# Observational signatures of non-GR theories gravity in cosmology



#### **HIP - Cosmology Seminar**

### Why modified gravity ?

# 1) Extend tests of gravity onto cosmological scales

 <u>The study of alternatives to GR tells us</u> about what to look for in the data.

#### 2) Cosmic acceleration

 <u>The "dark energy" may simply be a</u> <u>breakdown of GR on large scales.</u>

#### 3) GR is not a quantum theory

 Not unreasonable to suspect that a theory that fixes GR on quantum scales, may also differ from it on cosmological ones.

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**Beyond General Relativity ...** 

1) The Universe can expand at different rates.

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**Beyond General Relativity ...** 

1) The Universe can expand at different rates.

2) The gravitational force law is modified, but cannot in the Solar System !

#### **Modified Poisson Eq.**



#### "Standard" Poisson Eq.

$$\nabla^2 \Phi_{GR} = 4\pi G\rho$$

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Low density

If 
$$\rho \ll 1 \longrightarrow \nabla^2 \varphi \sim \rho$$

$$\frac{\nabla^2 \Phi}{\nabla^2 \Phi_{GR}} = 1 + \mathcal{O}(1)$$

**Order unity corrections.** 

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**Order unity corrections.** 

**High density** 

If 
$$\rho \gg 1 \longrightarrow \nabla^2 \varphi \sim \sqrt{\rho}$$

$$\frac{\nabla^2 \Phi}{\nabla^2 \Phi_{GR}} = 1 + \frac{1}{\sqrt{\rho}} \approx 1$$

**Recover standard GR**.

$$S = \int d^4 x \sqrt{g} \left[ \frac{R}{16\pi G} + \mathcal{L}_m + \frac{\Lambda}{8\pi G} \right]$$

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$$S = \int d^4 x \sqrt{g} \left[ \frac{R}{16\pi G} + \mathcal{L}_m + \frac{m^2}{6} R \Box^{-2} R \right]$$

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GR curvature term  

$$Particle physics and DM$$
Suff that accelerates  

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Action of the Dvali-Gabadadze-Porrati model (hep-th/0005016)

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- Matter and radiation are confined to a 4D brane (our spacetime) of a 5D bulk
- Gravity "leaks" from the brane to the bulk.



### Crossover scale $1 C^{(5)}$



Measure of the scales on the brane above which gravity becomes 5-dimensional.

#### Modified dynamical potential

$$\Psi = \Psi^{\rm GR} + \varphi/2$$

"Fifth force potential" governed by

#### Equation of motion of the additional scalar field

$$\nabla^2 \varphi + \frac{r_c^2}{3\beta(a)a^2} \left[ \left( \nabla^2 \varphi - \left( \nabla_i \nabla_j \varphi \right)^2 \right) \right] = \frac{8\pi G}{3\beta(a)} a^2 \delta \rho_m$$
$$\beta(a) = 1 + 2Hr_c \left( 1 + \frac{\dot{H}(a)}{3H^2(a)} \right)$$

Hubble expansion rate: will tune it to yield exactly LCDM, but this is not necessary!

$$H(a) = H_0 \sqrt{\Omega_{m0} a^{-3} + \Omega_{de}(a) + \Omega_{rc}} + \sqrt{\Omega_{rc}}$$

#### Fifth to normal force ratio profiles



#### Fifth to normal force ratio profiles



#### Fifth to normal force ratio profiles



### In the rest of this talk ...

1) Validating estimates of the growth rate of structure in modified gravity.

Barreira, Sánchez & Schmidt

Phys. Rev. D (2016)

arXiv:1605.03965

In the quest for ever precise measurements in cosmology, are we giving accuracy away ?

#### 2) Lensing by galaxy troughs in modified gravity.

Barreira, Bose, Li, Llinares

JCAP02(2017)031

arXiv:1605.08436

Can we find evidence of screening by comparing the lensing signal from over- and underdense regions?

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### The growth rate of structure

#### What we observe





### The growth rate of structure



### The growth rate of structure



# Step by step

**1)** Construct galaxy mock catalogues out of N-body simulations of both GR and DGP gravity.

**2)** Analyse the mocks with observational pipelines, as if analysing real data.

**3)** Check whether returned values of the growth rate are consistent with the cosmology of the simulations.

Yes ?

Can use measurements to test the desired theories.



Measurements are biased! Cannot use to test the theories.



**1)** Construct galaxy mock catalogues with N-body simulations of both GR and DGP gravity

→ This exercise has been standard practice for GR, but not modified gravity!

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 $\rightarrow$  Constraints on modified gravity have been placed ignoring that the data could be biased.

Yes?

No?

Can use measurements to test the desired theories.

Measurements are biased! Cannot use to test the theories.

### Modified gravity simulations

#### Equation of motion of the additional scalar field

$$\nabla^2 \varphi + \frac{r_c^2}{3\beta(a)a^2} \left[ \left( \nabla^2 \varphi - \left( \nabla_i \nabla_j \varphi \right)^2 \right) \right] = \frac{8\pi G}{3\beta(a)} a^2 \delta \rho_m$$

- 1. Discretize on AMR grid;
- 2. Iterate to find the scalar field at every AMR cell;
- 3. Construct total potential;
- **4. Standard N-body code with modified potential until next time step.**

$$\Psi = \Psi^{\rm GR} + \varphi/2$$

ECOSMOG code :

Baojiu Li et al arXiv:1110.1379 arXiv:1303.0008

 Modified gravity N-body code comparison project: Winther et al arXiv 1506.06384. All codes compared check out!

### Modified gravity simulations



### Modified gravity simulations



### Halo occupation distribution (HOD)

#### (i) Parametrize the number of galaxies that live in haloes of a given mass;

$$N_{\text{galaxies}}(M) = N_{\text{central}} + N_{\text{satellite}}$$

$$N_{\text{central}} = \frac{\Theta(M - M_{\min})}{2} \Big[ 1 + \operatorname{erf}\Big(\frac{\log_{10}M - \log_{10}M_{\min}}{\sigma_{\log_{10}M}}\Big) \Big]$$

$$N_{\text{satellite}} = N_{\text{central}}\Big(\frac{M - M_0}{M_1'}\Big)^{\alpha}$$

(ii) Assign galaxies to each halo by sampling from the HOD distribution;
 Centrals → position and velocity of the halo center

Satellites → position and velocity of randomly chosen halo particles

(iii) Tune the HOD parameters to match desired galaxy sample.

### Halo occupation distribution (HOD)







Clustering wedges (Sánchez et al 2013, 2014, 2016)

$$\xi_{\mu_1}^{\mu_2}(s) = \frac{1}{\mu_2 - \mu_1} \int_{\mu_1}^{\mu_2} \frac{\xi(s,\mu) \,\mathrm{d}\mu}{\mathrm{d}\mu}$$

$$\xi_{\perp}$$
 ::  $\mu_1 = 0$  ,  $\mu_2 = 0.5$   
 $\xi_{\parallel}$  ::  $\mu_1 = 0.5$  ,  $\mu_2 = 1$ 

s = galaxy pair separation

 $\mu = \text{cosine angle of pair with LOS}$ 

**Redshift space galaxy 2-point correlation function.** 

Measured directly from the mocks.





**Mode-coupling** 

$$P_{\rm NL}(k) = P_{\rm lin}(k)G(k)^2 + P_{\rm MC}(k)$$


# "Observing" the mocks



# "Observing" the mocks





No evidence for a biased performance in the DGP model !





But this is not necessarily the case for all (i) gravity

**Unbiased performance** of the clustering wedges model in DGP then permits **using results from real data** to constrain DGP gravity.



# Lensing by galaxy troughs in modified gravity.

Barreira, Bose, Li, Llinares JCAP02(2017)031 arXiv:1605.08436

Can we find evidence of screening by comparing the lensing signal from over- and underdense regions?

#### Motivation

#### Weak lensing by galaxy troughs in DES data Gruen et al, arXiv:1507.05090 2 G≧G. Lensing around overdense LOS *θ*\_=30' -0 10-1 Lensing around underdense LOS G≦G, -2 10 100 $\theta$ [arcmin]

#### Motivation

#### Weak lensing by galaxy troughs in DES data Gruen et al, arXiv:1507.05090 2 Lensing around overdense LOS *θ*\_=30' Lensing around underdense LOS What does the fifth force do G≤G this lensing signal? 10 100 $\theta$ [arcmin] Does the screening discriminate between underdense/overdense LOS?

# A variant of the DGP model

Modified dynamical potential

$$\Psi = \Psi^{\rm GR} + \varphi/2$$

$$\Phi_{\rm len} = \Phi_{\rm len}^{\rm GR}$$

In the nDGP model, the lensing potential is the same as in GR (for fixed mass)

$$\Phi_{\rm len} = \Phi_{\rm len}^{\rm GR} + \varphi/2$$

Introduce a phenomenological variant "nDGPlens" that directly modifies lensing.

Take parameter bordeline consistent with growth rate constraints

$$r_c H_0 = 1$$

Ray-Ramses : Lensing on the fly with the N-body simulations

Barreira, Llinares, Bose and Li arXiv:1601.02012



Evaluate the lensing convergence integral on the fly with the N-body simulations.

$$\kappa = \frac{1}{c^2} \int_0^{\chi_s} \frac{\chi \left(\chi_s - \chi\right)}{\chi_s} \nabla_{2D}^2 \Phi_{\text{len}} \, \mathrm{d}\chi$$





- All boxes simulate structure formation, but only do ray integrations during the redshift range associated with their position in the tile.
- Use different initial conditions to avoid repetition of structures.



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- All boxes simulate structure formation, but only do ray integrations during the redshift range associated with their position in the tile.
- Use different initial conditions to avoid repetition of structures.
- Total lensing signal is the sum of the contribution from each box.
   <u>Beware of 1st order Born approximation</u>: unperturbed photon trajectories.



# $\Lambda \text{CDM}$

Lensing modified because of modified <u>dynamical</u> potential (different LSS).

nDGP

Lensing modified because of modified *lensing* potential (same LSS).

 $\mathrm{nDGP}_{\mathrm{lens}}$ 



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Construct a "pseudo" halo lightcone using two output times per box.



Construct a "pseudo" halo lightcone using two output times per box.

#### The G field : projected halo number counts within some aperture.

$$\begin{aligned} G(\vec{\theta}) &= \sum_{i=1}^{N_{\text{halo}}} W_{\text{sel,i}} \left( \theta_T, z_l, z_u, M_{\min} \right) \\ W_{\text{sel,i}} &= \begin{cases} 1, & |\vec{\theta} - \vec{\theta_i}| \leq \theta_T, z_i \in [z_l, z_u], M_i \geq M_{\min} \\ 0, & \text{otherwise} \end{cases} \end{aligned}$$











#### M\_halo > 5e12 Msun/h 0.1 < z\_halo < 0.76



Fifth force has the same impact on G20/G80 LOS, despite them probing low/high density regions.

M\_halo > 5e12 Msun/h 0.1 < z\_halo < 0.76 No evidence for screening effects !!





M\_halo > 5e12 Msun/h Two redshift bins No evidence for screening effects !!

**Convergence** profiles



Fifth force effects are of the same size for other quantile choices.

Absence of screening als halo redshift binning.



 $\theta_T = 10', \,\, M_{
m min} = 1.0E + 13 \,\, M_\odot/h$ 

M\_halo > 1e13 Msun/h Different quantiles
# Screening with halo lensing

**Stacked halo lensing** 



# Screening with halo lensing



# Screening with halo lensing



- Lensing around G80 LOS is dominated by the mass between haloes, not inside.
- G80 LOS are overdense, just not enough to "trigger screening".

# Shear profiles



### Summary

#### 1) Validating estimates of the growth rate of structure.



Clustering wedges model used on BOSS DR12 data is compatible with DGP-like cosmologies.

But this is not necessarily the case for all (i) gravity models,(ii) range of scales, etc.

Always ensure compatibility between theory and data analysis !

### Summary

#### 1) Validating estimates of the growth rate of structure.



arcmin