{D}\phi V_0 \mathcal{L}_H \sqrt{-g} \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} X \mathbb{D}\phi G_0 \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} h_z \delta \alpha_H \psi \rho \bar{R}_{\mu\nu} M_*^2 \\
 & \sqrt{-g} \alpha_H \psi \rho \mathbb{D}\phi \psi \rho \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \delta \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} h_z \delta \alpha_H \psi \rho \bar{R}_{\mu\nu} M_*^2 \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} h_z \delta \alpha_H \psi \rho \bar{R}_{\mu\nu} M_*^2 \\
 & \psi \delta \mathcal{P} \alpha_H \psi \rho G_0 \psi \rho \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} X \alpha_H \psi \rho \bar{R}_{\mu\nu} \theta \mathbb{D}\phi G_0 \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} h_z \delta \alpha_H \psi \rho \bar{R}_{\mu\nu} M_*^2 \\
 & R_{\mu\nu} \mathbb{D}\phi \theta_{\mu\nu} h_z \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} \theta \mathbb{D}\phi G_0 \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} h_z \delta \mathcal{P} \delta \mathbb{D}\phi G_0 \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} h_z \delta \alpha_H \psi \rho \bar{R}_{\mu\nu} M_*^2 \\
 & \phi \psi \theta_{\mu\nu} h_z \alpha_H \psi \rho \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi G_0 \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} \theta \mathbb{D}\phi G_0 \mathcal{L}_H \alpha_H \psi \rho \bar{R}_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} M_*^2 \\
 & \alpha_H \mathcal{L}_H \alpha_H \psi \rho \mathcal{P} \theta \mathbb{D}\phi \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi G_0 \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi h_z \delta \psi \rho \bar{R}_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} M_*^2 \\
 & \Gamma_{\mu}^{\nu} \Pi \delta \psi \mathcal{E} \Gamma_{\mu}^{\nu} \psi \mathcal{X} \mathcal{P} \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi G_0 \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi h_z \delta \psi \rho \bar{R}_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} M_*^2 \\
 & G_0 \mathcal{L}_H \delta \mathcal{G}_0 \mathcal{X} h_z \delta \mathcal{D}\phi \Pi \mathcal{R} \mathcal{E} \alpha_H \psi \rho \bar{R}_{\mu\nu} h_z \delta \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi G_0 \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi h_z \delta \psi \rho \bar{R}_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} M_*^2 \\
 & k^2 X \mathcal{H} \theta_{\mu\nu} \alpha_H \psi \rho \mathcal{G}_0 \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi G_0 \mathcal{L}_H \psi \rho \mathcal{P} \delta \mathbb{D}\phi h_z \delta \psi \rho \bar{R}_{\mu\nu} h_z \delta \psi \rho \bar{R}_{\mu\nu} M_*^2
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developed with [Emilio Bellini](#), [Julien Lesgourgues](#), [Iggy Sawicki](#)

# Horndeski in the Cosmic Linear Anisotropy Solving System

$\bar{G}$	$\sqrt{-g}$	$\mathcal{L}_H$	$a_H$	$\psi$	$\rho$	$P$	$\Phi$	$\theta$	$\sqrt{-g}$	$\mathcal{L}_H$	$a_H$	$\psi$	$\rho$	$\dot{x}$	$R_{\mu\nu}$	$\phi$	$q_{\mu\nu}$	$h_{\nu}$
$G_0$	$\Phi$	$a_M$	$\delta$	$\rho$	$\alpha_M$	$\Box \phi$	$G_0$	$G_0$	$\Phi$	$a_M$	$\delta$	$\rho$	$\dot{x}$	$R_{\mu\nu}$	$\psi$	$q_{\mu\nu}$	$h_{\nu}$	
$\delta$	$R_{\mu\nu}$	$\phi$	$\partial_{\mu\nu}$	$\lambda_{\mu\nu}$	$\sigma$	$X$	$h_{\mu\nu}$	$\delta$	$R_{\mu\nu}$	$\phi$	$\partial_{\mu\nu}$	$h_{\mu\nu}$	$\delta$	$R_{\mu\nu}$	$\psi$	$q_{\mu\nu}$	$h_{\nu}$	
$H$	$\delta$	$\Psi$	$h_{\mu\nu}$	$\sigma$	$\sqrt{-g}$	$\Box \phi$	$G_0$	$G_0$	$H$	$\delta$	$\Psi$	$h_{\mu\nu}$	$\sigma$	$\Omega$	$\Phi$	$\Gamma_{\mu\nu}^{\alpha}$	$\phi$	$z$
$q_{\mu\nu}$	$a_M$	$H$	$\delta$	$\rho$	$\alpha_M$	$\Box \phi$	$\alpha_T$	$q_{\mu\nu}$	$a_M$	$\delta$	$\Psi$	$h_{\mu\nu}$	$\sigma$	$P$	$X$	$G_0$	$L_H$	$M_0^2$
$\Phi$	$\Gamma_{\mu\nu}^{\alpha}$	$H$	$\Pi$	$\psi$	$\sigma$	$\Pi$	$\Pi$	$\alpha_T$	$q_{\mu\nu}$	$a_M$	$H$	$\delta$	$\sigma$	$P$	$X$	$G_0$	$L_H$	$M_0^2$
$X$	$G_0$	$L_H$	$a_M$	$\psi$	$\sigma$	$\Pi$	$G_0$	$G_0$	$X$	$G_0$	$L_H$	$\delta$	$\sigma$	$P$	$X$	$V_X$	$G_0$	$L_H$
$w$	$X^2$	$X$	$\delta$	$\partial_{\mu\nu}$	$\partial_{\mu\nu}$	$\sqrt{-g}$	$w$	$k^2$	$X$	$H$	$G_0$	$a_M$	$\alpha_M$	$\Box \phi$	$q_{\mu\nu}$	$h_{\nu}$	$H$	$V_X$
$V_X$	$G_0$	$\Box \phi$	$H$	$R$	$\alpha_M$	$\Pi$	$V_X$	$G_0$	$\Box \phi$	$G_0$	$L_H$	$\delta$	$\sigma$	$G_0$	$\Box \phi$	$q_{\mu\nu}$	$h_{\nu}$	$V_X$
$G_0$	$\Box \phi$	$G_0$	$G_0$	$\psi$	$\sigma$	$G_0$	$G_0$	$\Psi$	$G_0$	$\Box \phi$	$G_0$	$L_H$	$\delta$	$\sigma$	$G_0$	$\Box \phi$	$q_{\mu\nu}$	$h_{\nu}$
$\alpha_M$	$\Box \phi$	$\partial_{\mu\nu}$	$\Phi$	$V_X$	$\psi$	$G_0$	$G_0$	$\alpha_T$	$\Box \phi$	$\partial_{\mu\nu}$	$G_0$	$L_H$	$\delta$	$\sigma$	$G_0$	$\Box \phi$	$q_{\mu\nu}$	$h_{\nu}$
$G_0$	$G_0$	$G_0$	$G_0$	$\psi$	$\sigma$	$G_0$	$G_0$	$\alpha_T$	$\Box \phi$	$\partial_{\mu\nu}$	$G_0$	$L_H$	$\delta$	$\sigma$	$G_0$	$\Box \phi$	$q_{\mu\nu}$	$h_{\nu}$
$\delta$	$\psi$	$\alpha_M$	$X$	$\alpha_B$	$\Box \phi$	$G_0$	$G_0$	$\alpha_B$	$\Box \phi$	$G_0$	$L_H$	$\delta$	$\sigma$	$V_X$	$\alpha_B$	$\Box \phi$	$q_{\mu\nu}$	$h_{\nu}$
$\alpha_B$	$G_0$	$\alpha_B$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$

hi\_class

$h_{\mu\nu}$	$\psi$	$\rho$	$R_{\mu\nu}$	$\psi$	$R_{\mu\nu}$	$\psi$	$R_{\mu\nu}$
$H$	$\phi_{\mu\nu}$	$\delta$	$\delta$	$X$	$\Pi$	$G_0$	$\delta$
$G_0$	$\alpha_B$	$\alpha_B$	$\Box \phi$	$G_0$	$\alpha_B$	$\Box \phi$	$\alpha_M$
$\mathcal{L}_H$	$\alpha_B$	$\alpha_B$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$
$\mathcal{L}_H$	$\alpha_M$	$V_X$	$\mathcal{L}_H$	$\sqrt{-g}$	$\delta$	$\delta$	$\delta$
$\sqrt{-g}$	$\alpha_P$	$\Psi$	$\rho$	$\delta$	$X$	$\Pi$	$G_0$
$\Psi$	$\delta$	$\rho$	$\alpha_B$	$G_0$	$\Psi$	$G_0$	$\alpha_M$
$R_{\mu\nu}$	$\Box \phi$	$\partial_{\mu\nu}$	$h_{\mu\nu}$	$H$	$\Pi$	$R_{\mu\nu}$	$\phi$
$\phi$	$\Psi$	$h_{\mu\nu}$	$H$	$\Pi$	$R_{\mu\nu}$	$\phi_{\mu\nu}$	$\alpha_R$
$\alpha_M$	$H$	$\alpha_S$	$\delta$	$\delta$	$\delta$	$\delta$	$\delta$
$\Gamma_{\mu\nu}^{\alpha}$	$\Pi$	$\delta$	$\mathcal{E}$	$\mathcal{E}$	$\mathcal{E}$	$\mathcal{E}$	$\mathcal{E}$
$G_0$	$\mathcal{L}_H$	$\delta$	$G_0$	$X$	$\mathcal{L}_H$	$\delta$	$\delta$
$\delta$	$X$	$\delta$	$G_0$	$h_{\mu\nu}$	$R$	$\mathcal{E}$	$\mathcal{L}_I$
$\alpha_B$	$X$	$\delta$	$G_0$	$\alpha_B$	$\mathcal{L}_H$	$\delta$	$\delta$
$G_0$	$\delta$	$G_0$	$X$	$h_{\mu\nu}$	$\alpha_B$	$\delta$	$\delta$
$\delta$	$X$	$H$	$\delta$	$\alpha_B$	$G_0$	$G_0$	$G$

• Early modified gravity\*

• Non-linear effects:  
BAO and Bispectrum

• Ultra-large scales\*

\* at the horizon / beyond quasi-static

developed with [Emilio Bellini](#), [Julien Lesgourgues](#), [Iggy Sawicki](#)

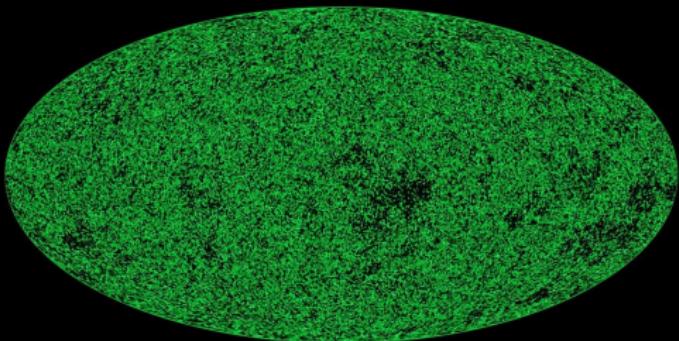
# hi\_class: How to use it...

## Linear cosmology

$$\left. \begin{array}{l} G_2, G_3, G_4, G_5 \\ \dot{\phi}(t_0), \ddot{\phi}(t_0) \end{array} \right\} \rightarrow \left. \begin{array}{l} \text{Kineticity } \alpha_K \\ \text{Braiding } \alpha_B \\ M_p \text{ running } \alpha_M \\ \text{Tensor excess } \alpha_T \end{array} \right\} \rightarrow \left. \begin{array}{l} D_A(z) \\ C_\ell \\ P(k) \\ \dots \end{array} \right.$$

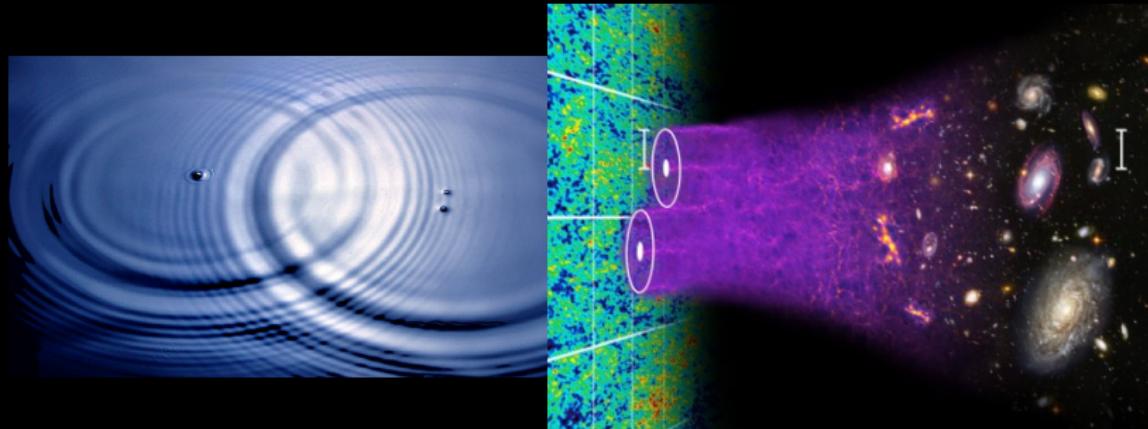
- Start with concrete model  $G$ 's + IC
  - ★ covariant Galileons  $G_2, G_3 \propto X, G_4, G_5 \propto X^2$   
...
- Start with parameterization  $\alpha$ 's +  $H$ 
  - ★  $\alpha_i = \text{constant}$
  - ★  $\alpha_i \propto \Omega_{de}$   
...

# Non-linear Effects

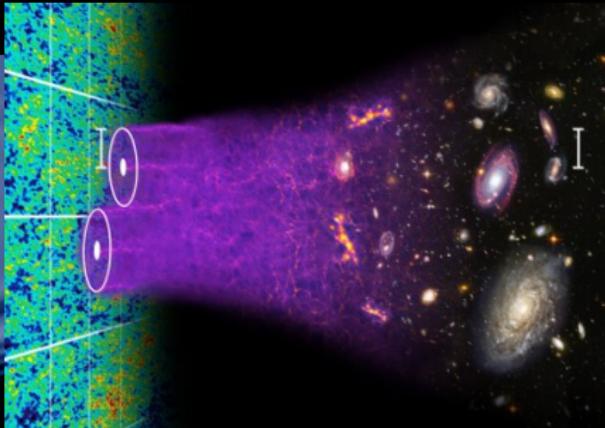
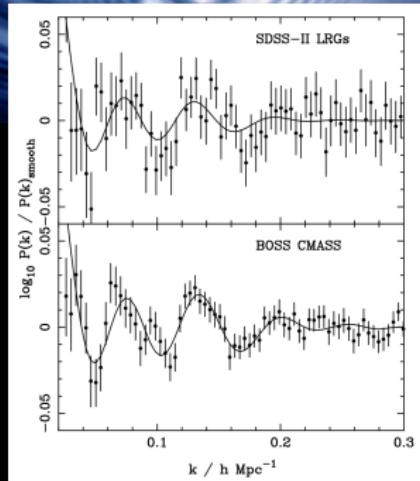
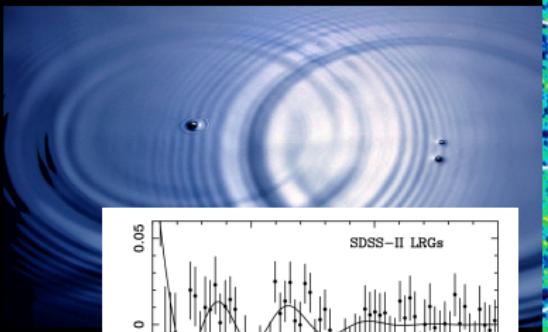


PRD 92 (2015) 6, 063522 with E. Bellini

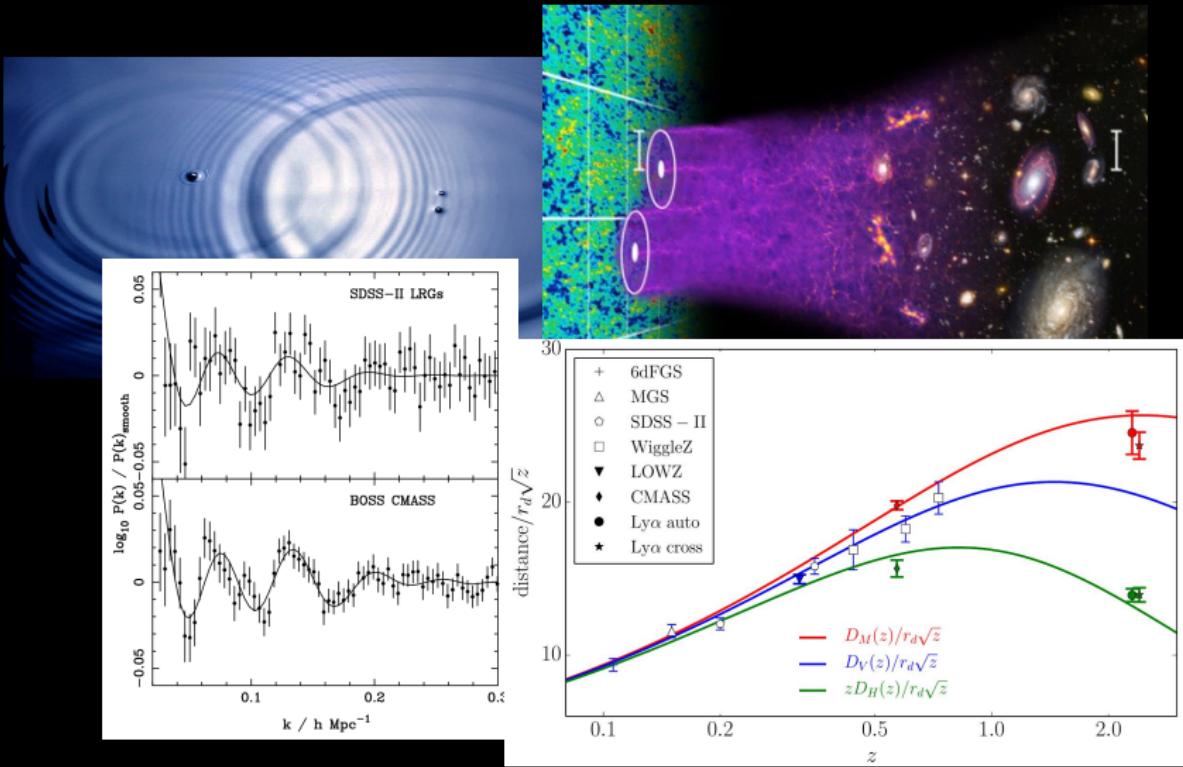
# Baryon Acoustic Oscillations



# Baryon Acoustic Oscillations



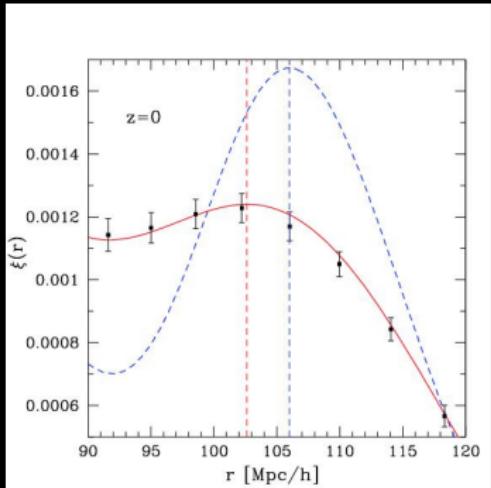
# Baryon Acoustic Oscillations



# Non-linear evolution of the BAO scale

BAO scale in the galaxy distribution → comoving standard ruler

$$r_{\text{phys}} = a(t) \cdot r_{\text{coord}}$$



(from Crocce & Scoccimarro - PRD '08)

\* BAO shift beyond Einstein gravity?

# Non-linear evolution of the BAO scale

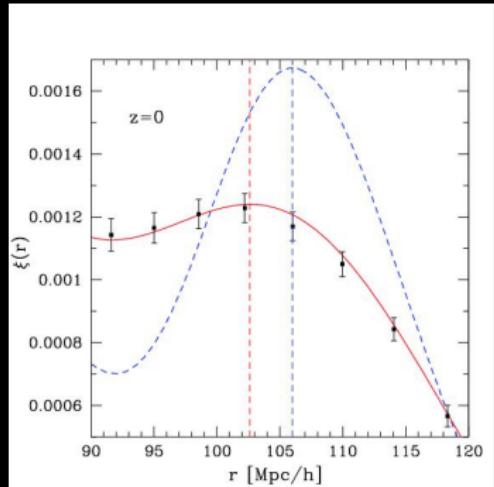
BAO scale in the galaxy distribution → comoving standard ruler

$$r_{\text{phys}} = a(t) \cdot r_{\text{coord}} + \mathcal{O}(\delta^2)$$

## Non-linear BAO evolution ( $z=0$ )

- Shift  $\sim 0.3\%$  smaller
- Broadening  $\sim 8 \text{ Mpc}/h$

(Prada *et al.* 1410.4684)



(from Crocce & Scoccimarro - PRD '08)

\* BAO shift beyond Einstein gravity?

# Eulerian perturbation theory

Adjust to a template (Padmanabhan & White '08):

$$P(k) = P_{11}(k/\alpha) \approx P_{11}(k) - \boxed{(\alpha - 1)kP'_{11}(k)}$$

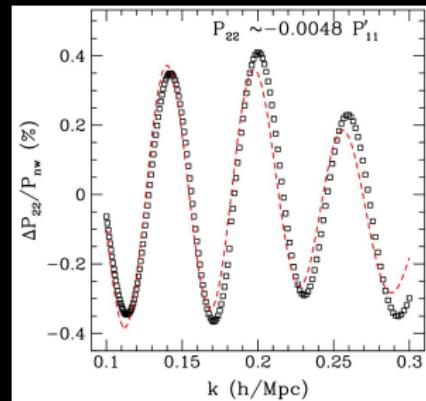
# Eulerian perturbation theory

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$$P(k) = \underbrace{P_{11}(k)}_{\text{linear}} + \underbrace{\sum_n P_{1n}(k)}_{\text{propagator}} + \underbrace{\sum_{n,m>1} P_{nm}(k)}_{\text{mode coupling}} \quad (P_{nm} \sim \langle \delta_n \delta_m \rangle)$$
$$\propto P_{11}(k)$$

- $P_{1n} \propto P_{11}$
- Mode coupling:  $\supset (\dots)kP'_{11} \propto P_{22}$



(from Padmanabhan & White - PRD'09)

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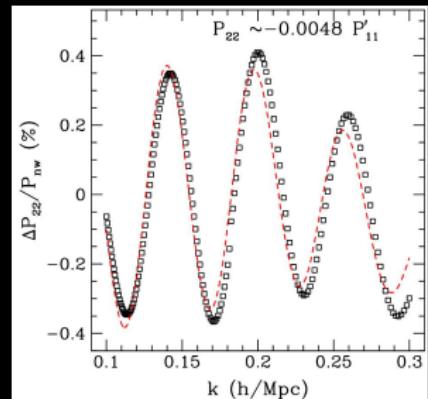
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$$\propto P_{11}(k)$$

- $P_{1n} \propto P_{11}$
- Mode coupling:  $\supset (\dots)kP'_{11} \propto P_{22}$

## Peak-background split (Sherwin & Zaldarriaga '12)

$$\alpha - 1 \approx \frac{47}{105} \sigma_{r_{BAO}}^2 \quad (\text{standard GR})$$



(from Padmanabhan & White - PRD'09)

# Mode coupling & BAO shift in modified gravity

Non-linear gravitational interactions  $\Psi = \mathcal{I}_1 \delta\rho + \mathcal{I}_2 \delta\rho^2 + \dots$

Modified mode coupling:

$$F_2(p, q, \mu) = C_0(t) + C_1(t)\mu \left( \frac{p}{q} + \frac{q}{p} \right) + C_2(t) \left[ \mu^2 - \frac{1}{3} \right]$$

Kernel restrictions:  $C_0 + \frac{2}{3}C_2 = 2C_1, \quad C_1 = \frac{1}{2}$

(Takushima *et al.* '14, Bellini *et al.* '15)

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(Takushima *et al.* '14, Bellini *et al.* '15)

Generalized shift formula (Bellini, MZ '15)

$$\alpha_k - 1 = \frac{2}{5} \left( 2C_0(t) - \frac{1}{2} \right) \sigma_{r_{BAO}}^2 \Rightarrow \begin{cases} \text{Linear growth} \\ \text{Non-linear gravity: } C_0 \neq \frac{17}{21} \end{cases}$$

# BAO Shift for Galileons: linear growth

$$\alpha_k - 1 \approx \frac{2}{5} \left( 2C_0(t) - \frac{1}{2} \right) \sigma_{r_{BAO}}^2 \Rightarrow \begin{cases} \text{Linear: } \sigma_{r_{BAO}}^2 \\ \text{Non-linear: } C_0 \end{cases}$$

- Implement Covariant Galileon in `hi_class` ✓
- Obtain  $\delta_1(z)$ ,  $P_{11}(k)$ , &  $\sigma_{r_{BAO}}$

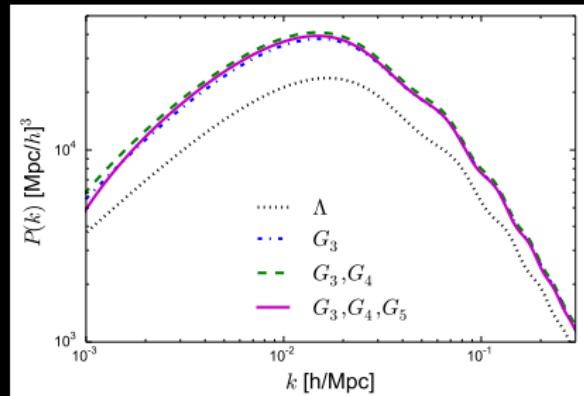
$$G_2 = -X$$

$$G_3 = c_3 X/M^3$$

$$G_4 = \frac{M_p^2}{2} + c_4 X^2/M^6$$

$$G_5 = c_5 X^2/M^9$$

Best fit models (Barreira *et al.* '14)

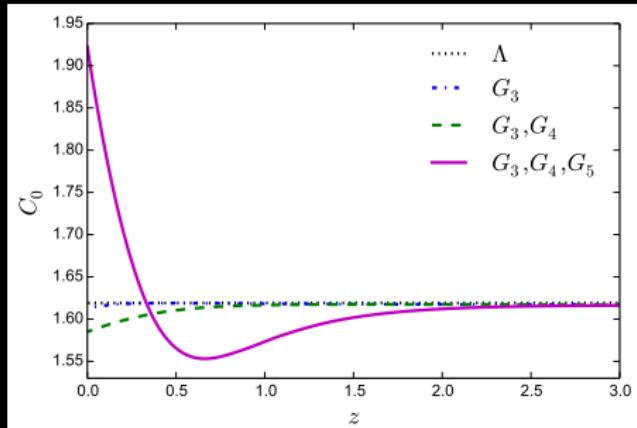


# BAO Shift for Galileons: mode coupling

$$\alpha_k - 1 \approx \frac{2}{5} \left( 2C_0(t) - \frac{1}{2} \right) \sigma_{r_{BAO}}^2 \Rightarrow \begin{cases} \text{Linear: } \sigma_{r_{BAO}}^2 \\ \text{Non-linear: } C_0 \end{cases}$$

- Expand  $\mathcal{L}_H$  over FRW:  
scalar perturbations  $\rightarrow \mathcal{O}(\delta^3)$
- Quasi-static + sub-horizon approx.
- Identify inhomogeneous sources:  
 $\ddot{\delta}_2 + \dots = S_2 [\delta_1(p), \delta_1(q)]$
- Integrate monopole component

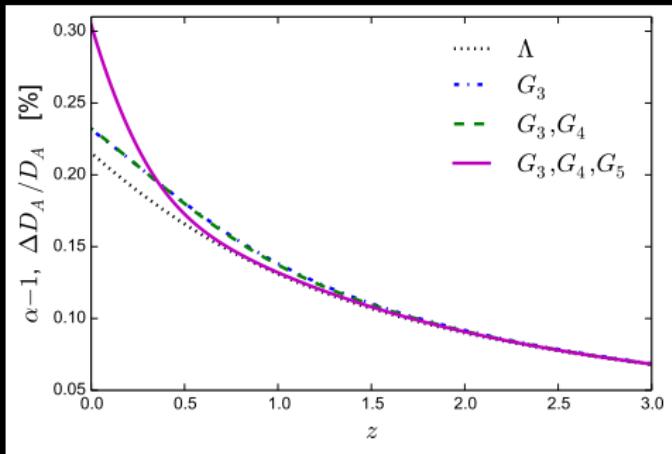
$$S_2 \longrightarrow C_0(t)$$



# BAO Shift for Galileons

$$\alpha_k - 1 \approx \frac{2}{5} \left( 2C_0(t) - \frac{1}{2} \right) \sigma_{r_{BAO}}^2 \Rightarrow \begin{cases} \text{Linear: } \sigma_{r_{BAO}}^2 \\ \text{Non-linear: } C_0 \end{cases}$$

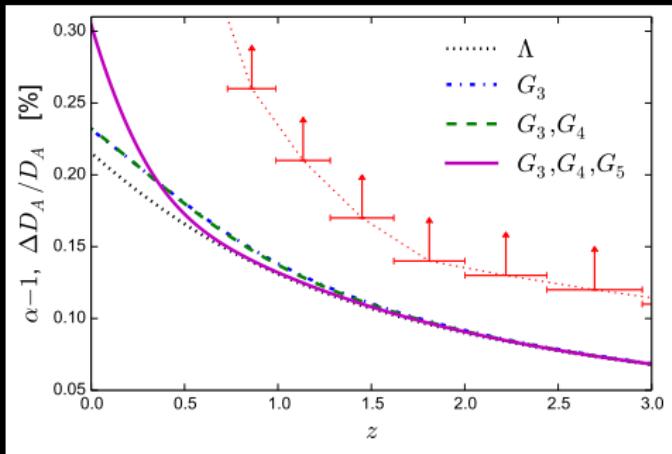
- Can have significant enhancement at  $z \sim 0$



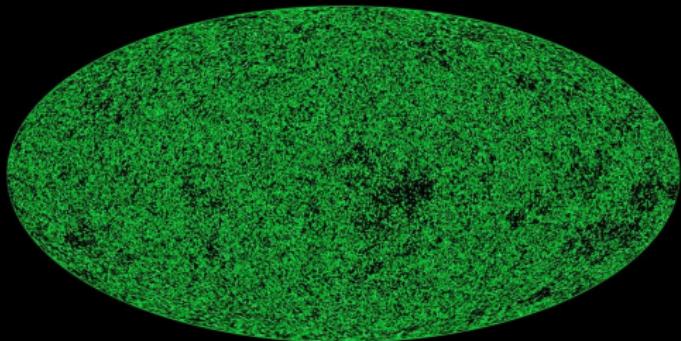
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$$\alpha_k - 1 \approx \frac{2}{5} \left( 2C_0(t) - \frac{1}{2} \right) \sigma_{r_{BAO}}^2 \Rightarrow \begin{cases} \text{Linear: } \sigma_{r_{BAO}}^2 \\ \text{Non-linear: } C_0 \end{cases}$$

- Can have significant enhancement at  $z \sim 0$
- Forecast  $\Rightarrow$  irrelevant...  
(Weinberg *et al.* '12)
- But interesting NL effects...



# Ultra-large Scales



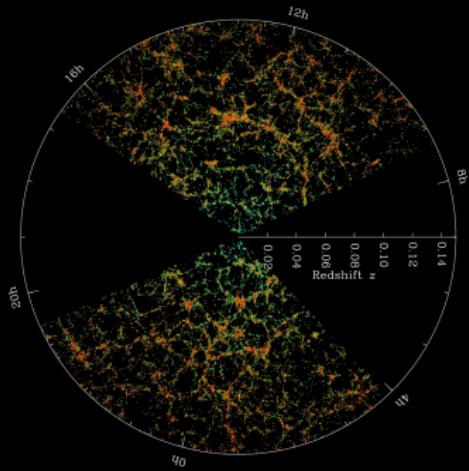
Janina Renk's Master Thesis  
with L. Amendola and F. Montanari

160x.xxxxx

# Counting Galaxies

Galaxy catalogues:

- observe angles and redshift:  $(\hat{n}, z)$

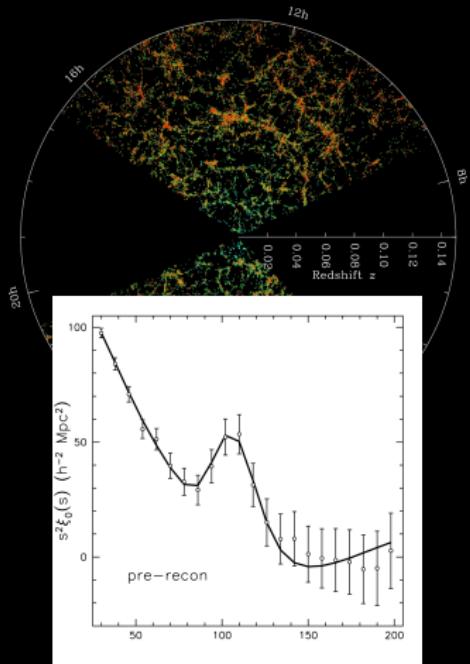


SDSS collaboration

# Counting Galaxies

Galaxy catalogues:

- observe angles and redshift:  $(\hat{n}, z)$
- project  $(\hat{n}, z) \rightarrow \vec{x} \rightarrow \boxed{\xi(r)}$   
→ assumes  $H(z)$ !



SDSS collaboration

# Counting Galaxies

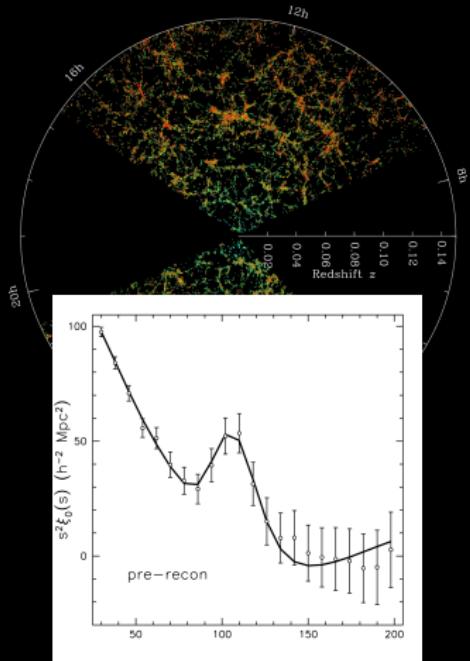
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→ assumes  $H(z)$ !

## Galaxy Number Counts

$$\Delta(\hat{n}, z) = \frac{n_g(\hat{n}, z) - \langle n_g \rangle(z)}{\langle n_g \rangle(z)}$$

- Observable  $\Rightarrow$  Gauge invariant
- Consistent with any model
- Well defined on all scales

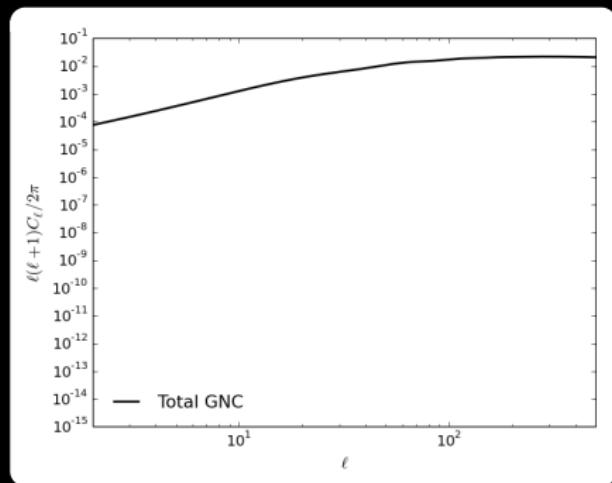


SDSS collaboration

# Relativistic effects (Yoo et al. '09, Bonvin & Durrer '11, Challinor & Lewis '11)

$$\Delta(\hat{n}, z) = \underbrace{\Delta_\delta + \Delta_{\text{rsd}}}_{\xi(r, \mu)} + \underbrace{\Delta_\kappa + \Delta_v + \Delta_{\text{pot}}}_{\text{relativistic effects}}$$

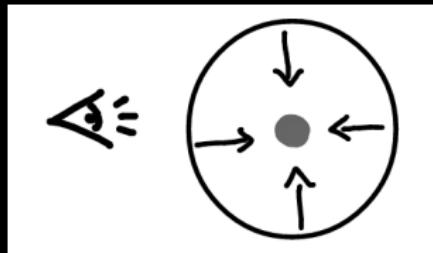
Correlations:  $\langle \Delta(\hat{n}, z) \Delta(\hat{n}', z') \rangle = \sum_l \frac{2l+1}{4\pi} C_l(z, z') P_l(\cos(\theta))$



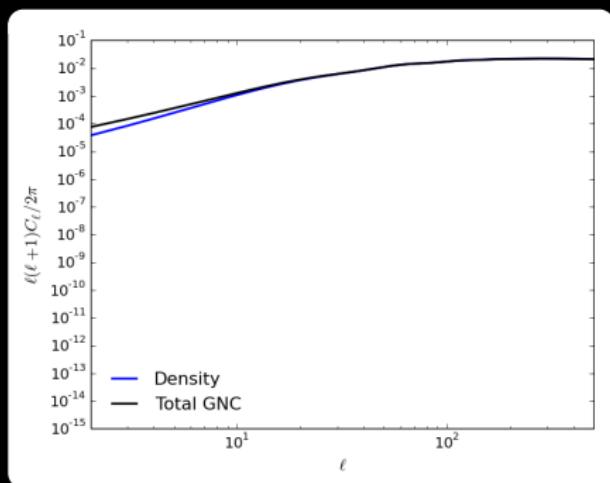
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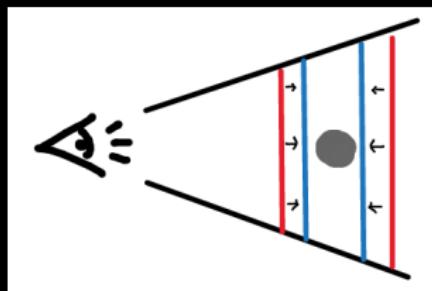
Newtonian Clustering



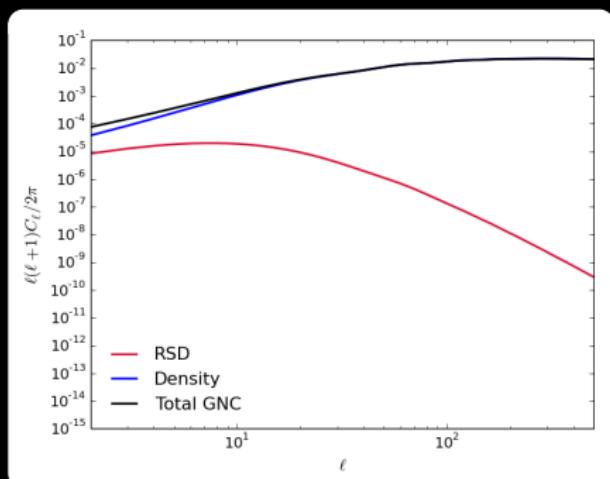
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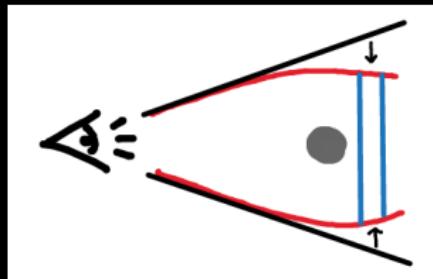
Redshift-Space Distortions



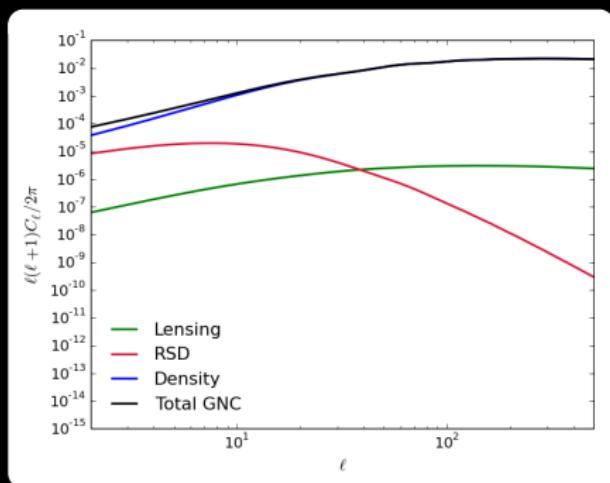
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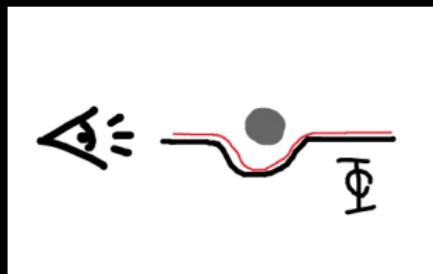
Lensing Magnification



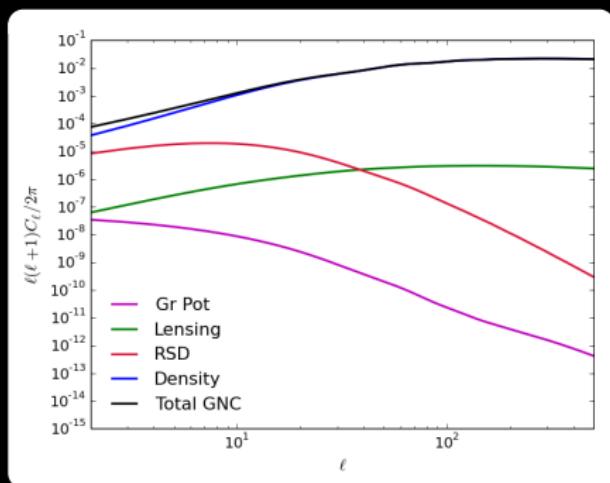
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GR effects: time delay,  
ISW, SW...

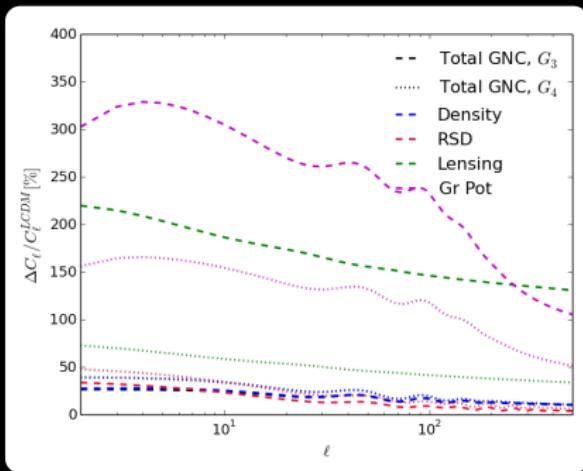
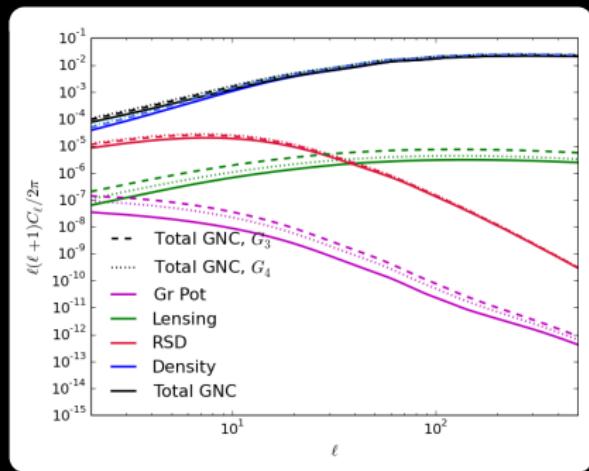


# Relativistic effects in Horndeski Gravity

- `hi_class + class_Gal` (Di Dio, Montanari et al. '13)

# Relativistic effects in Horndeski Gravity

- hi\_class + class\_Gal (Di Dio, Montanari et al. '13)

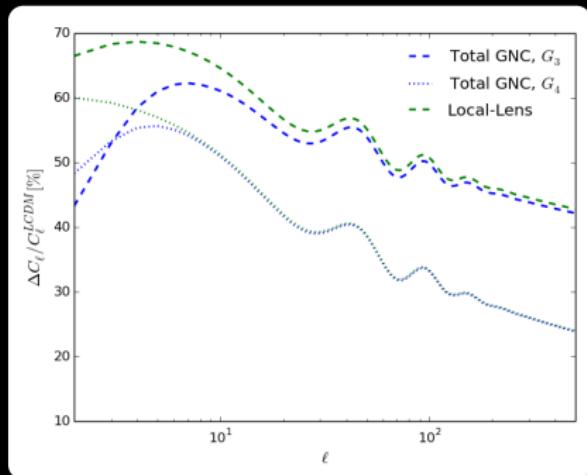
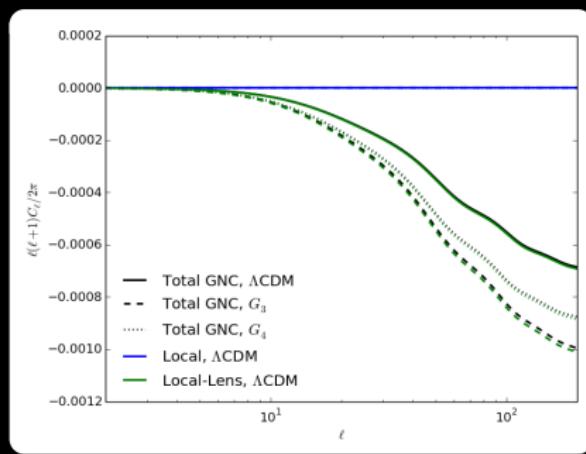


- Galileon  $\Rightarrow$  modified  $\Phi, \Psi \Rightarrow \uparrow$  Lens. & GR effects
- $z = z' = 0.3$   $\Rightarrow \uparrow$  correction for  $\downarrow$  dominant effect

$$\Delta \text{GR} > \Delta \text{lens} > \Delta \text{RSD} > \Delta \text{density}$$

# Relativistic effects in Horndeski Gravity

- Cross-correlated different redshifts (Montanari & Durrer '15)



- $z = 0.3, z' = 1 \Rightarrow$  Correction from lensing magnification
- Departures hard to measure

# Conclusions

- Contemporary scalar-tensor cosmology well understood
- Early MG strongly constrained:  $\alpha_M \lesssim 10^{-3}$ ,  $\alpha_T \lesssim 10^{-2}$   
Stability priors + effects on the CMB
- BAO: great standard ruler  
(even for extreme gravity in future surveys)
- Ultra-large scales:  
rel. effects enhanced but hard to measure
- Lots to learn about gravity in new regimes
  - ★ non-linear
  - ★ at the Horizon

Kiitos paljon

# hi\_class

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