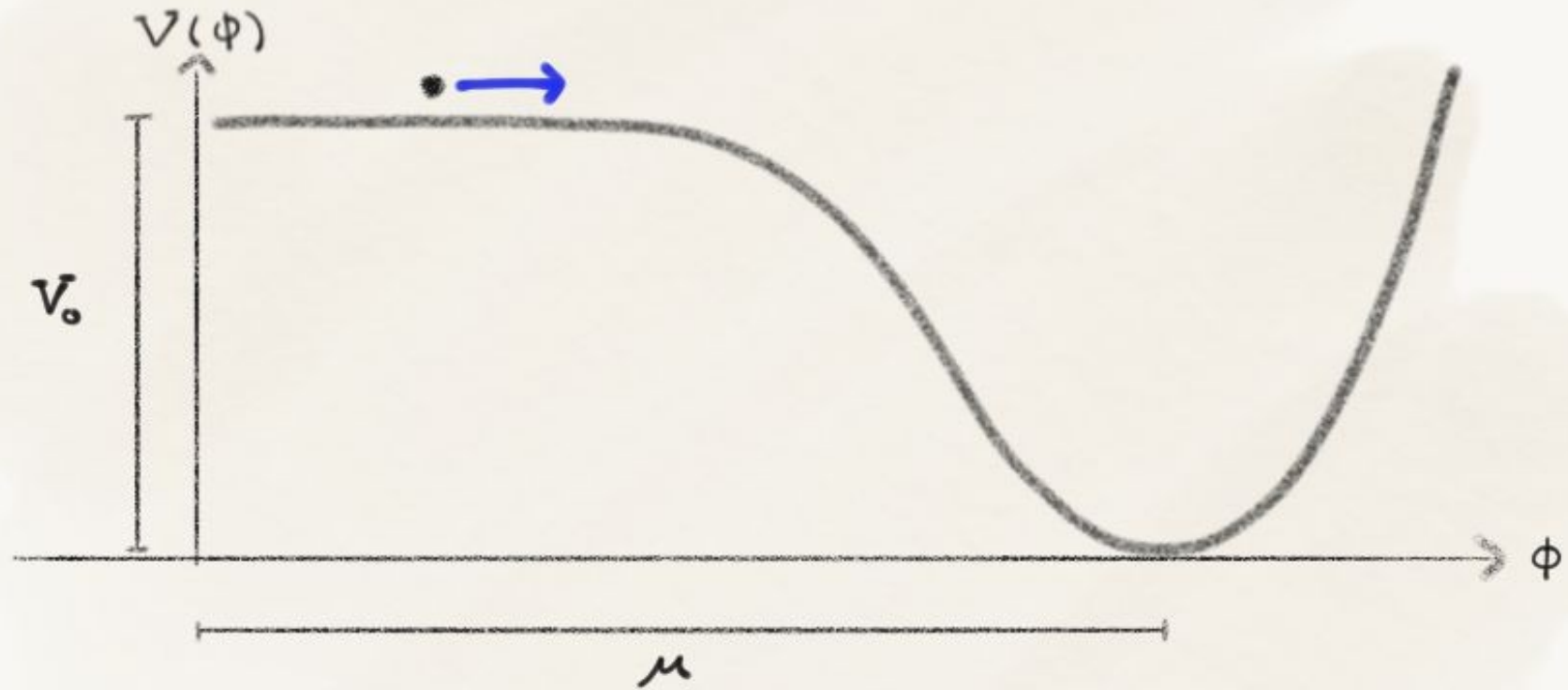


SWAMP CREATURES OF THE INFLATION LANDSCAPE

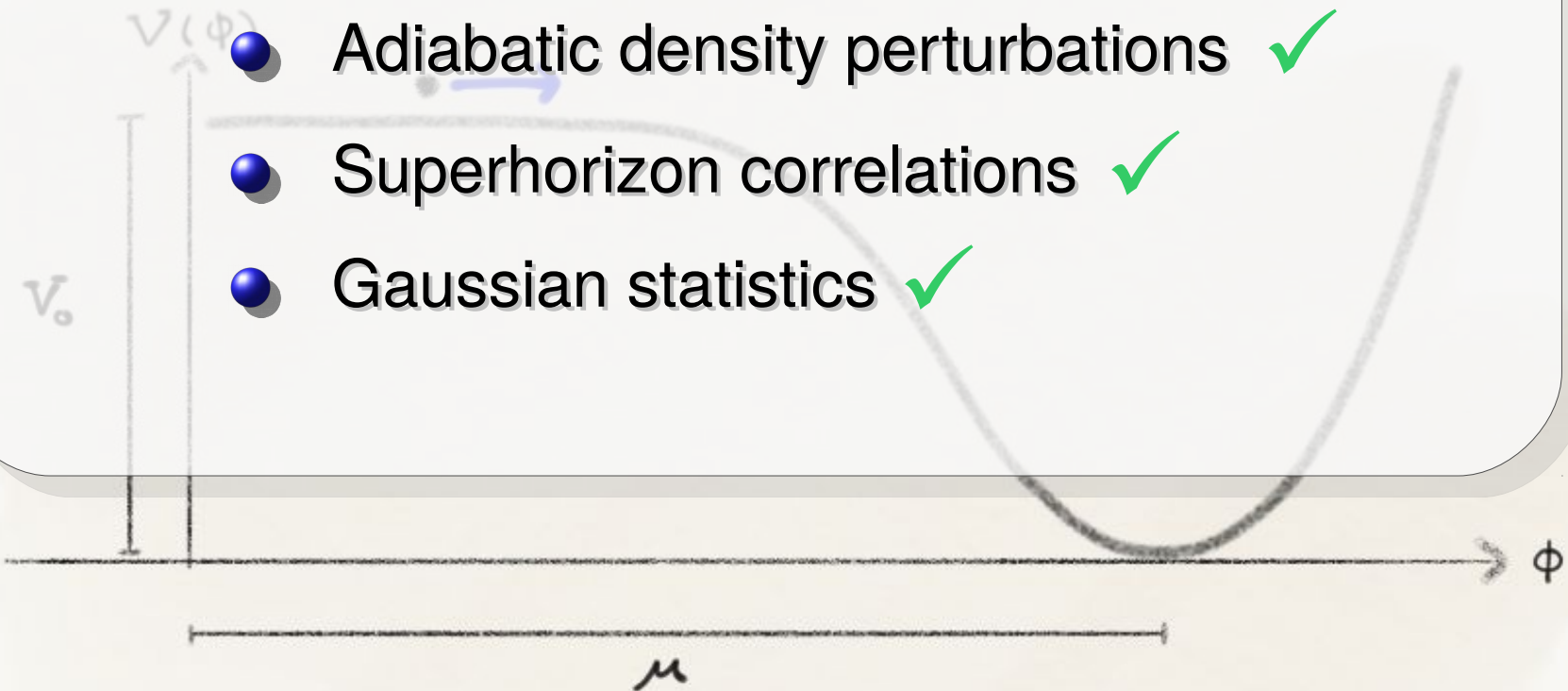


Will Kinney
Helsinki Institute of Physics
3 April 2019

Inflation: Basic Predictions



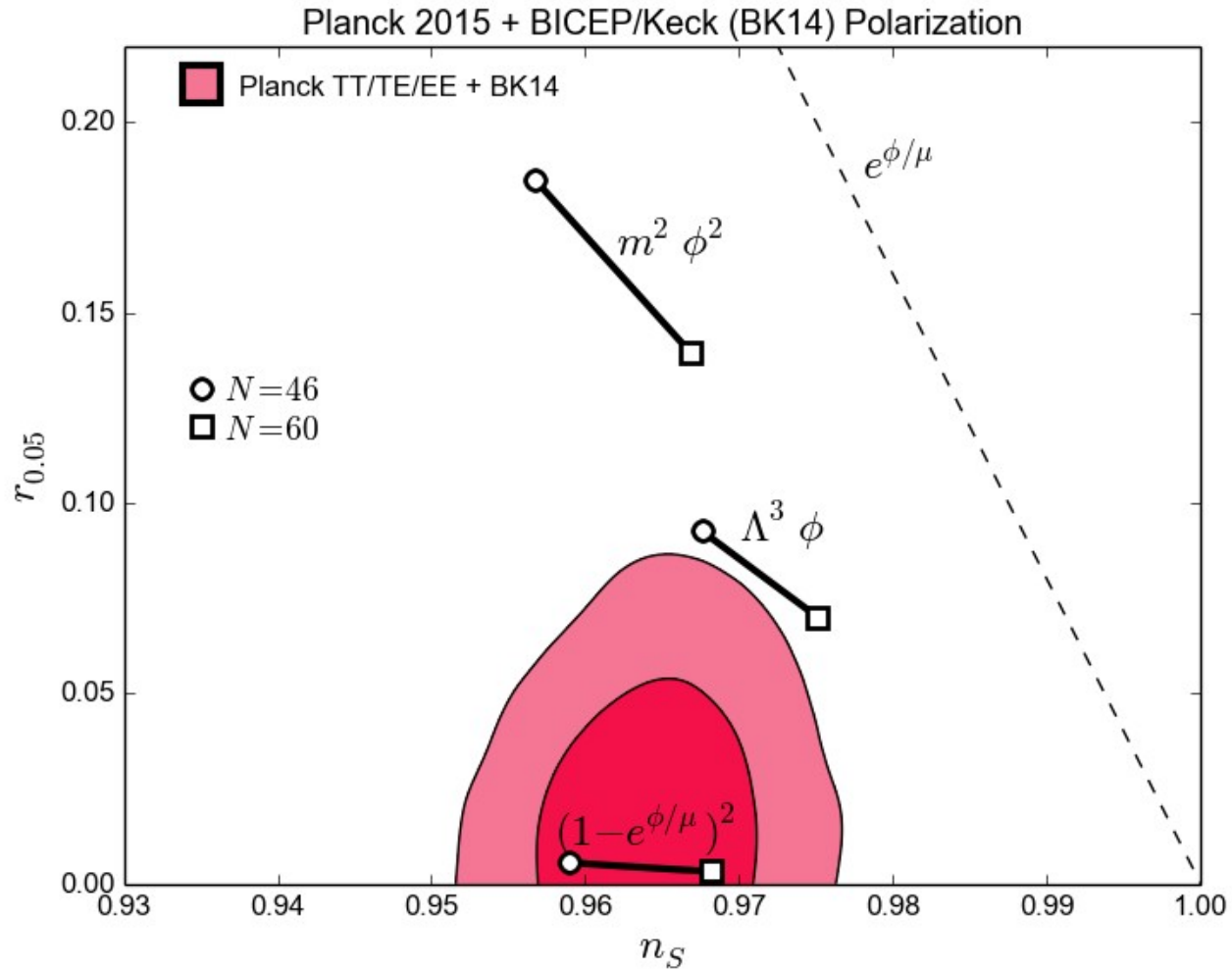
Inflation: Basic Predictions



$$\mathcal{L} = \frac{1}{2} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - V(\phi)$$

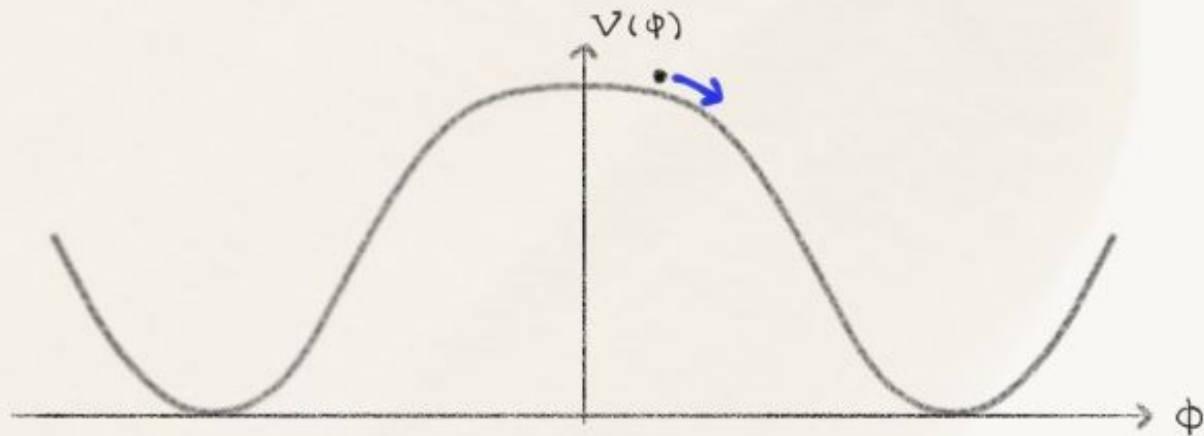
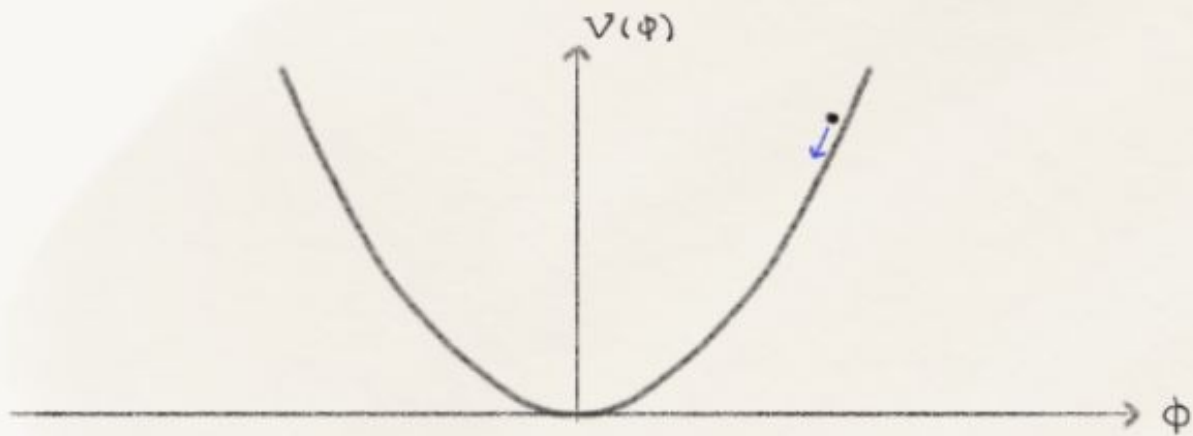
Fully consistent with data.

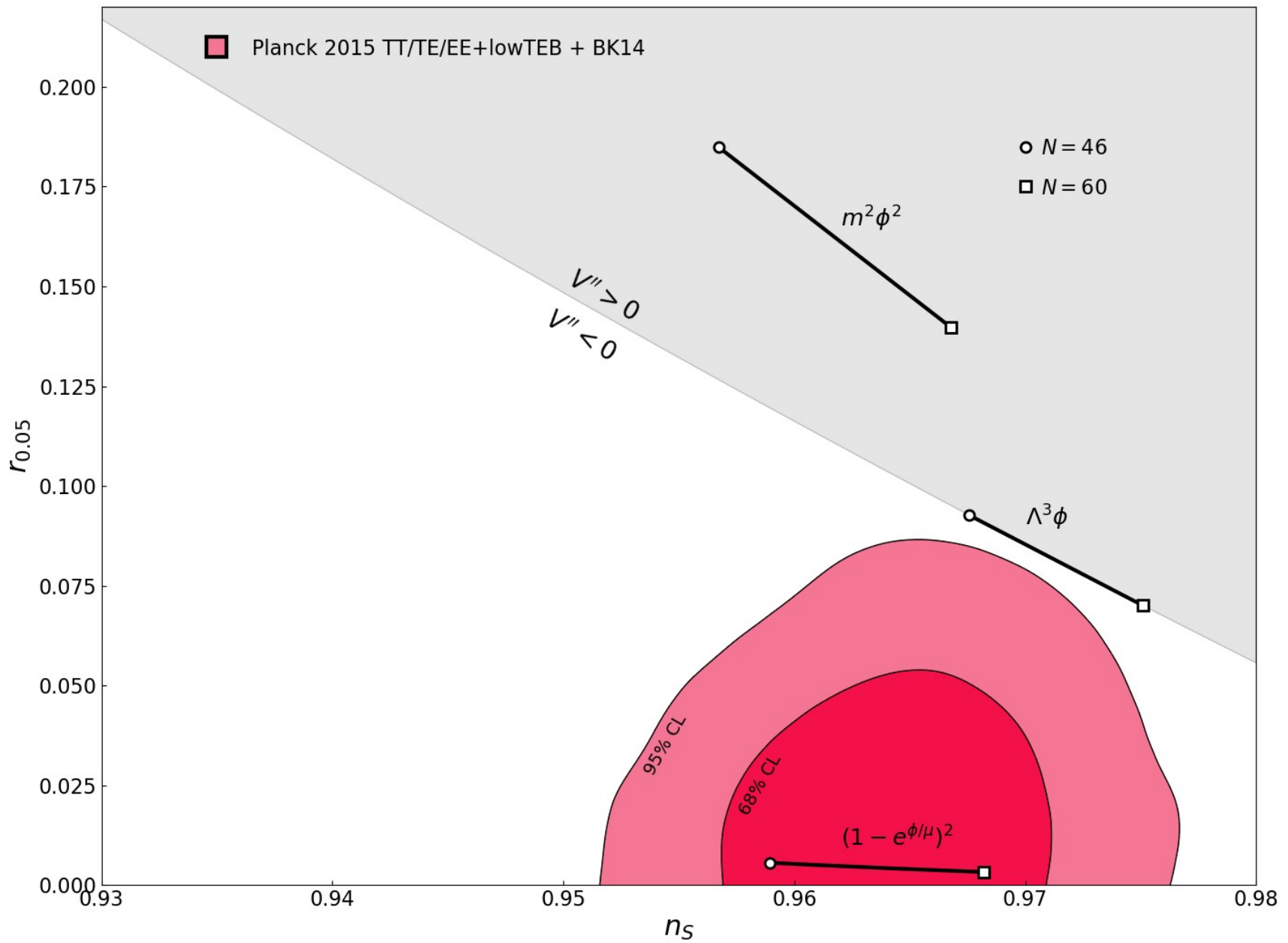
$$r = 8M_P^2 \left(\frac{V'}{V} \right)^2$$



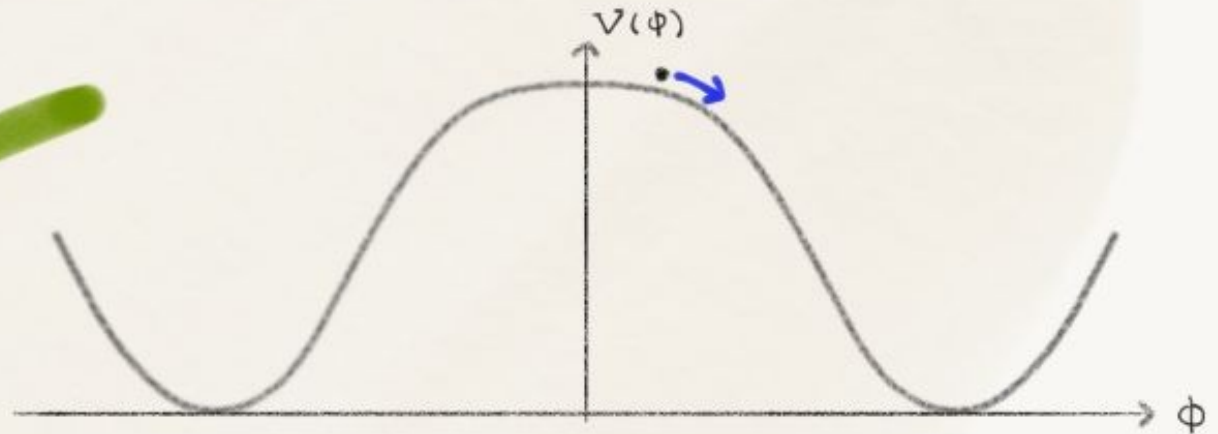
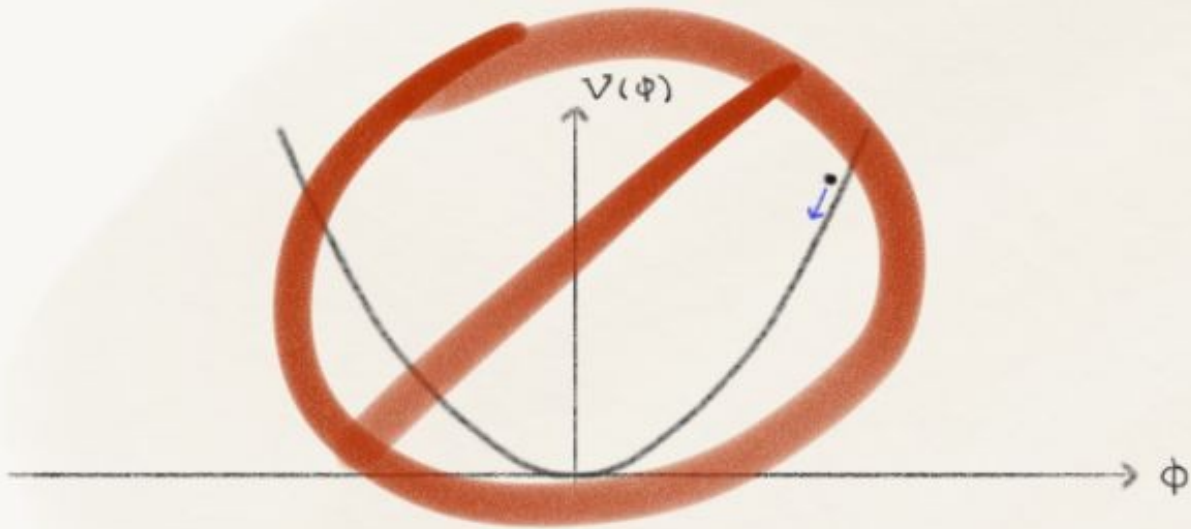
$$n_S = 1 - 3M_P^2 \left(\frac{V'}{V} \right)^2 + 2M_P^2 \frac{V''}{V}$$

Convex or Concave?





Convex or Concave?

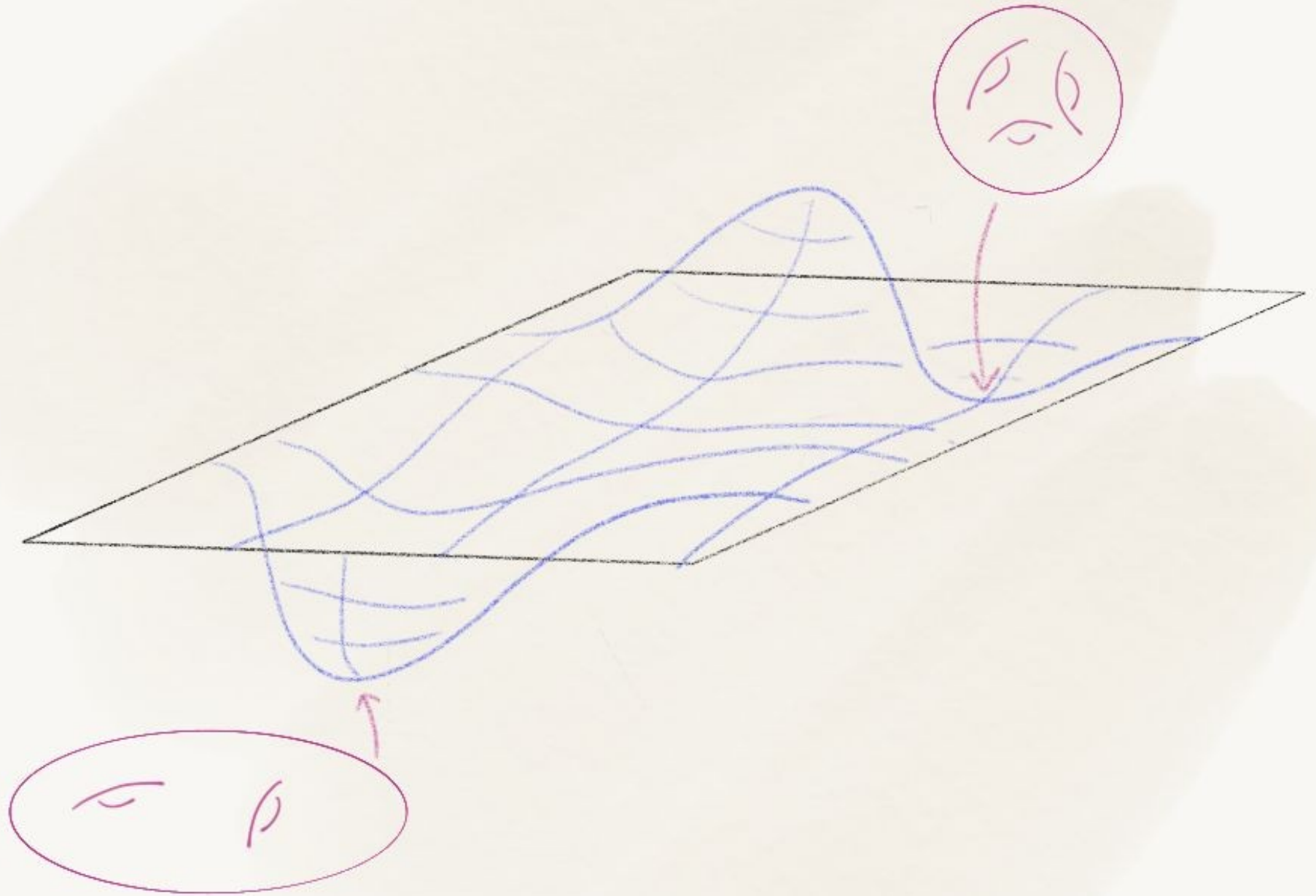


Inflation: Swampland or Landscape?



WHK, Vagnozzi, Visinelli [arXiv:1808.0624]

The String Landscape





NO UV COMPLETION



NO UV COMPLETION



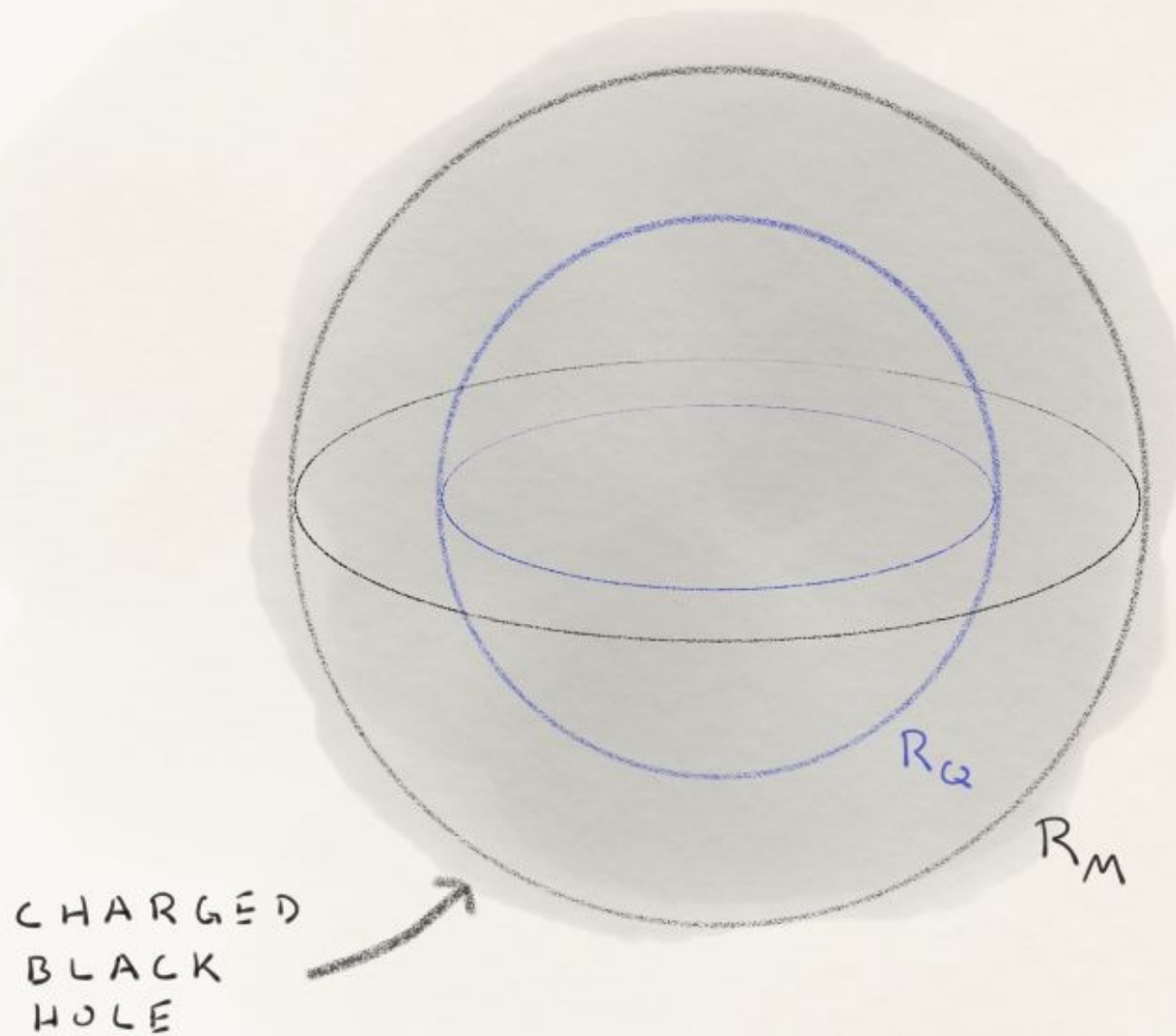
The Marshland Conjecture

[David M.C. Marsh](#), [J.E. David Marsh](#)

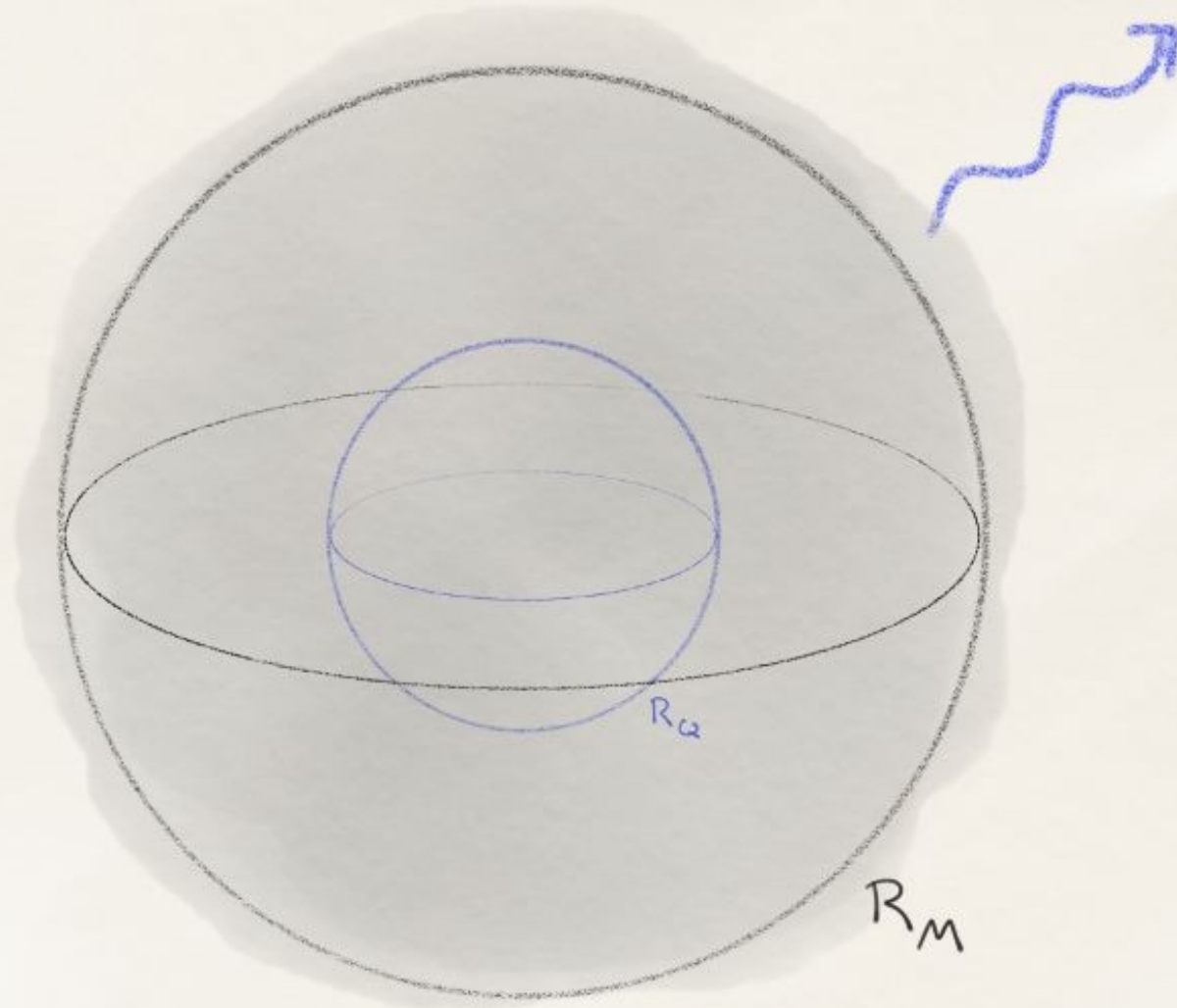
(Submitted on 29 Mar 2019)

We posit the existence of the Marshland within string theory. This region is the boundary between the landscape of consistent low-energy limits of quantum gravity, and the swampland of theories that cannot be embedded within string theory because they violate certain trendy and obviously uncontroversial conjectures. The Marshland is probably fractal, and we show some pretty pictures of fractals that will be useful in talks. We further show that the Marshland contains theories with a large number of light axions, allowing us to cite lots of our own papers. We show that the Marshland makes up most of the volume of the landscape, and admits a novel, weakly broken \mathbb{Z}_2 Marshymmetry that we find strong evidence for by considering a carefully crafted example.

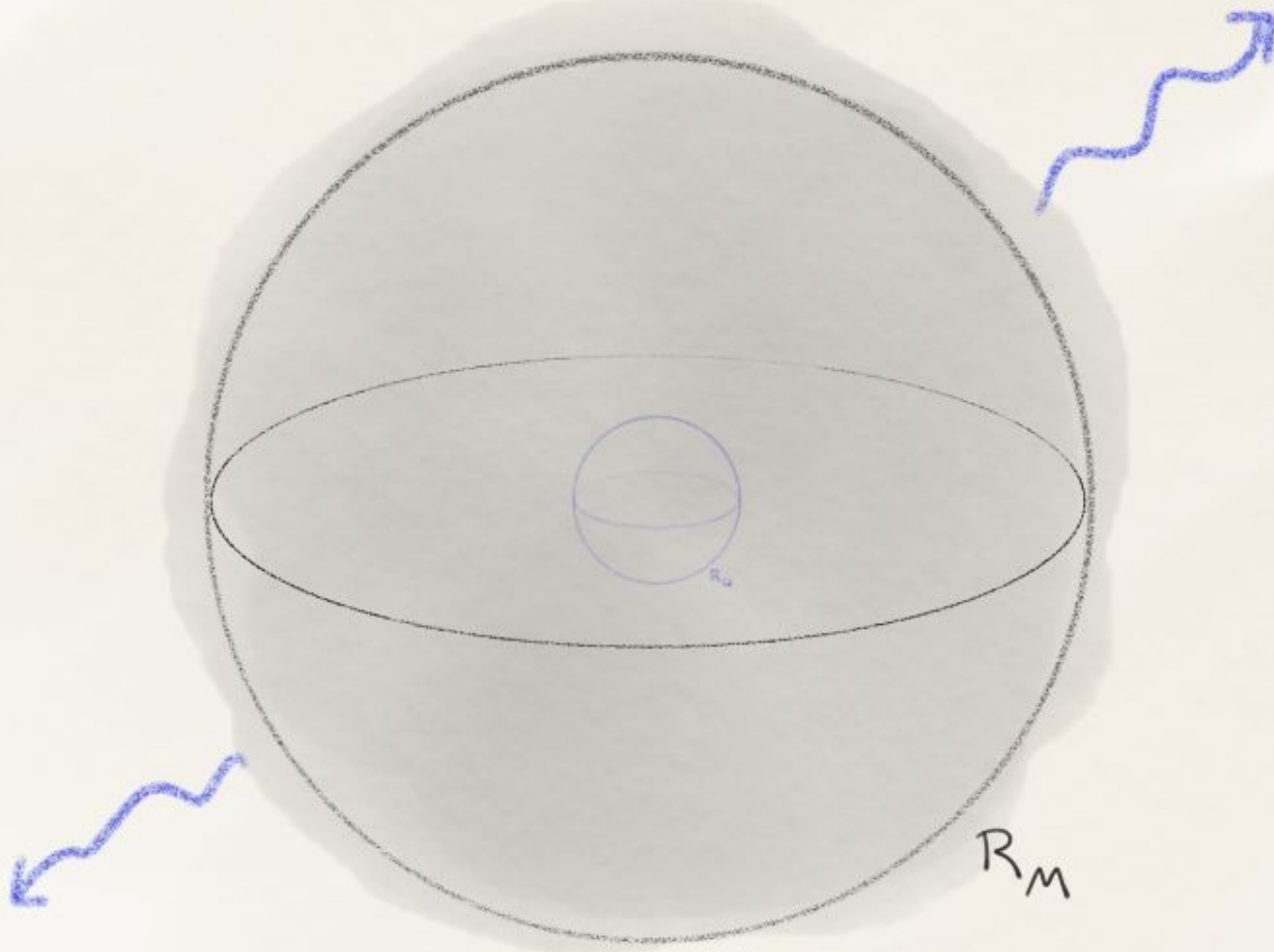
The Weak Gravity Conjecture



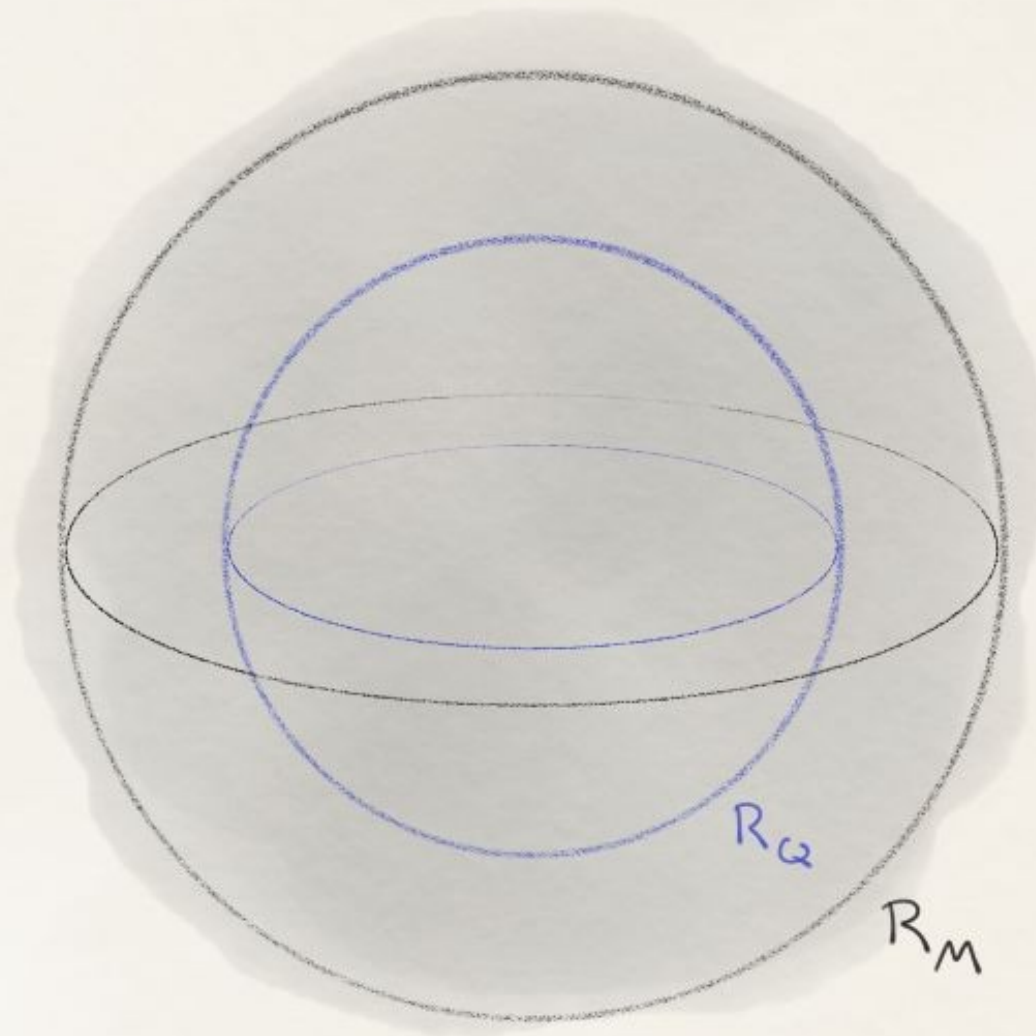
The Weak Gravity Conjecture



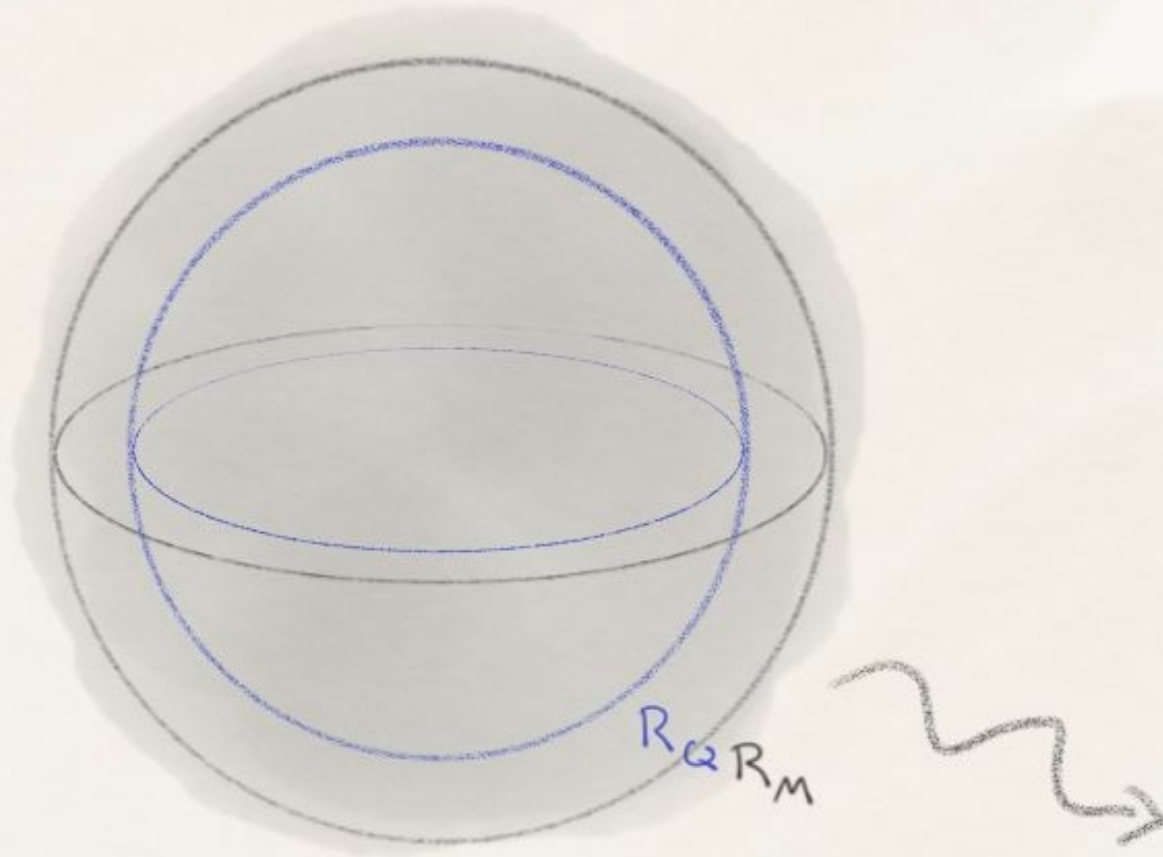
The Weak Gravity Conjecture



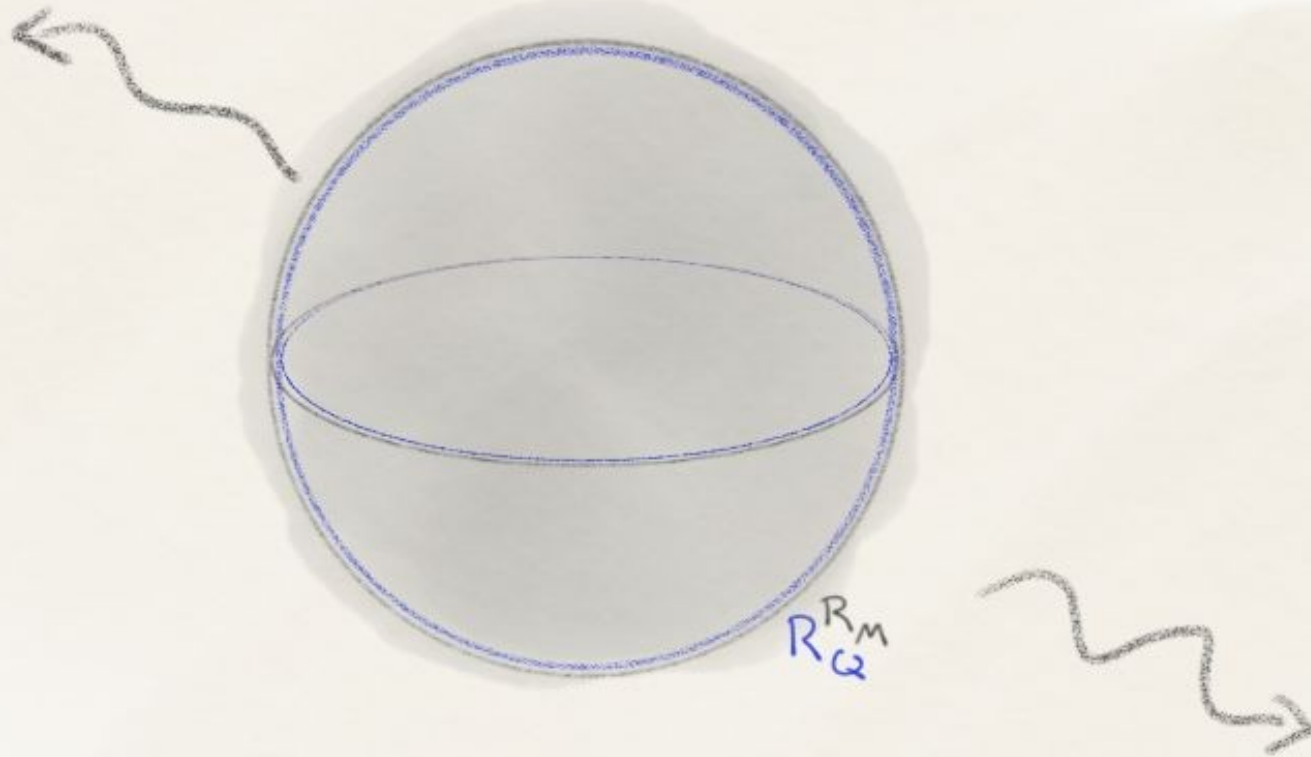
The Weak Gravity Conjecture



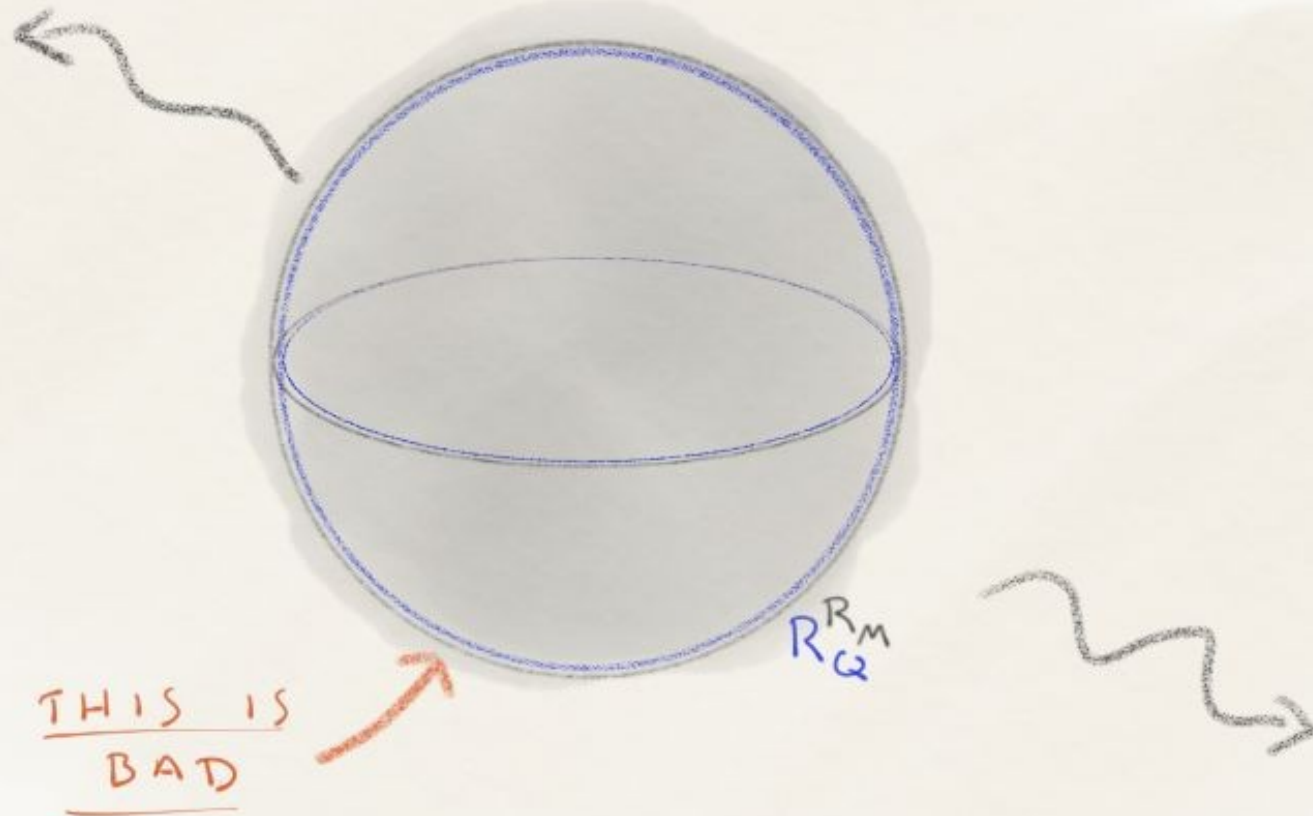
The Weak Gravity Conjecture



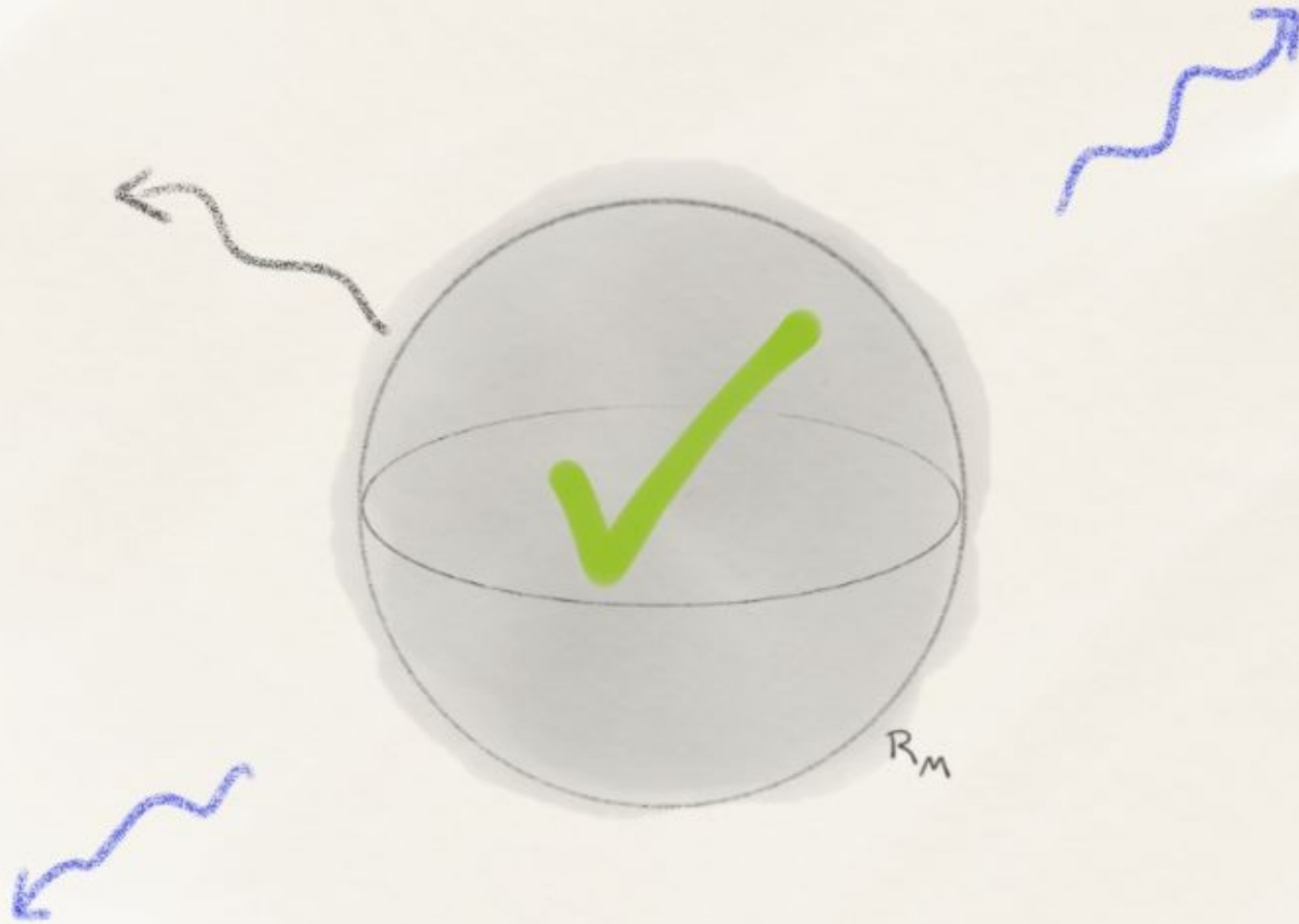
The Weak Gravity Conjecture



The Weak Gravity Conjecture



The Weak Gravity Conjecture



The Weak Gravity Conjecture

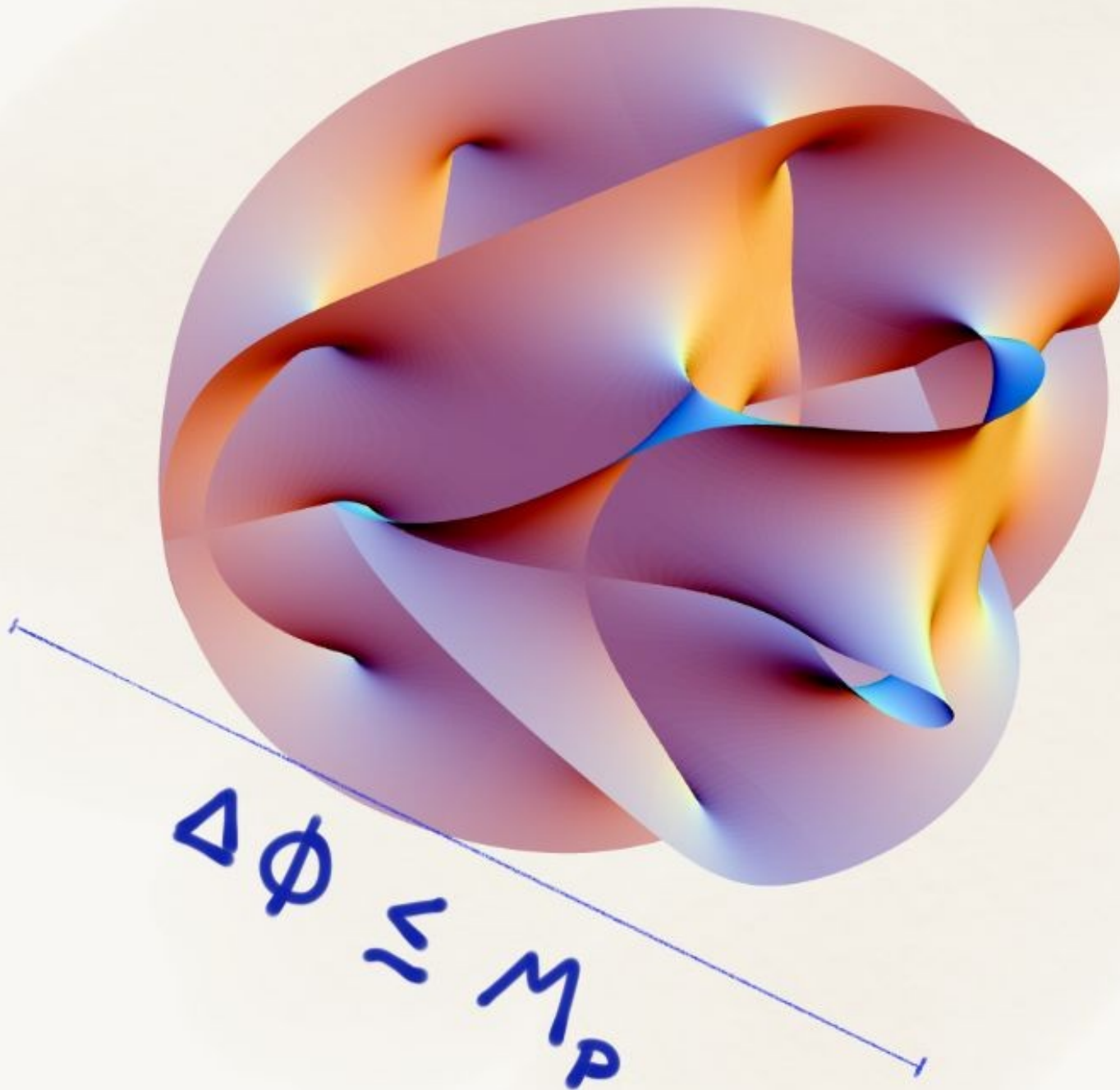
Any UV-complete theory must contain light charged states under all global symmetries.

$$M < Q M_P \quad \forall U(1)$$

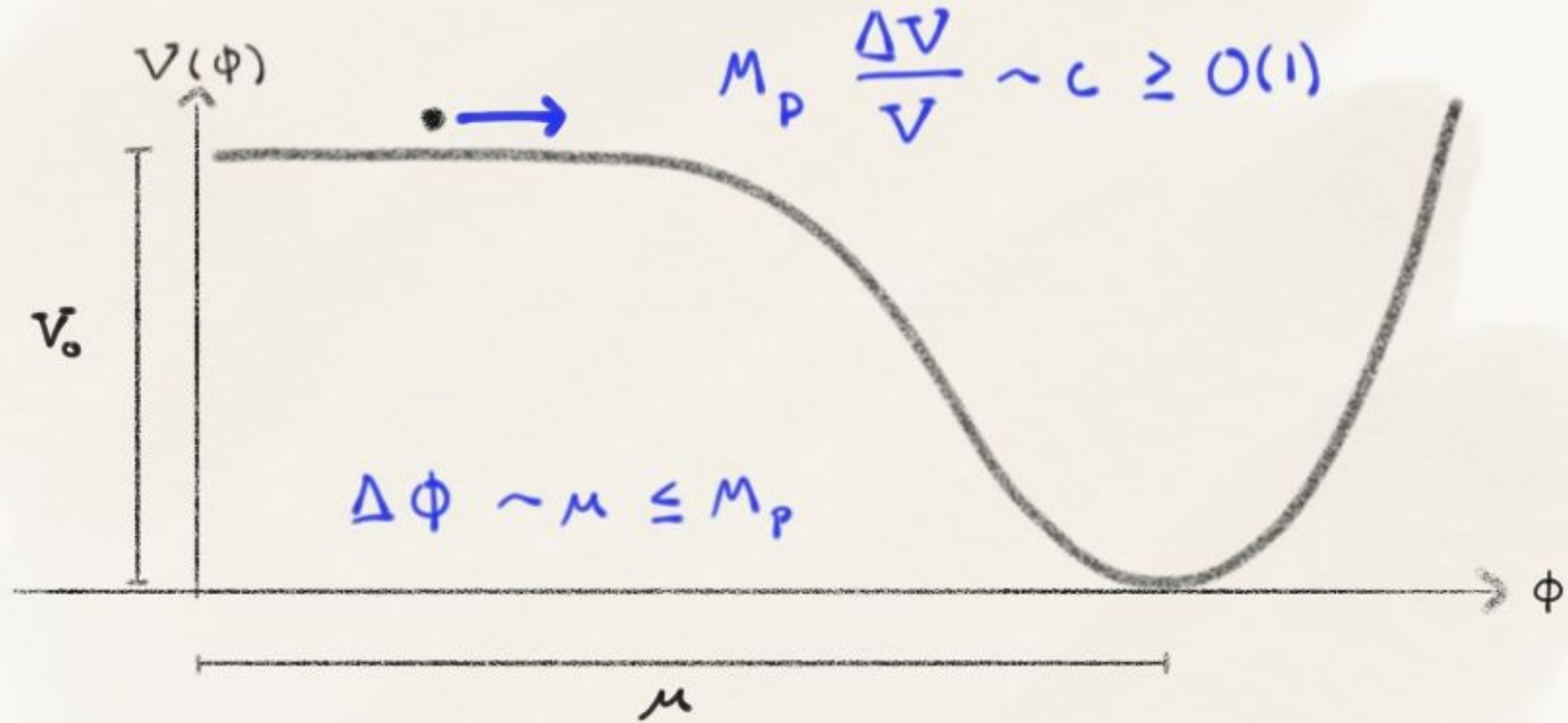
R_Q

R_M

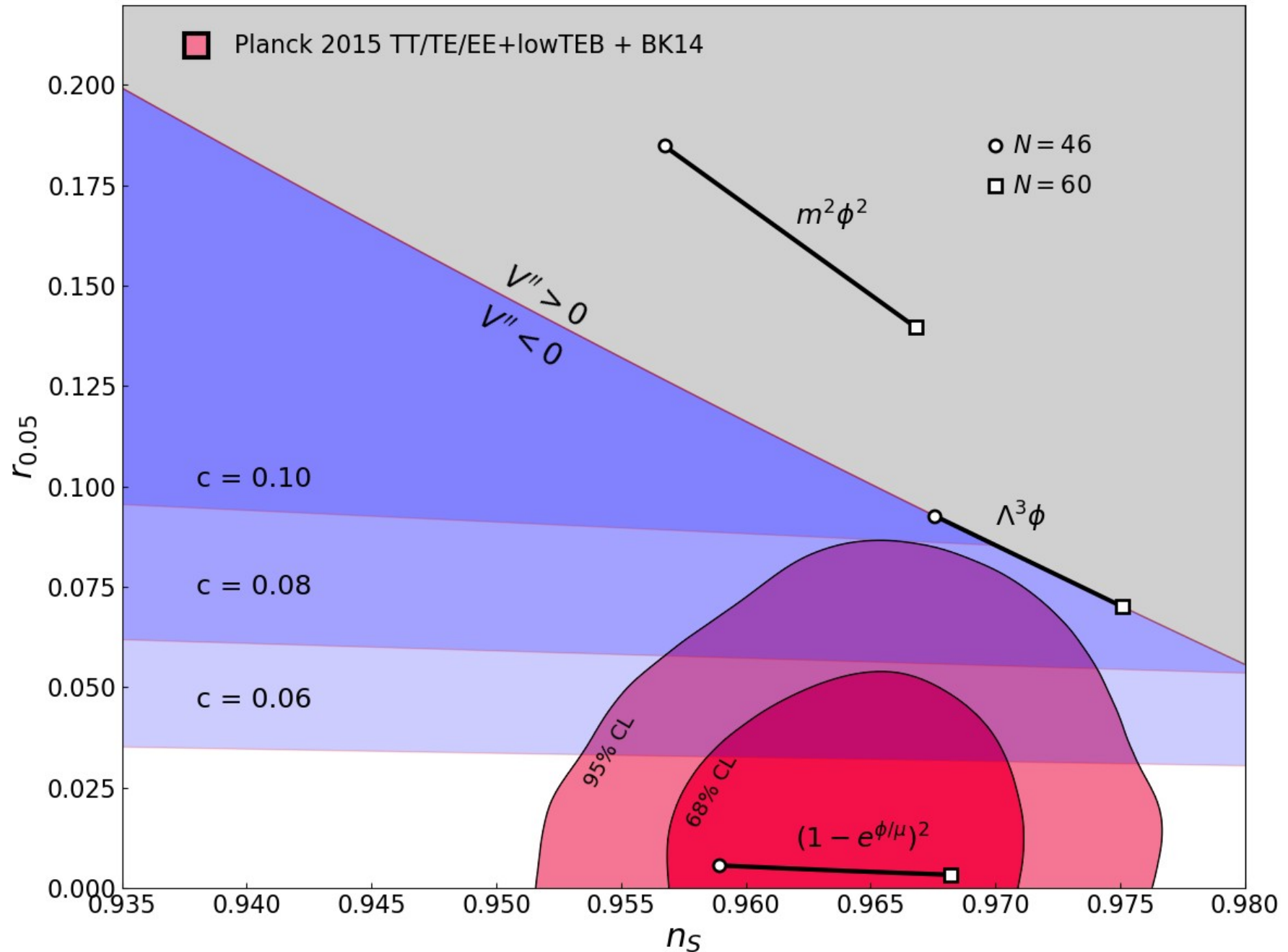
The deSitter Swampland Conjecture



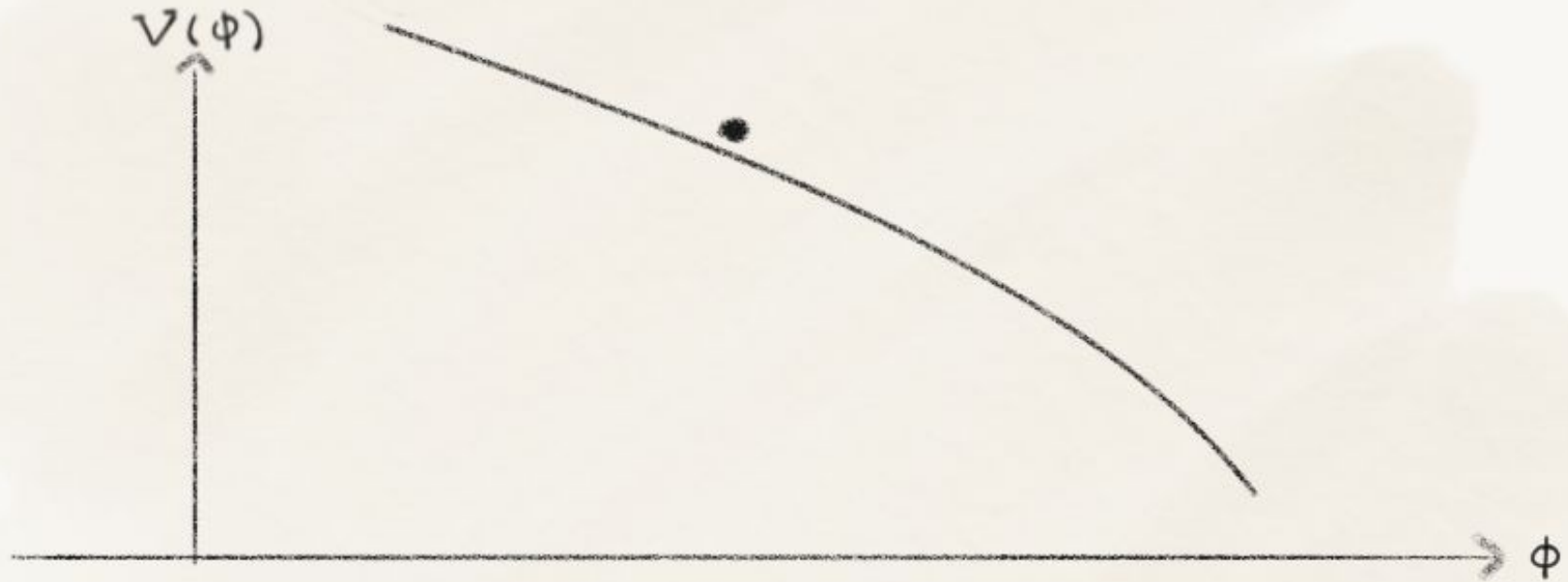
The de Sitter Swampland Conjecture



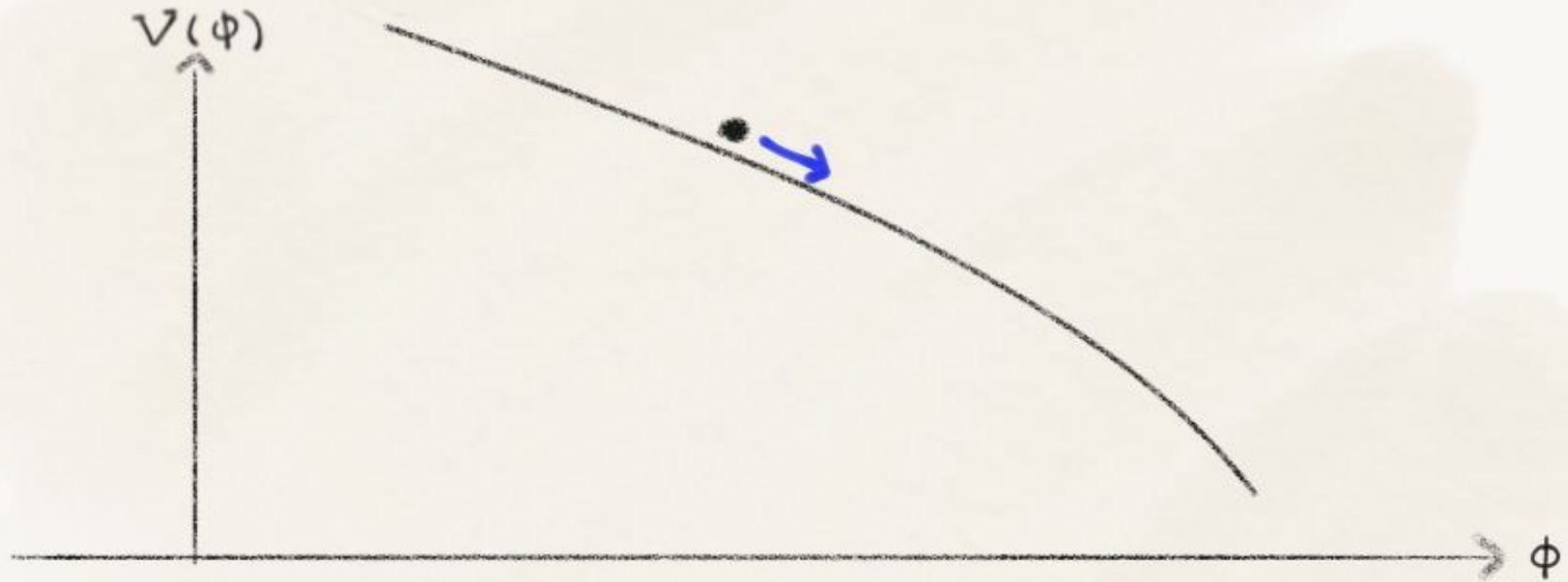
Single-Field Inflation and the Swampland



Eternal Inflation

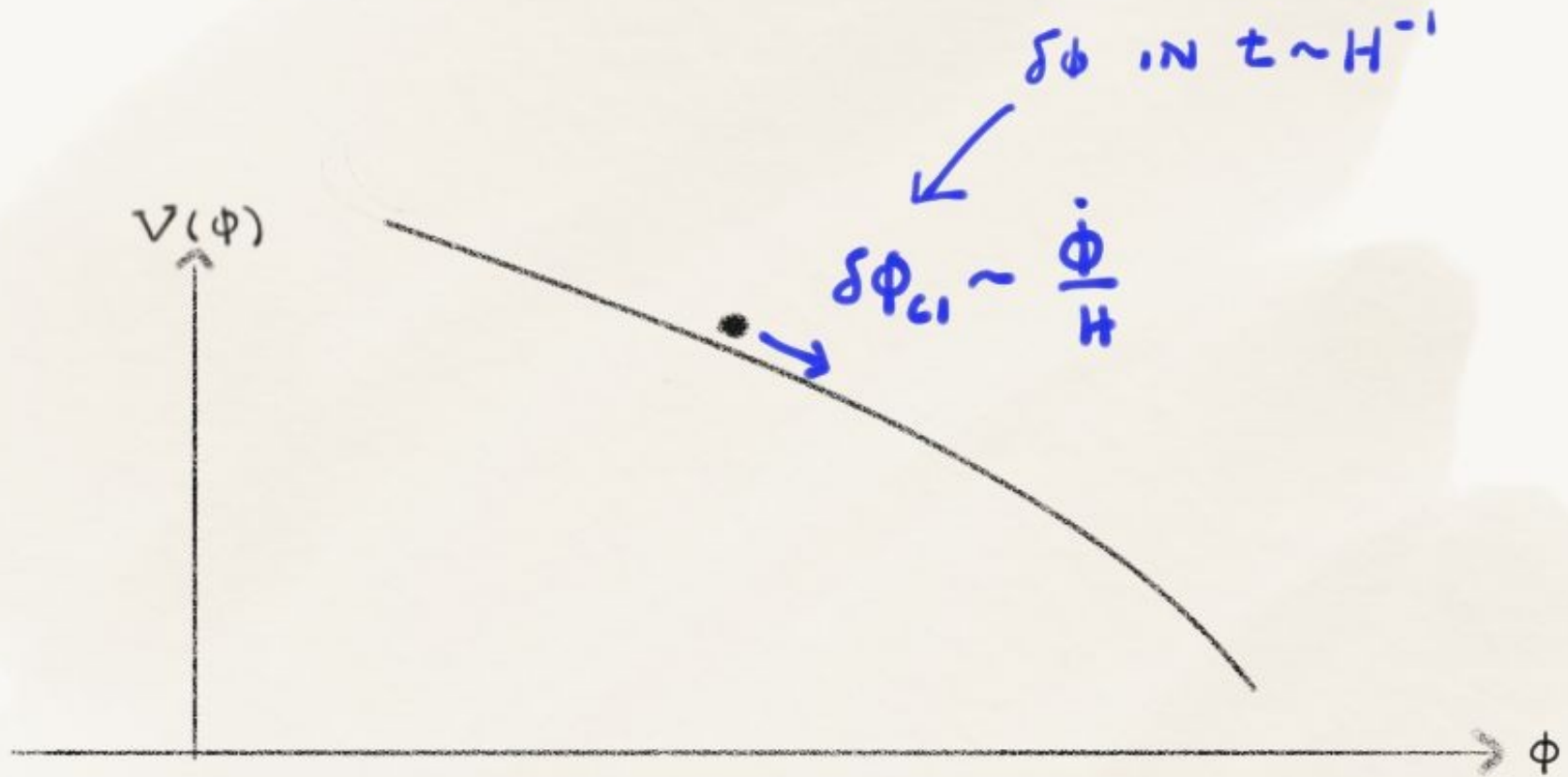


Eternal Inflation

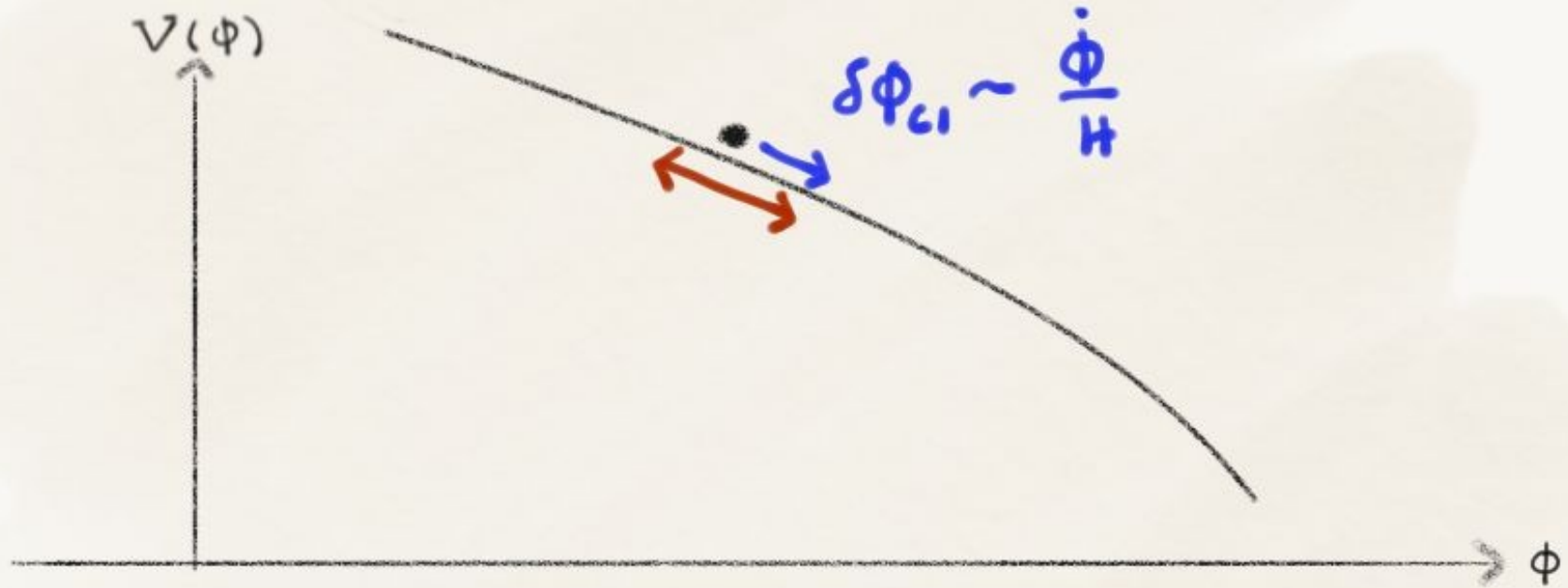


$$\ddot{\phi} + 3H\dot{\phi} + \underbrace{\frac{\delta V}{\delta \phi}}_{\text{CLASSICAL EVOLUTION}} = 0$$

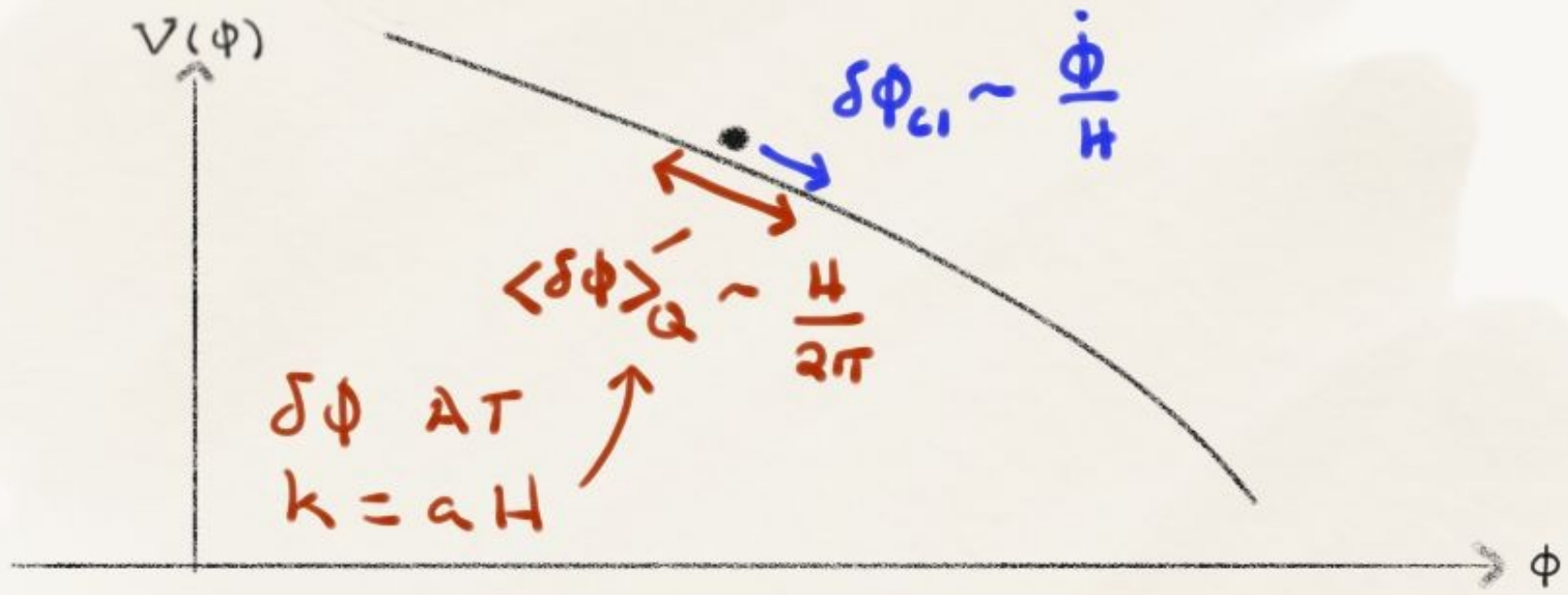
Eternal Inflation



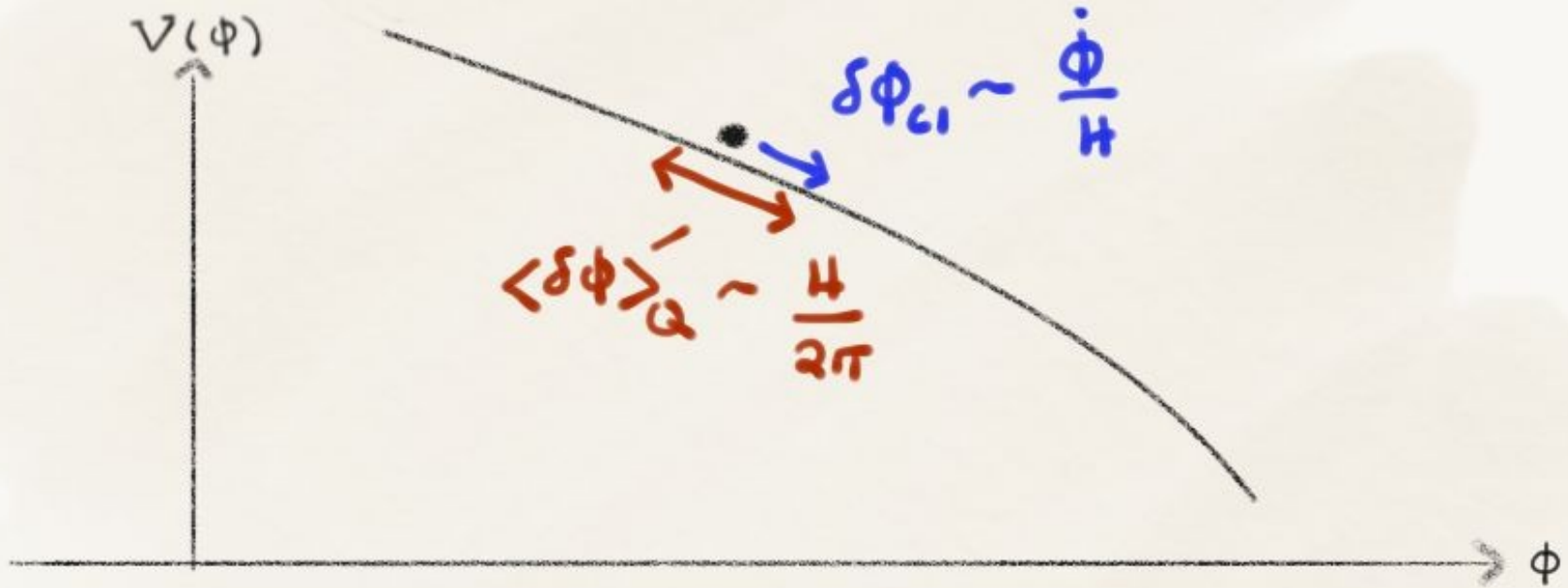
Eternal Inflation



Eternal Inflation

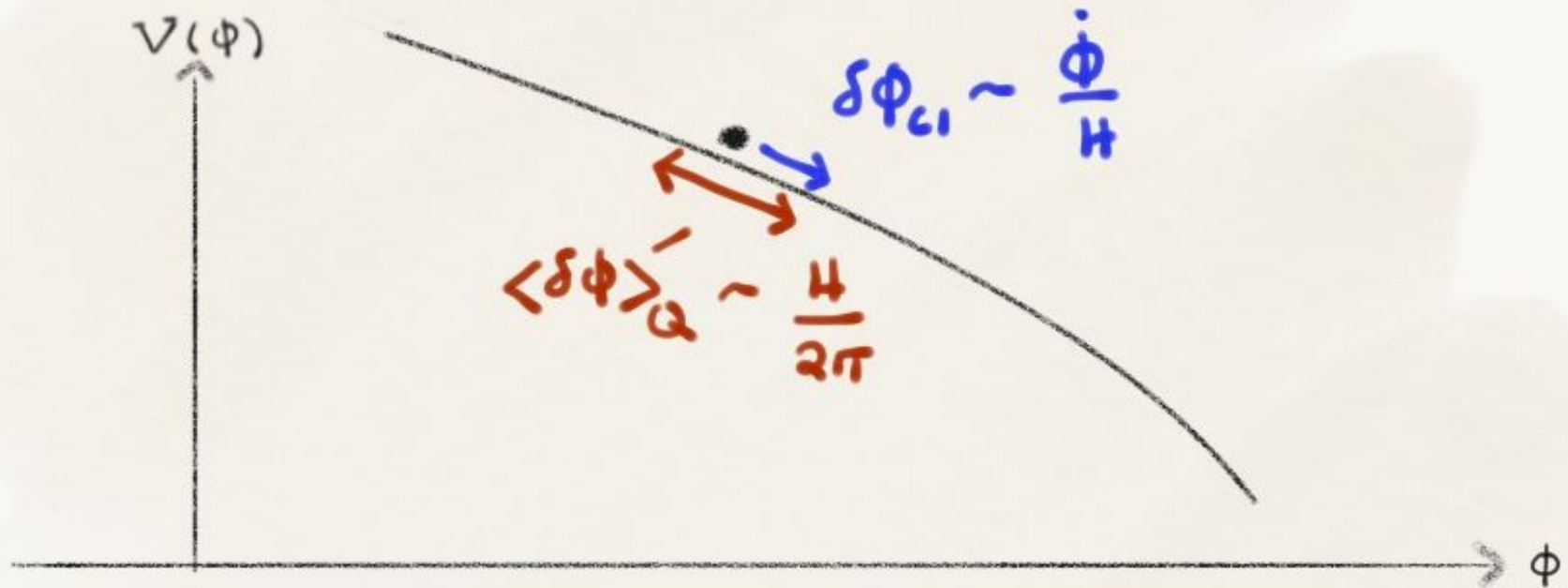


Eternal Inflation



$$\frac{\langle\delta\phi\rangle_q}{\delta\phi_{cl}} = \frac{H^2}{2\pi\dot{\phi}} = P(k) > 1$$

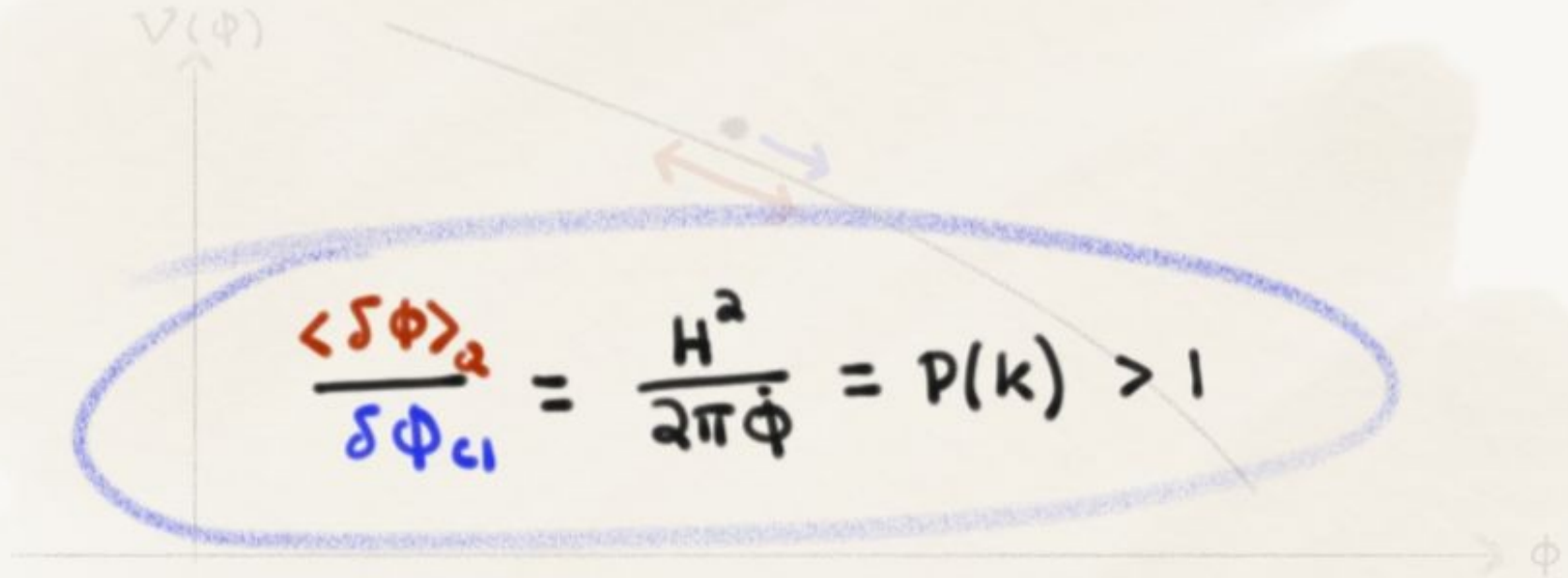
Eternal Inflation



$$\frac{\langle \delta\phi \rangle_a}{\delta\phi_{cl}} = \frac{H^2}{2\pi\dot{\phi}} = P(k) > 1$$

↑ CURVATURE
PERTURBATION!

Condition for Eternal Inflation

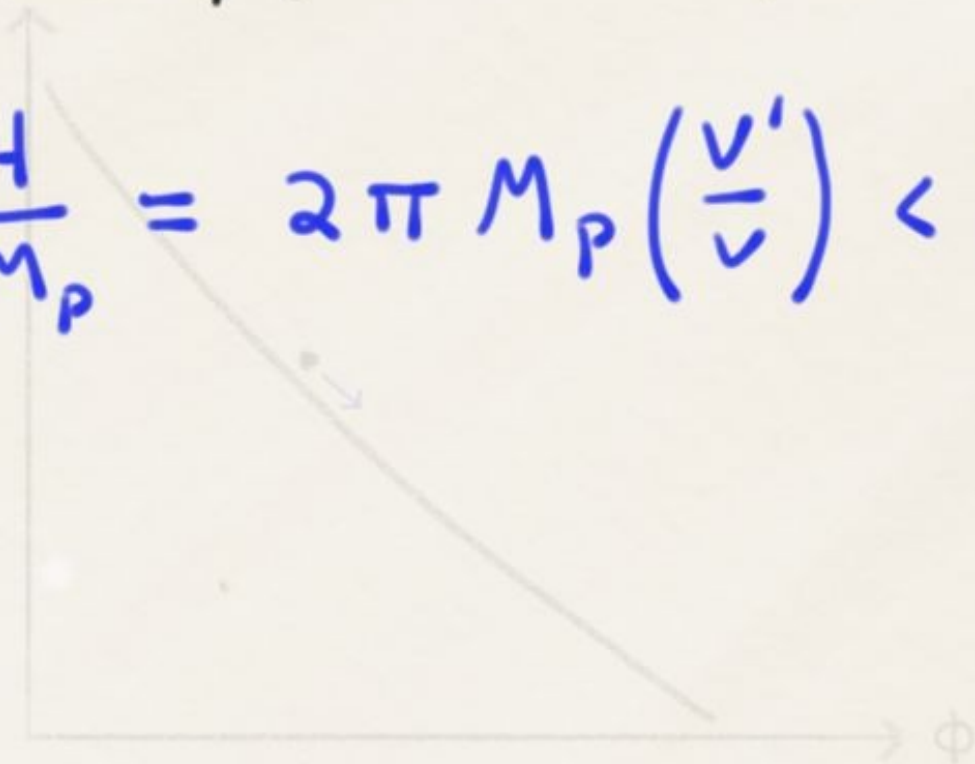


$$P(k) = \frac{H^2}{8\pi^2 M_p^2 \epsilon} = 1 \quad \Rightarrow \quad \frac{H}{M_p} = 2\pi\sqrt{2\epsilon}$$

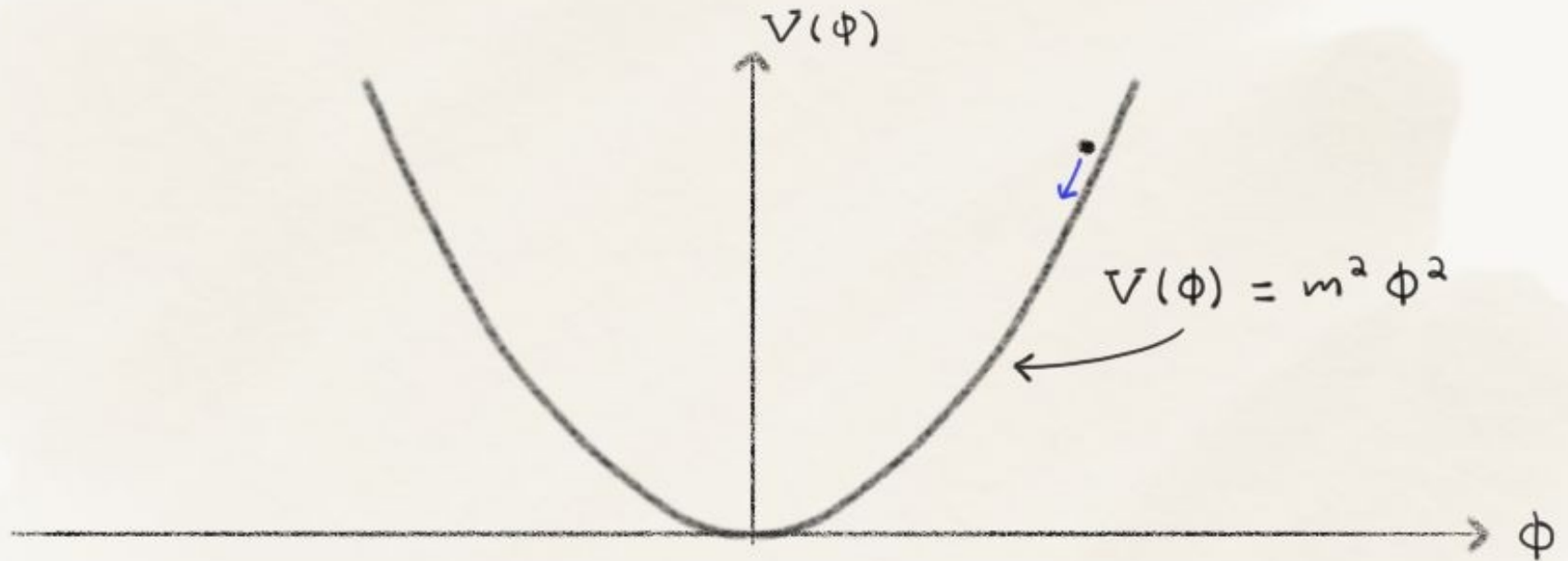


Eternal Inflation and the Swampland

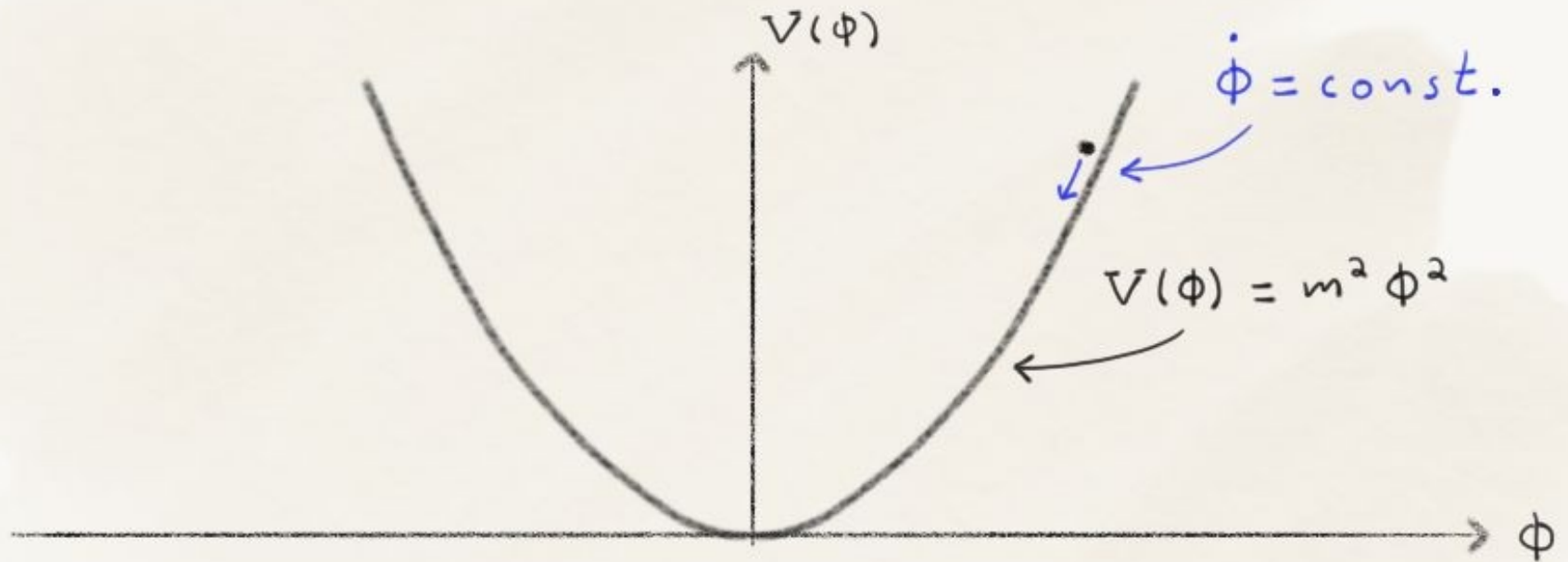
$$P(k) = \frac{H^2}{8\pi^2 M_p^2 \epsilon} = 1 \quad \Rightarrow \quad \frac{H}{M_p} = 2\pi \sqrt{2\epsilon}$$

$$\frac{H}{M_p} = 2\pi M_p \left(\frac{V'}{V} \right) < 1$$


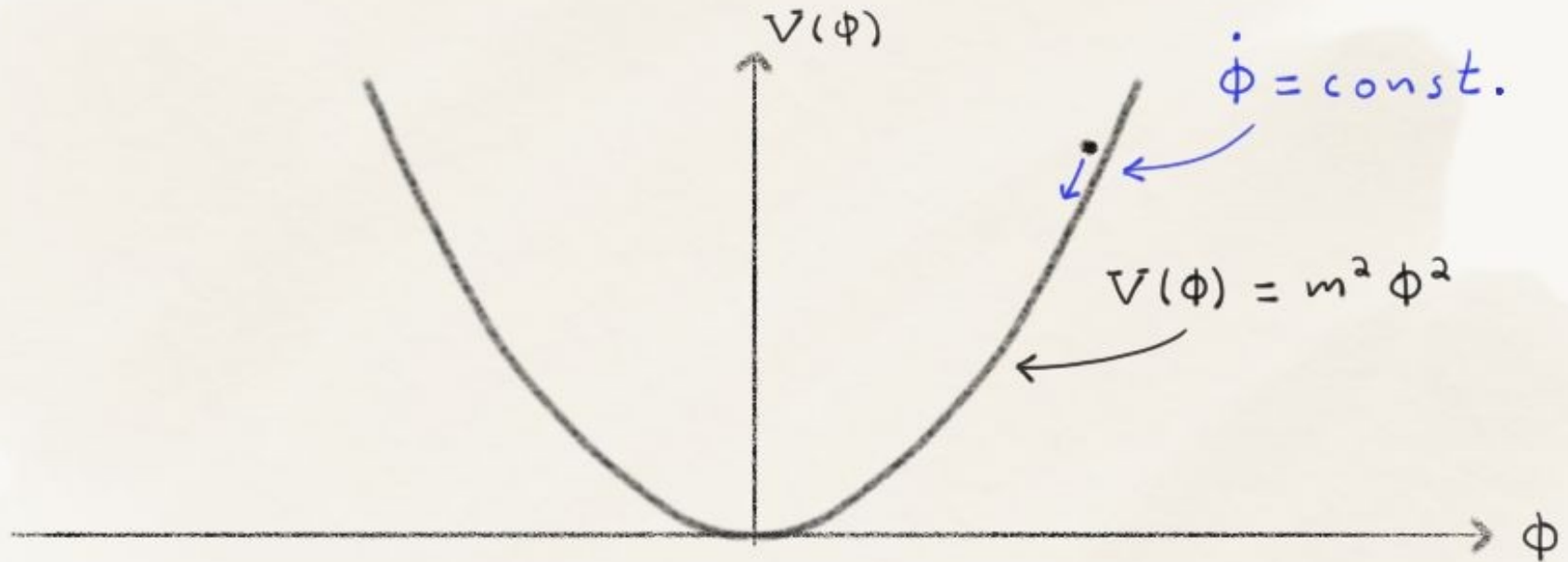
Chaotic Inflation



Chaotic Inflation

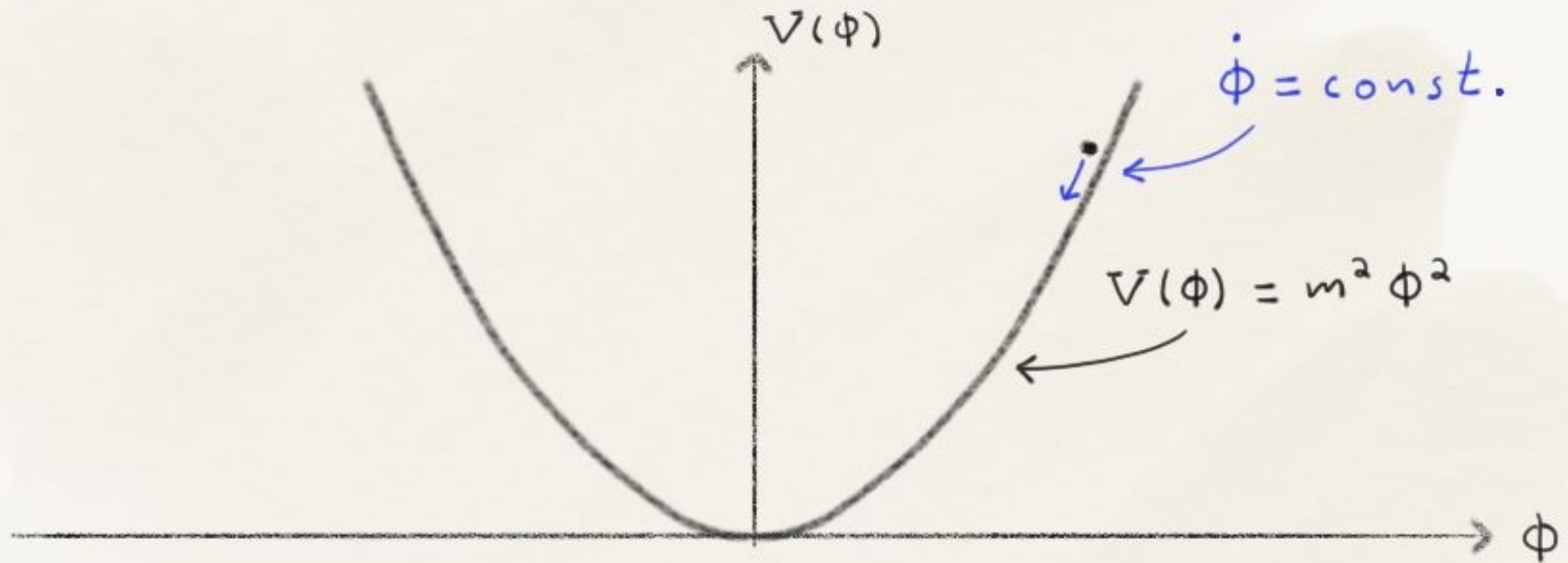


Chaotic Inflation



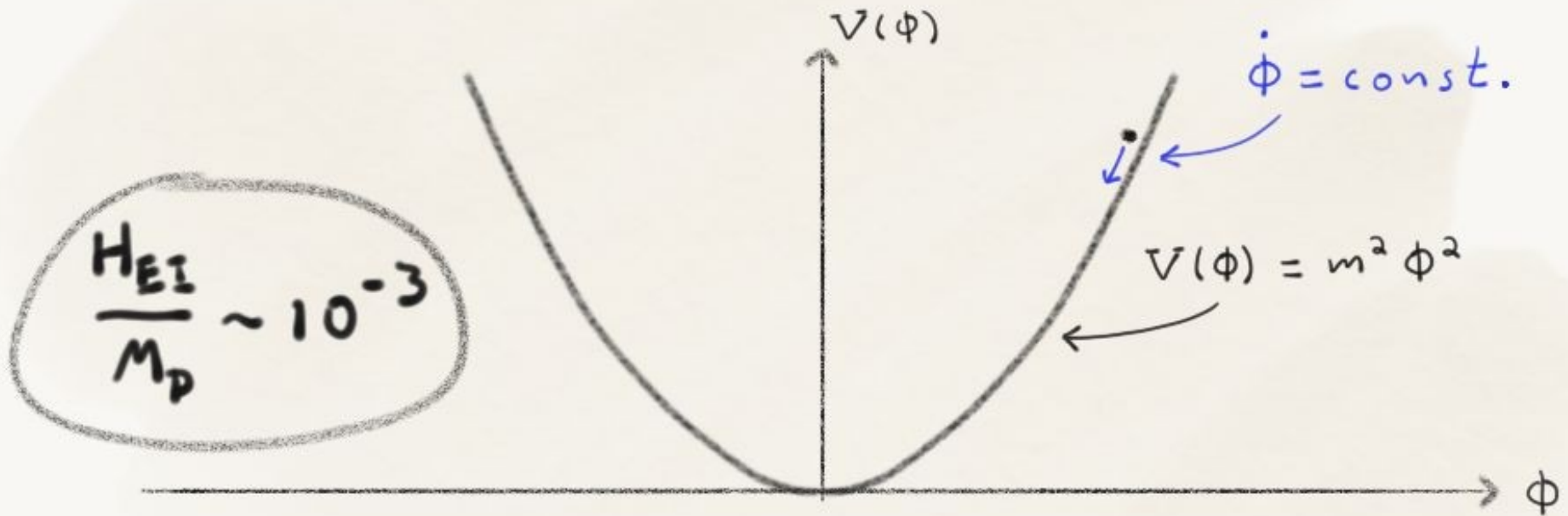
$$P(k) = \frac{H^4}{4\pi^2 \dot{\phi}^2}$$

Chaotic Inflation



$$P(k) = \frac{H^4}{4\pi^2 \dot{\phi}^2} \Rightarrow \frac{H_{\text{EI}}}{H_*} = \frac{1}{[P(k_*)]^{1/4}} \sim 10^2$$

Chaotic Inflation



$$P(k) = \frac{H^4}{4\pi^2 \dot{\phi}^2} \Rightarrow \frac{H_{EI}}{H_*} = \frac{1}{[P(k_*)]^{1/4}} \sim 10^2$$

Eternal Inflation and the Swampland

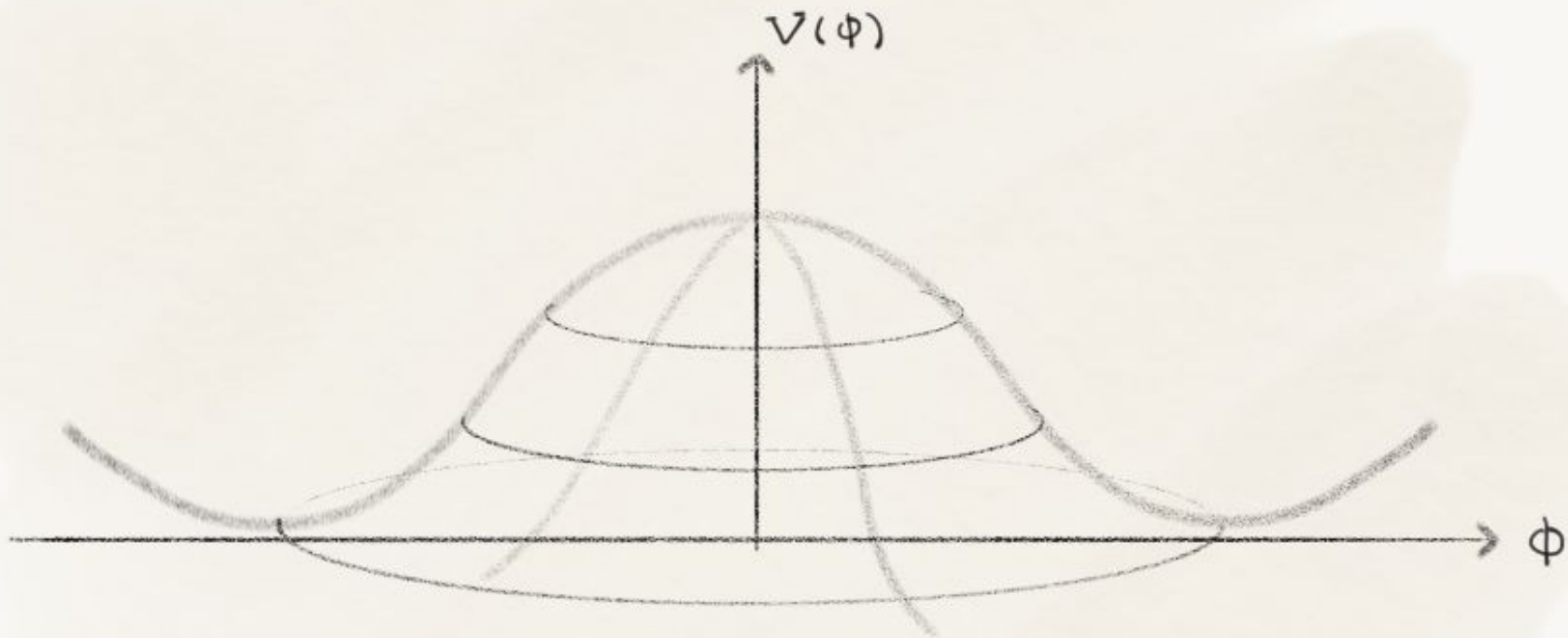
$$P(k) = \frac{H^2}{8\pi^2 M_P^2 \epsilon} = 1 \quad \Rightarrow \quad \frac{H}{M_P} = 2\pi\sqrt{2\epsilon}$$

$$\frac{H}{M_P} = 2\pi M_P \left(\frac{V'}{V} \right) < 1$$

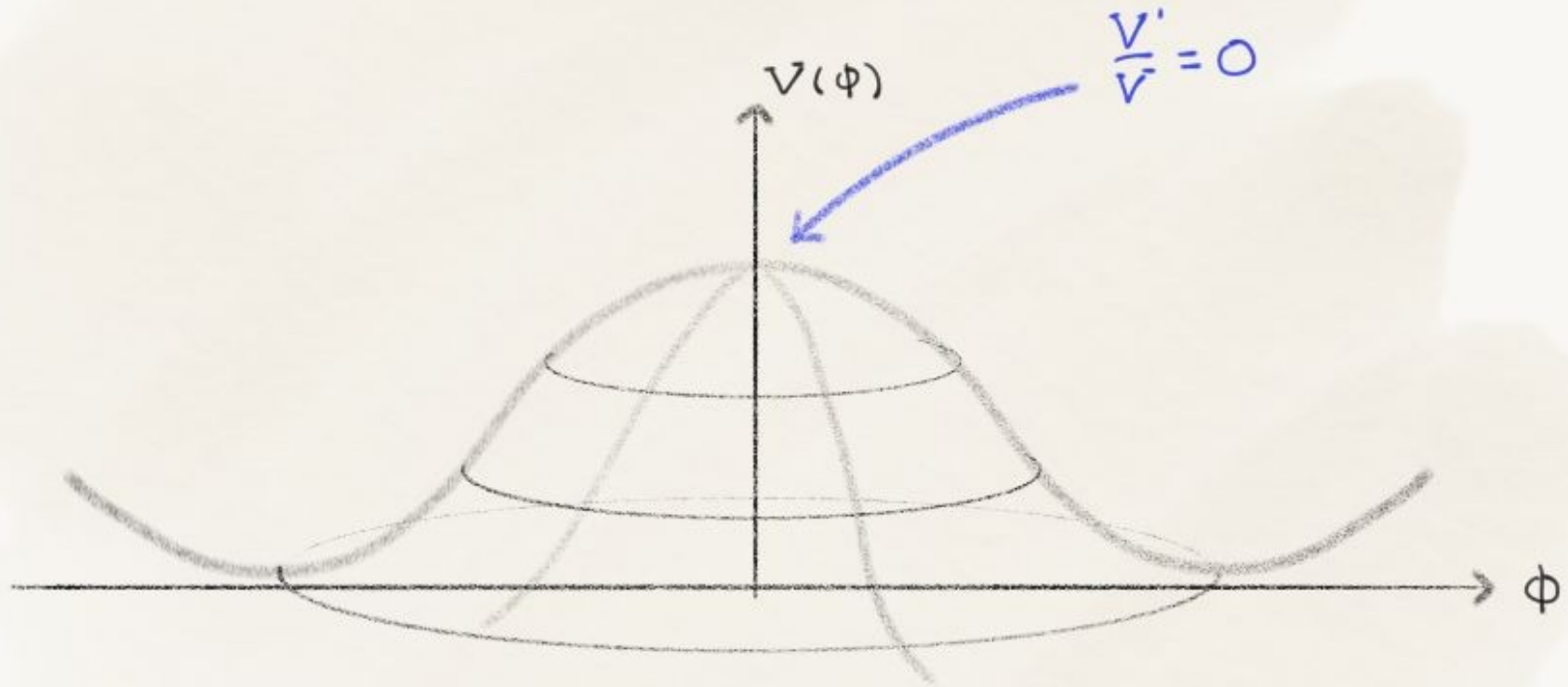
$$\rightarrow M_P \left(\frac{V'}{V} \right) > c \sim \mathcal{O}(1)$$

SWAMPLAND ϕ

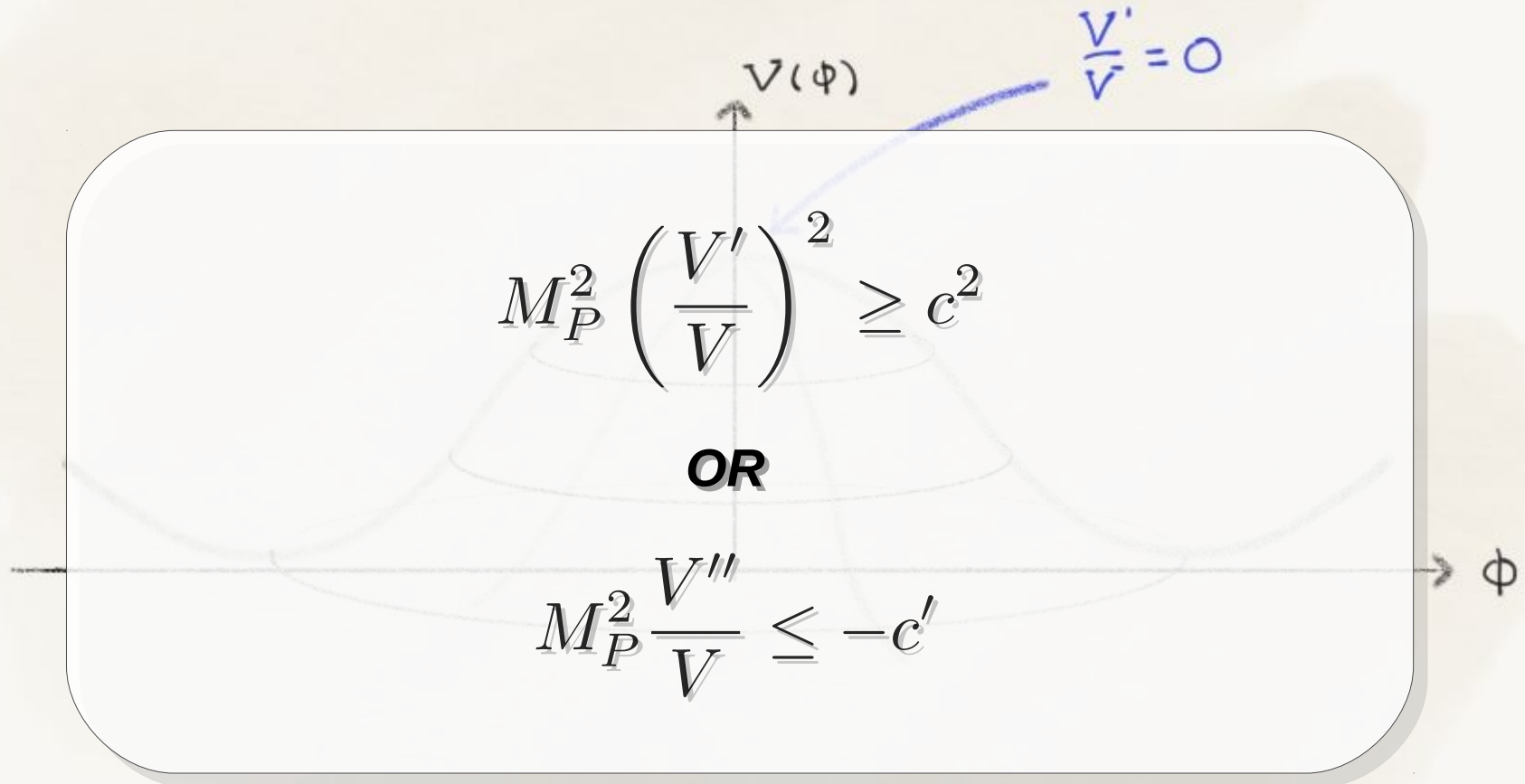
What about symmetry breaking?



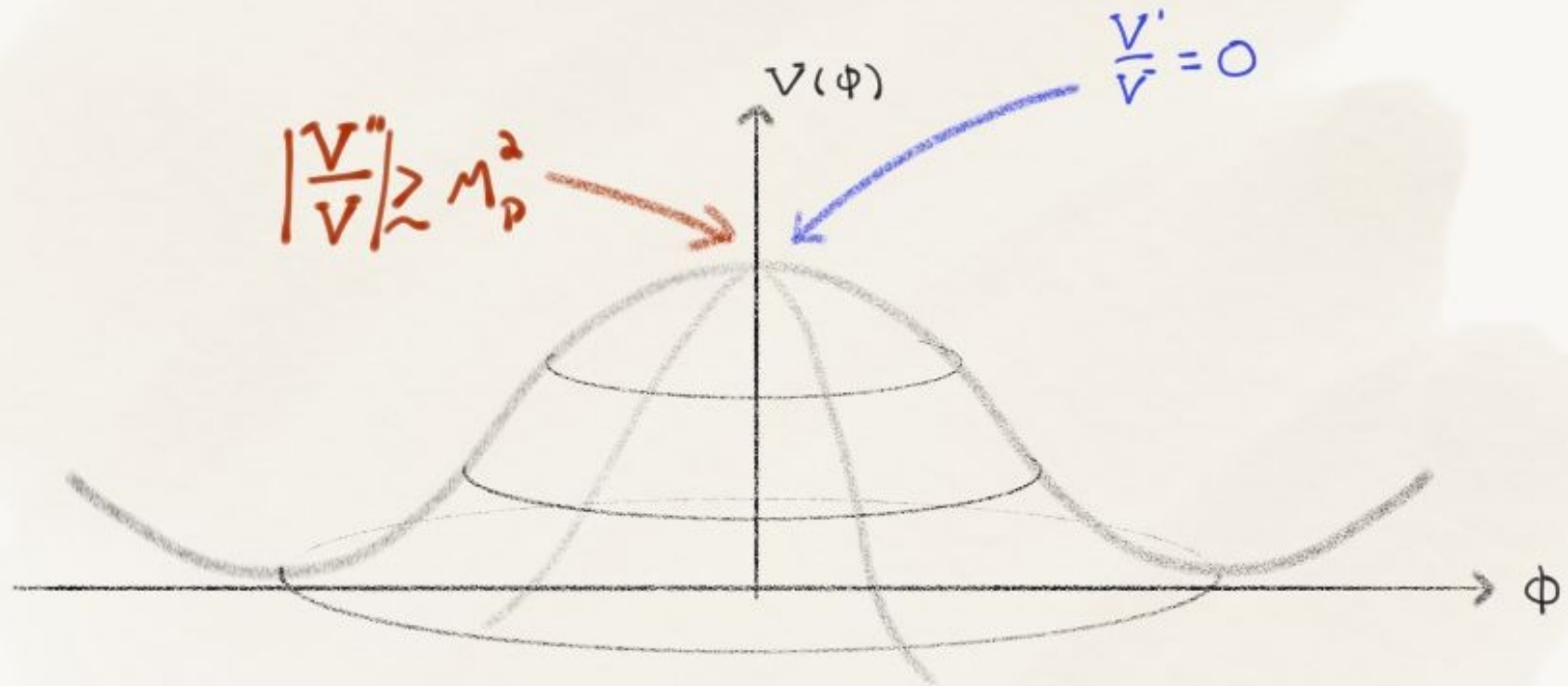
What about symmetry breaking?



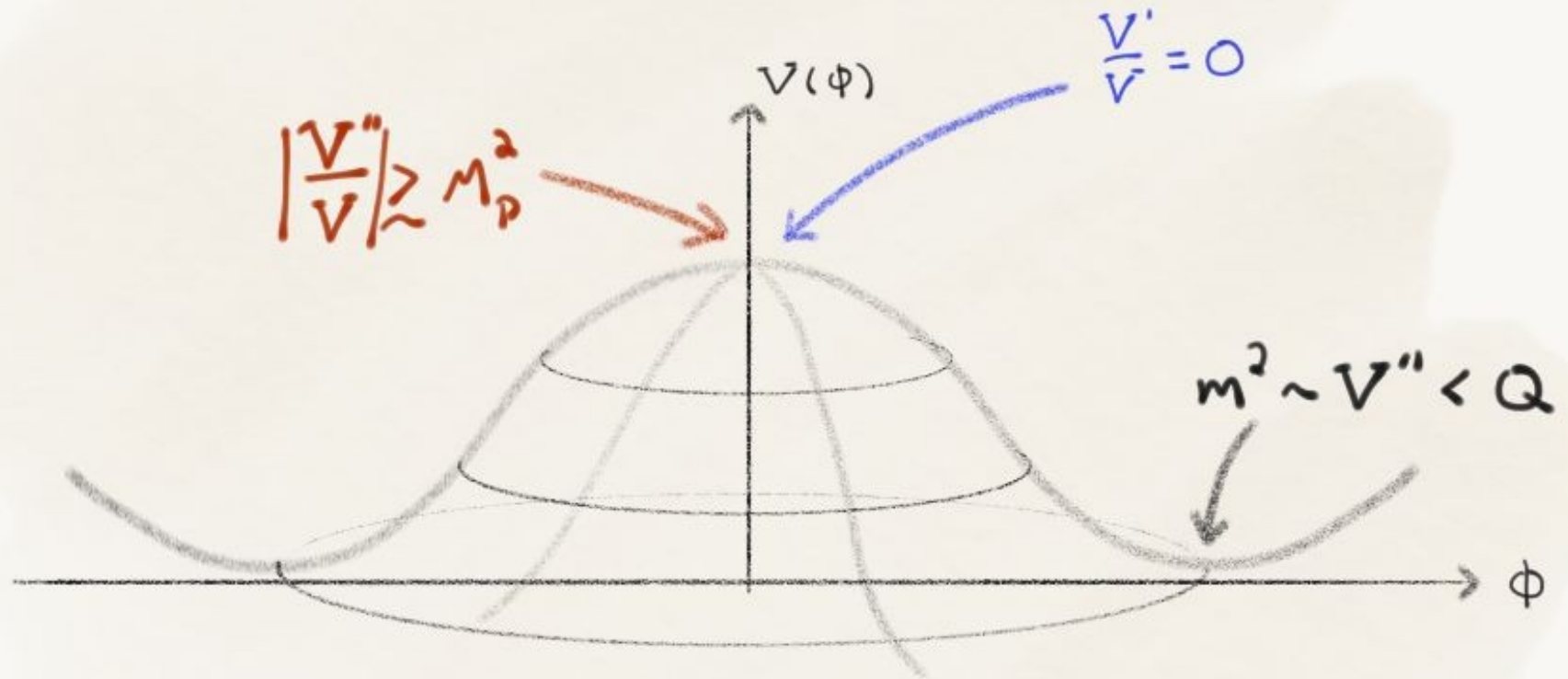
The Refined Swampland Conjecture



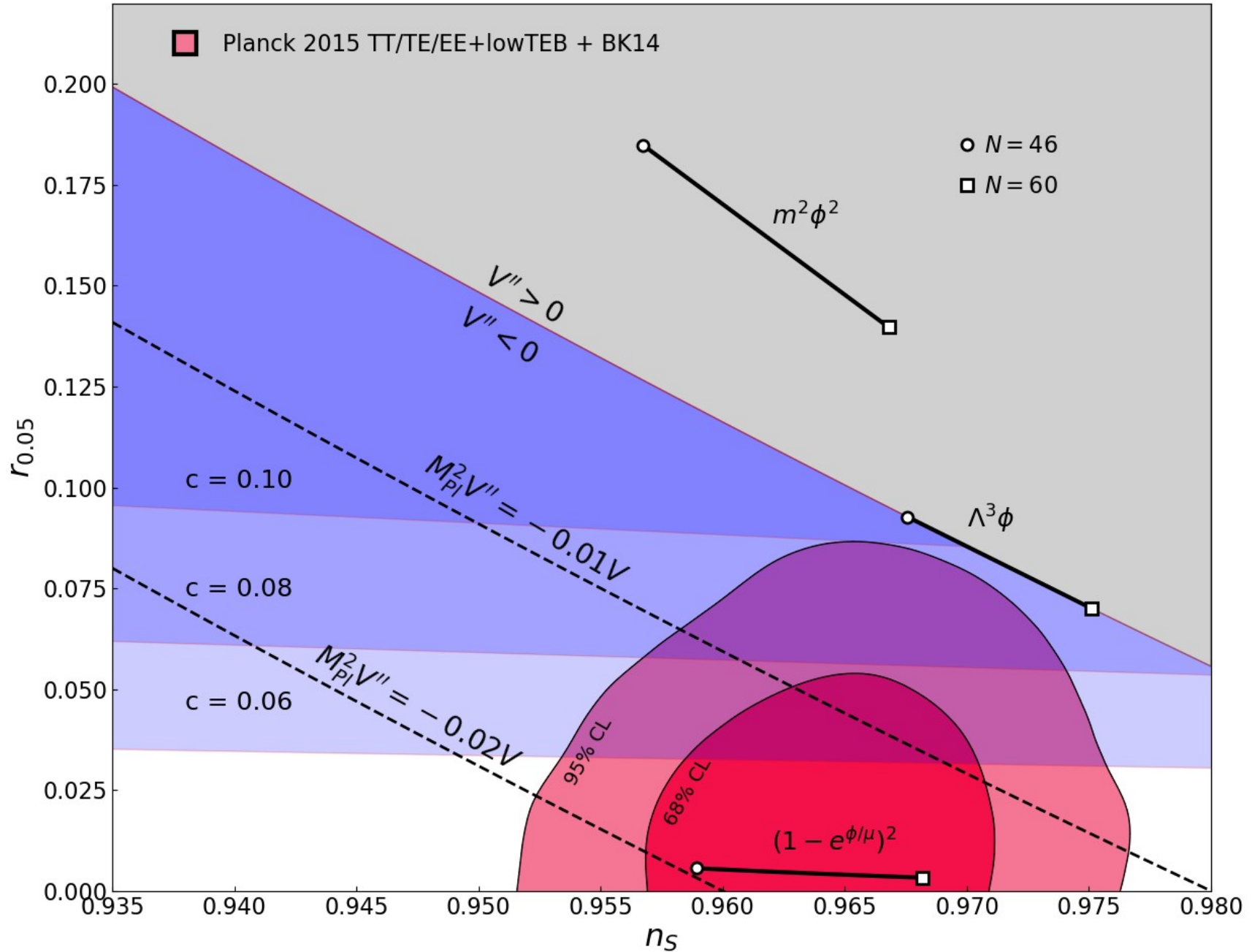
The *Refined* Swampland Conjecture



The *Refined* Swampland Conjecture



Single-Field Inflation and the Swampland



Eternal Inflation and the Swampland

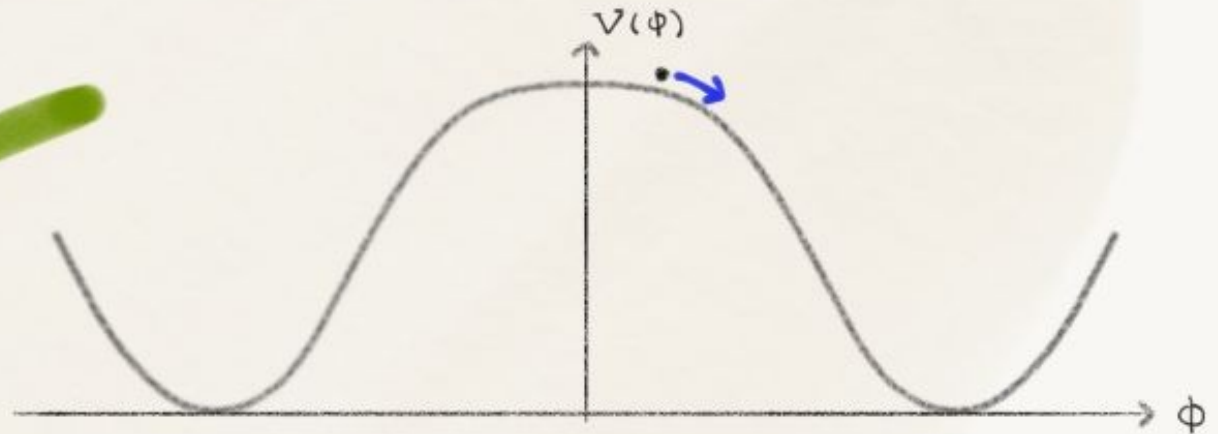
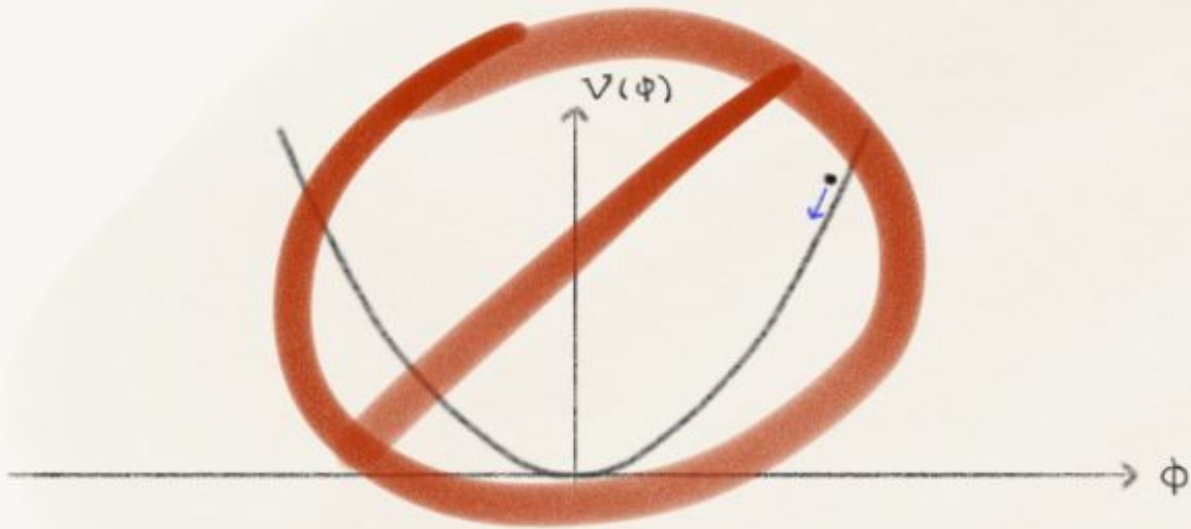
$$P(k) = \frac{H^2}{8\pi^2 M_p^2 \epsilon} = 1 \quad \Rightarrow \quad \frac{H}{M_p} = 2\pi\sqrt{2\epsilon}$$

$$\frac{H}{M_p} = 2\pi M_p \left(\frac{V'}{V} \right) < 1$$

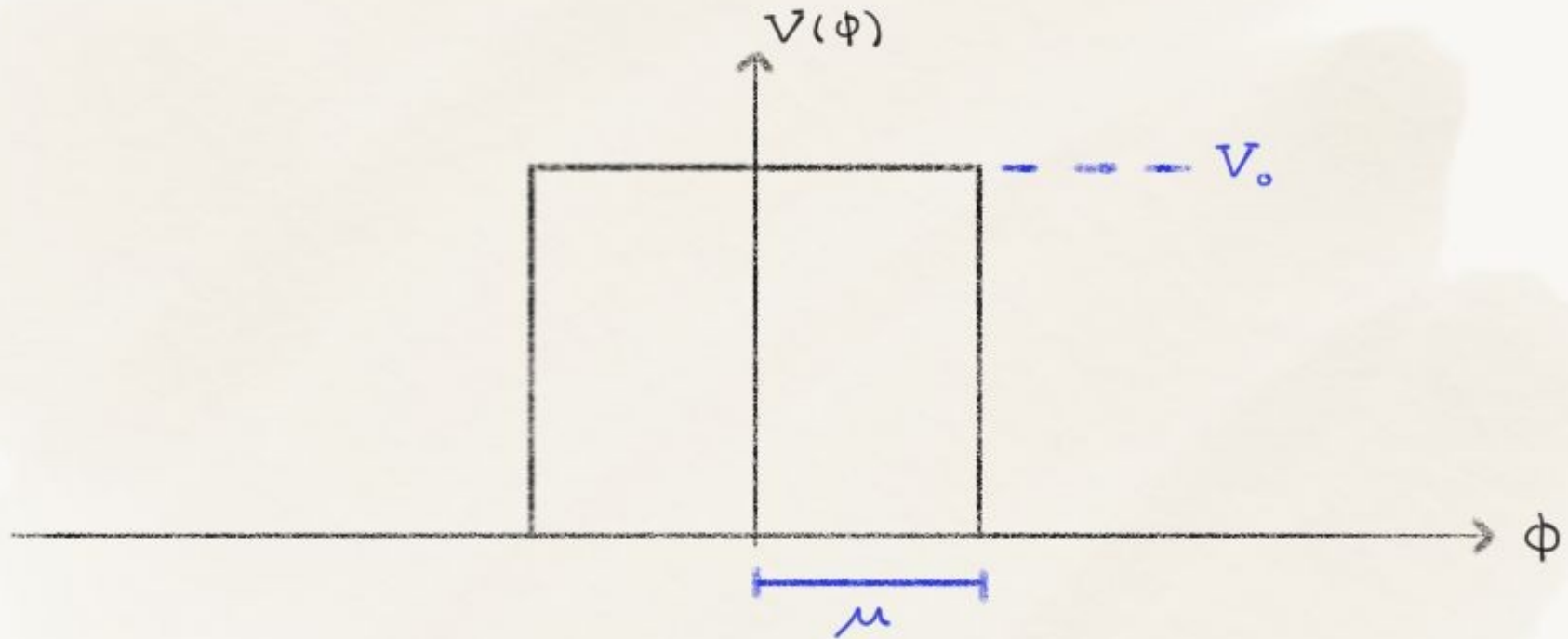
$$\rightarrow M_p \left(\frac{V'}{V} \right) > c \sim \mathcal{O}(1)$$

SWAMPLAND ϕ

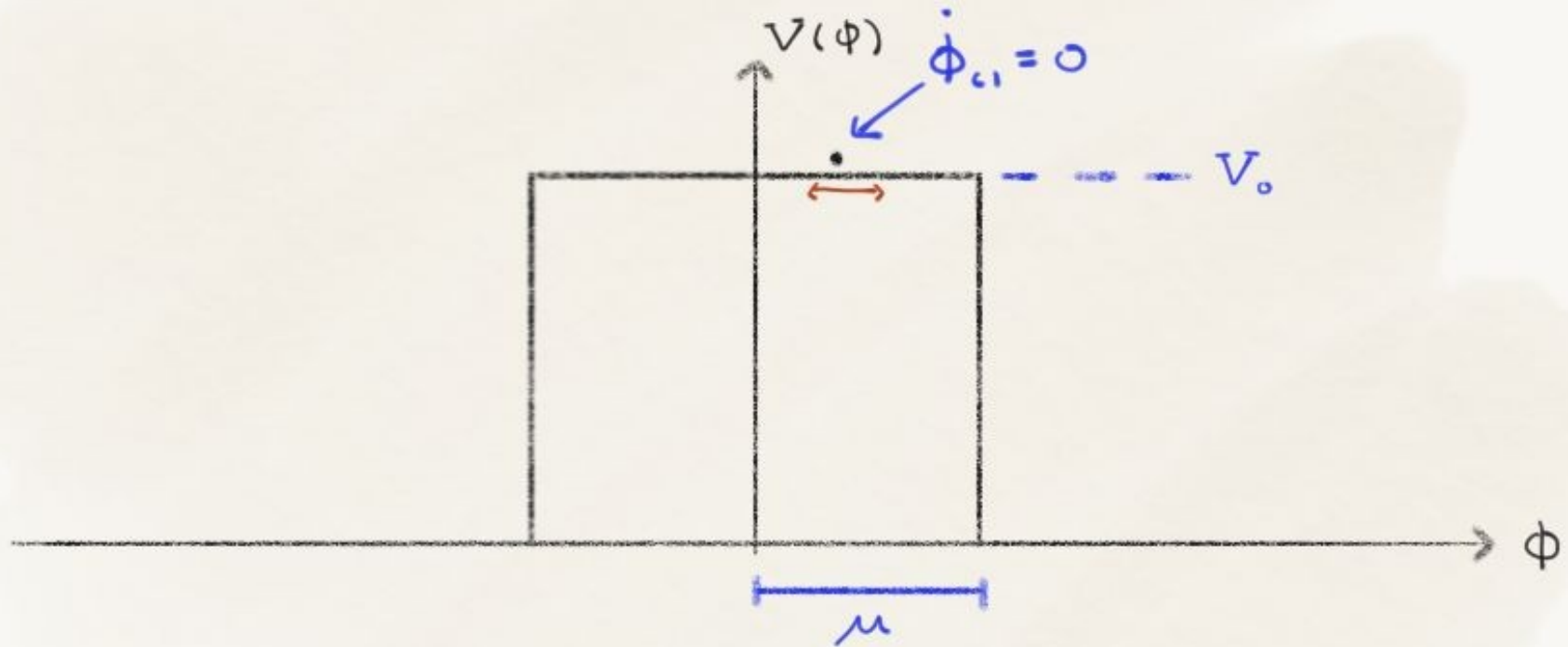
Convex or Concave?



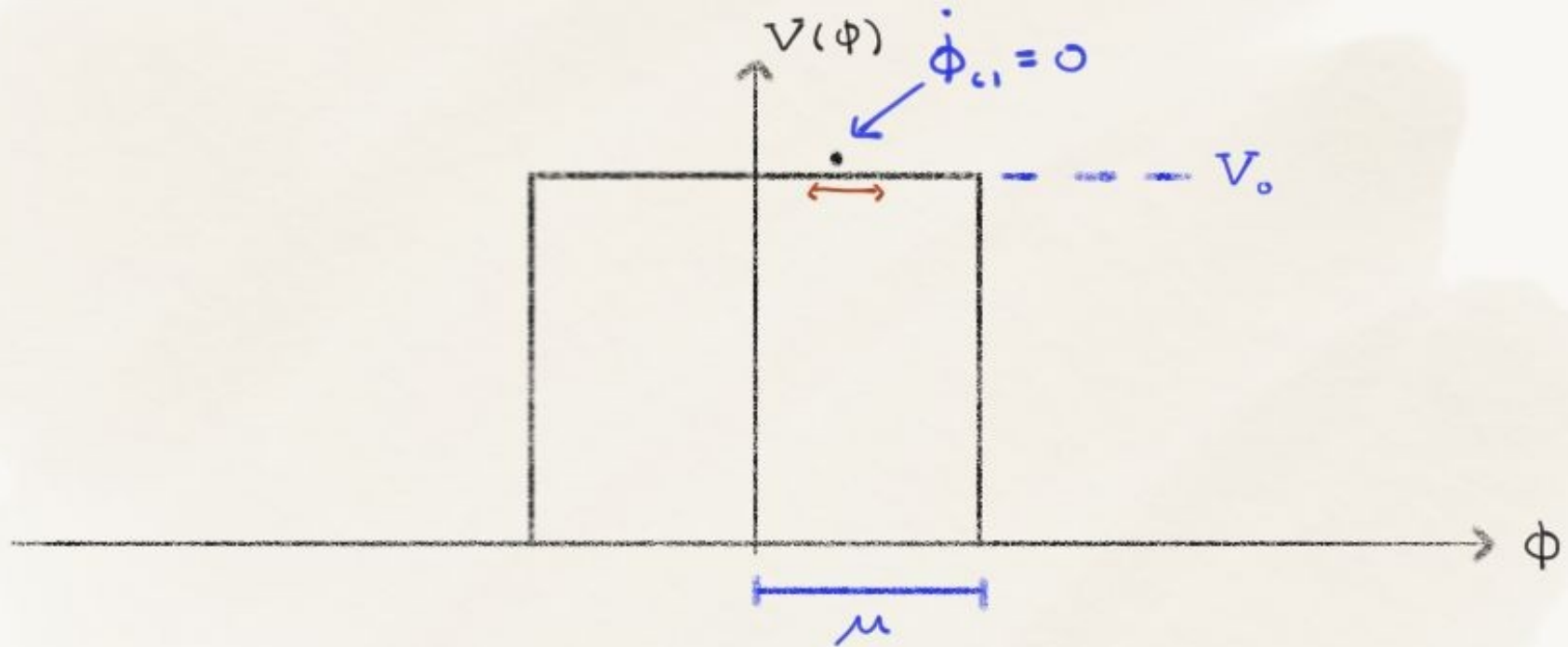
Top-Hat Potentials



Top-Hat Potentials



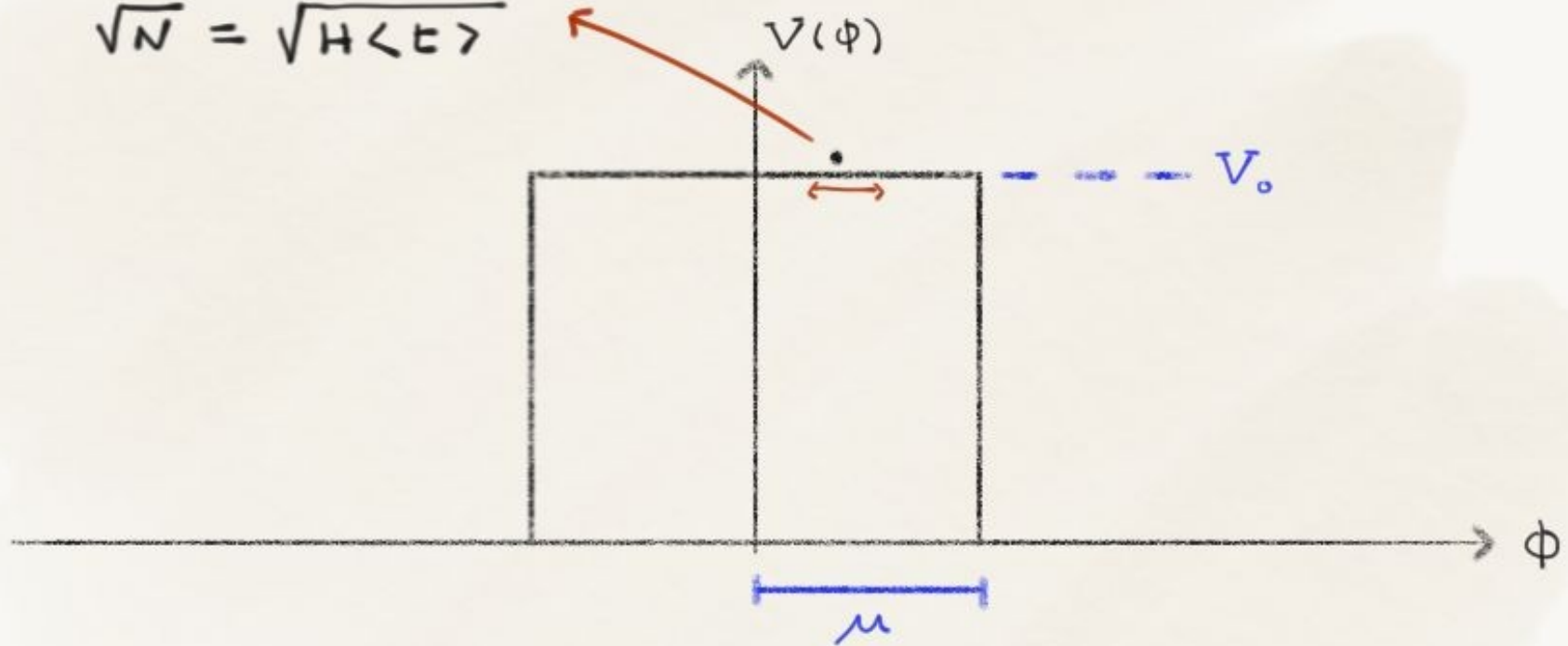
Top-Hat Potentials



$$P(k) = \frac{H^2}{2\pi \dot{\phi}} \rightarrow \infty$$

Top-Hat Potentials

Random Walk
 $\sqrt{N} = \sqrt{H \langle \epsilon \rangle}$

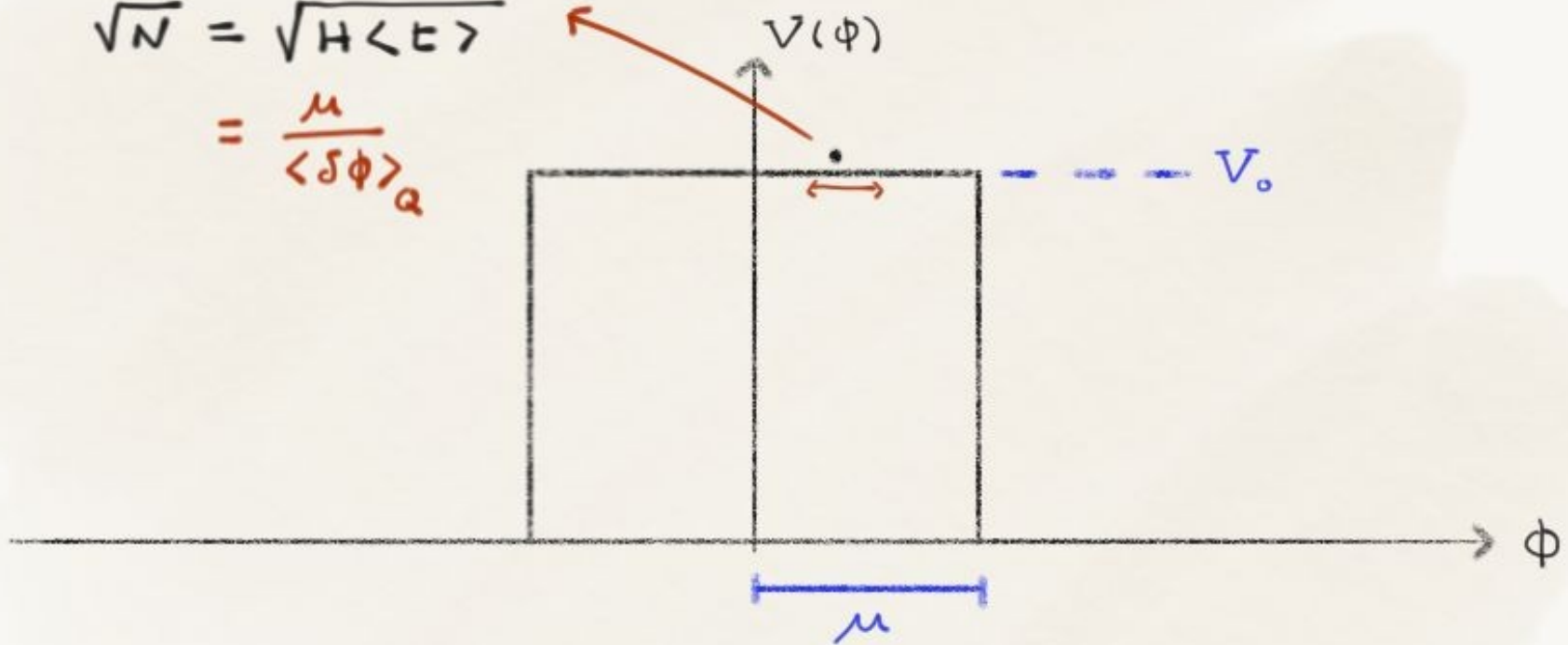


Top-Hat Potentials

Random Walk

$$\sqrt{N} = \sqrt{H \langle t \rangle}$$

$$= \frac{\mu}{\langle \delta\phi \rangle_q}$$



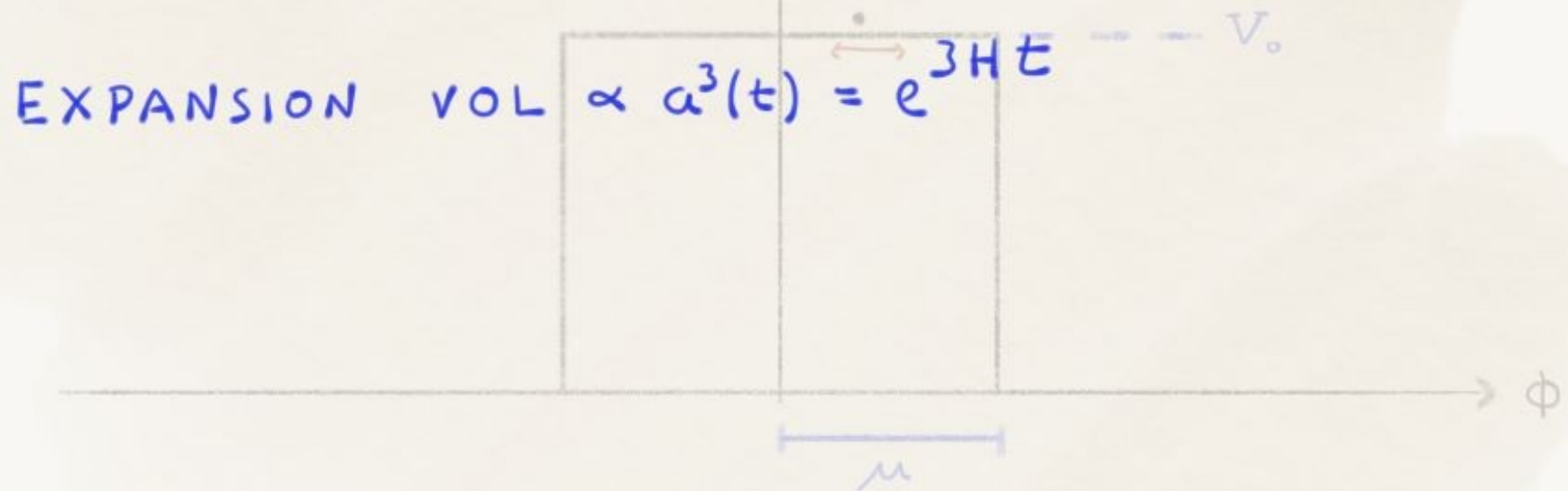
$$\Gamma_I \propto e^{-t/\langle t \rangle} = \exp\left[-\left(\frac{\langle \delta\phi \rangle_q}{\mu}\right)^2 H t\right]$$



PROBABILITY THAT INFLATION ENDS
IN TIME t

Top-Hat Potentials

$$\Gamma_I \propto e^{-t/\langle t \rangle} = \exp \left[- \left(\frac{\langle \delta \phi \rangle_a}{\mu} \right)^2 H t \right]$$



Top-Hat Potentials

$$\Gamma_I \propto e^{-t/\langle t \rangle} = \exp \left[- \left(\frac{\langle \delta \Phi \rangle_a}{\mu} \right)^2 H t \right]$$

EXPANSION VOL $\propto a^3(t) = e^{3Ht}$ $\dots V_0$

$$\Gamma(t) \propto \exp \left\{ \left[3 - \left(\frac{\langle \delta \Phi \rangle_a}{\mu} \right)^2 \right] H t \right\}$$



FRACTION OF HUBBLE PATCHES
IN DE SITTER PHASE

Top-Hat Potentials

$$\Gamma_{\text{I}} \propto e^{-t/\langle t \rangle} = e^{-\int_0^t \left[3 - \left(\frac{\langle \delta\phi \rangle_Q}{\mu} \right)^2 \right] H dt}$$

EXPANSION VOL $\propto a^3(t) = e^{3Ht} \dots V_0$

$$\Gamma(t) \propto \exp \left\{ \left[3 - \left(\frac{\langle \delta\phi \rangle_Q}{\mu} \right)^2 \right] H t \right\}$$

ETERNAL INFLATION μ

$$\frac{\mu}{\langle \delta\phi \rangle_Q} = \frac{2\pi\mu}{H} > \frac{1}{\sqrt{3}}$$

Top-Hat Potentials

$$\Gamma_I \propto e^{-t/\langle t \rangle} = e^{-\int_0^t \left[3 - \left(\frac{\langle \delta\phi \rangle_Q}{\mu} \right)^2 \right] H dt}$$

EXPANSION VOL $\propto a^3(t) = e^{3Ht} \dots V_0$

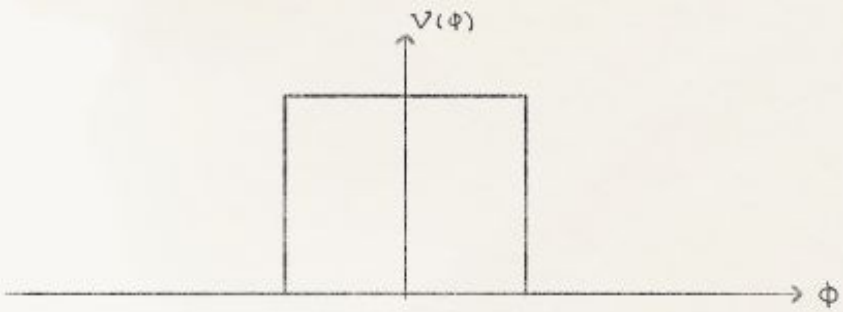
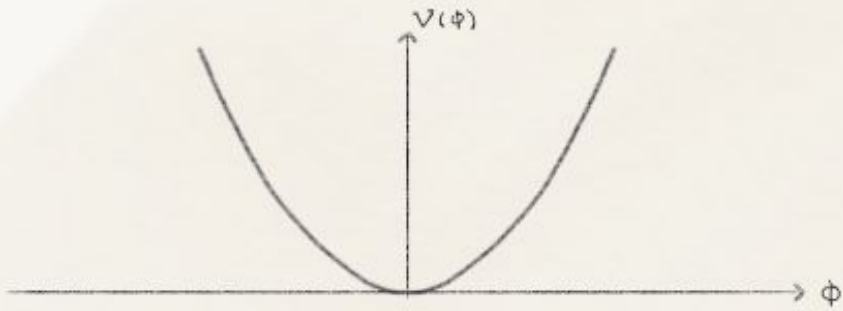
$$\Gamma(t) \propto \exp \left\{ \left[3 - \left(\frac{\langle \delta\phi \rangle_Q}{\mu} \right)^2 \right] H t \right\}$$

ETERNAL INFLATION

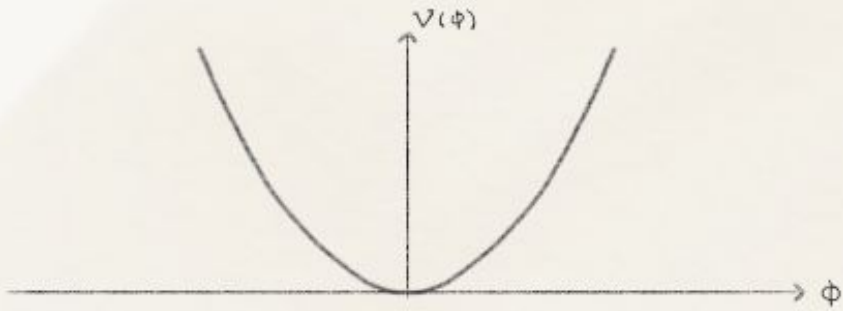
$$\frac{\mu}{\langle \delta\phi \rangle_Q} = \frac{2\pi\mu}{H} > \frac{1}{\sqrt{3}} \Rightarrow$$

$$\mu > \frac{\sqrt{V_0}}{6\pi M_p}$$

Two Qualitatively Different Types

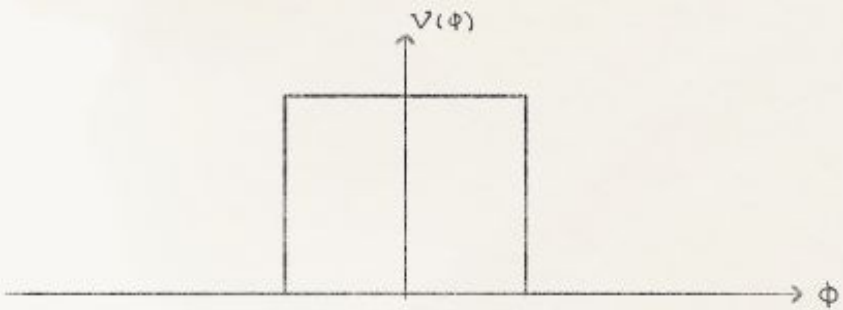


Two Qualitatively Different Types

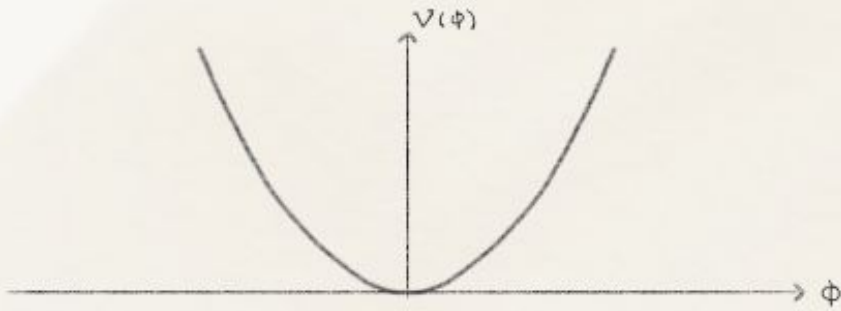


$$\dot{\phi} \sim \text{const.}$$

$$H_{E\Sigma} \gg H_*$$

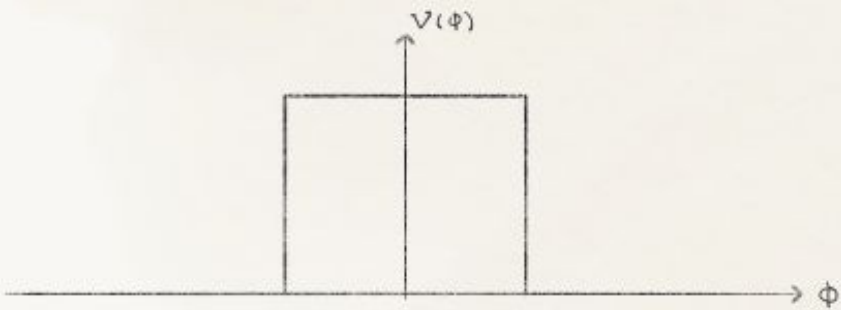


Two Qualitatively Different Types



$$\dot{\phi} \sim \text{const.}$$

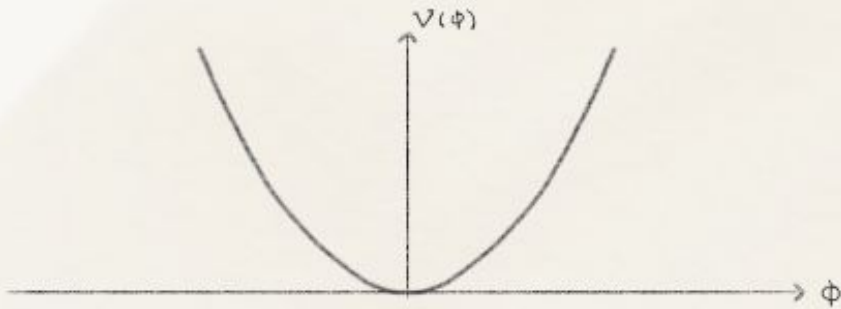
$$H_{E I} \gg H_*$$



$$H \sim \text{const.}$$

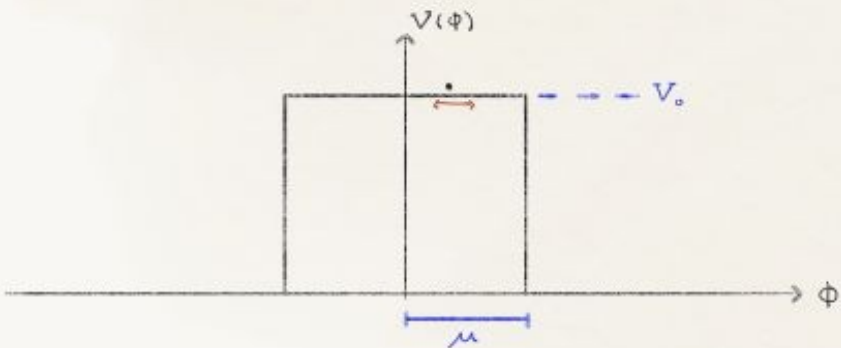
$$\dot{\phi}_{E I} \rightarrow 0$$

Two Qualitatively Different Types



$$\dot{\phi} \sim \text{const.}$$

$$H_{E\Gamma} \gg H_*$$

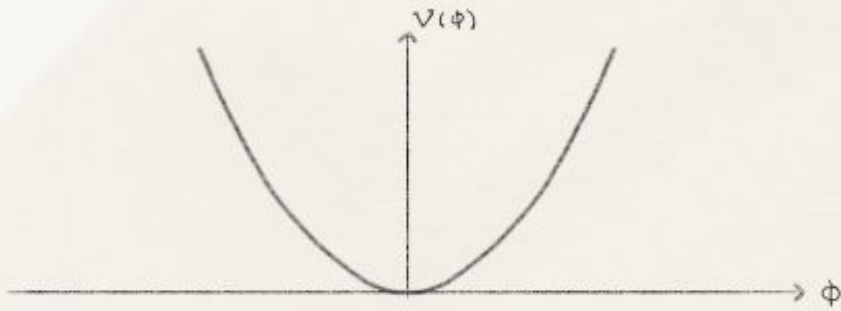


$$H \sim \text{const.}$$

$$\dot{\phi}_{E\Gamma} \rightarrow 0$$

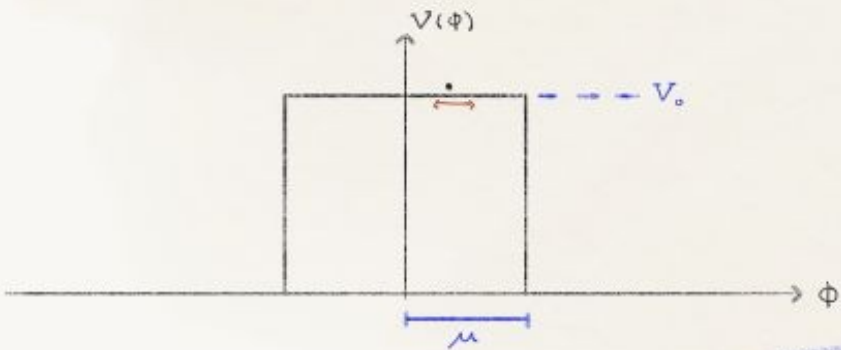
$$V_0 \sim \Lambda^4 \Rightarrow \frac{\mu}{\Lambda} > \frac{\Lambda}{6\pi M_p}$$

Two Qualitatively Different Types



$$\dot{\phi} \sim \text{const.}$$

$$H_{E I} \gg H_*$$



$$H \sim \text{const.}$$

$$\dot{\phi}_{E I} \rightarrow 0$$

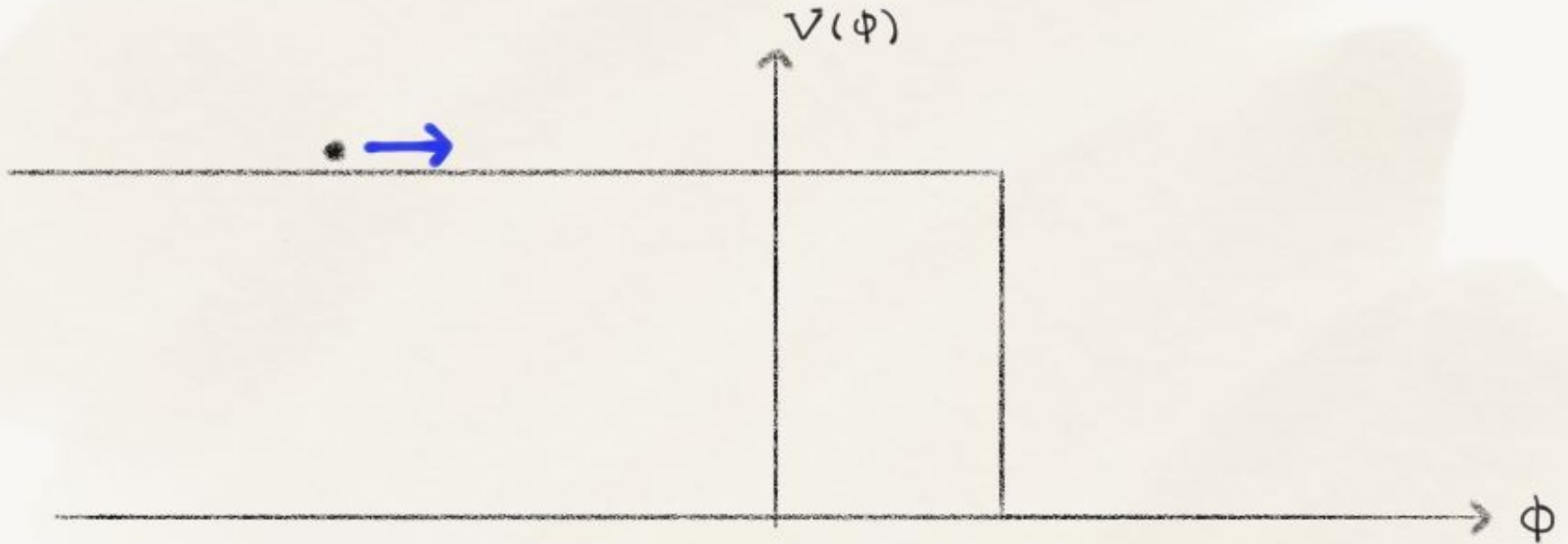
$$V_0 \sim \Lambda^4$$

 \Rightarrow

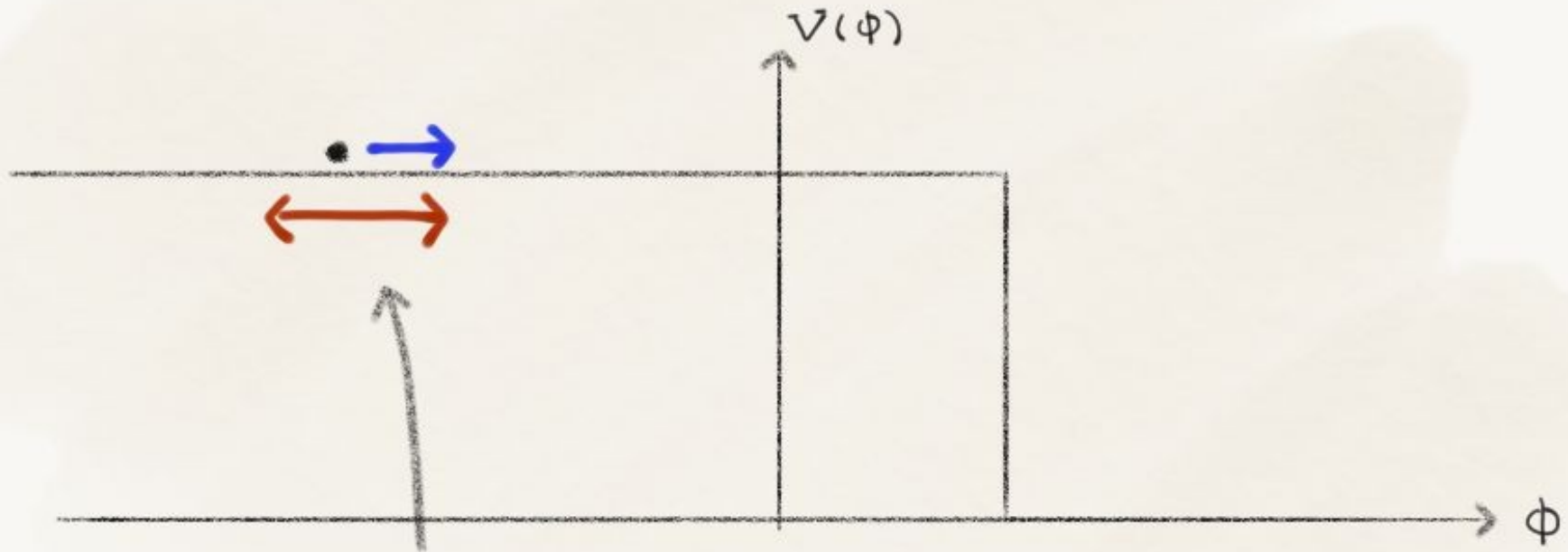
$$\frac{\mu}{\Lambda} > \frac{\Lambda}{6\pi M_p}$$

← NO INHERENT SCALE

Plateau Potentials (e.g. Starobinsky)

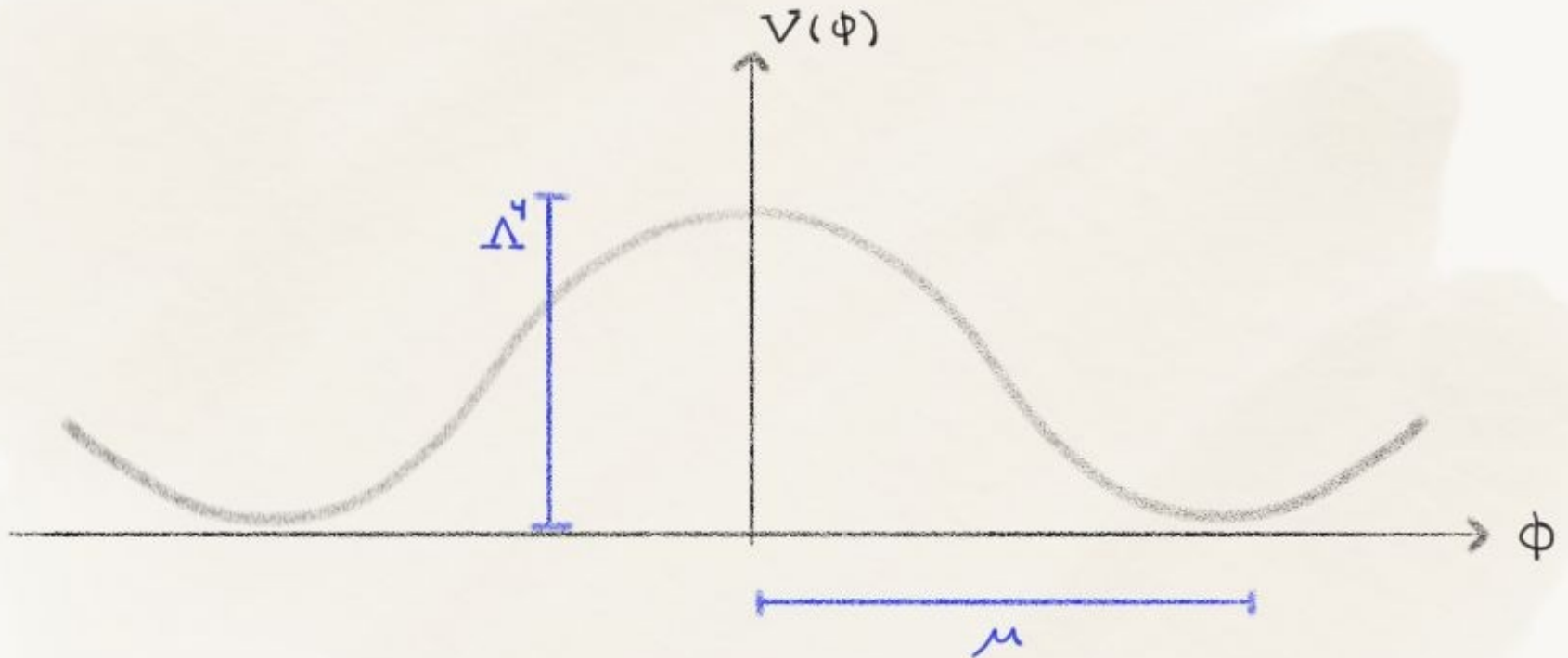


Plateau Potentials (e.g. Starobinsky)

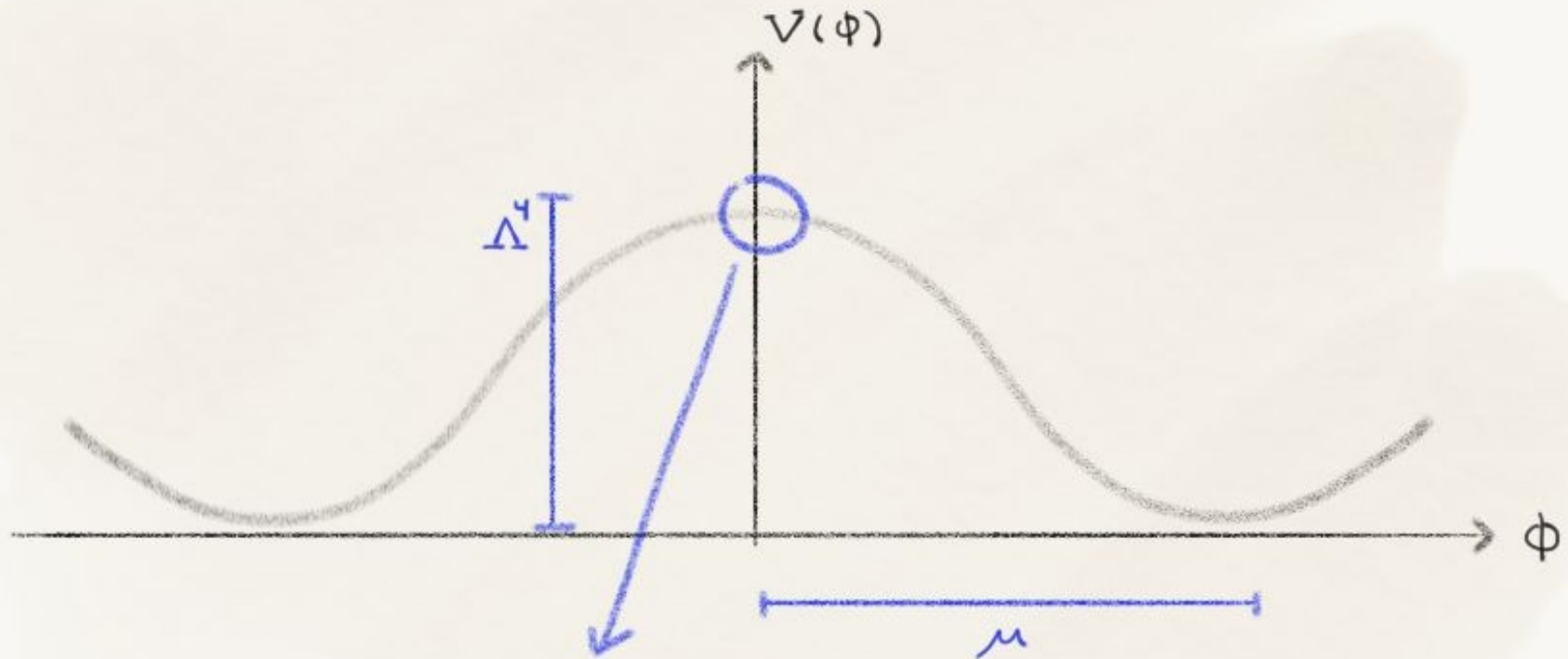


TRIVIAALLY
ETERNAL

Hilltop Inflation



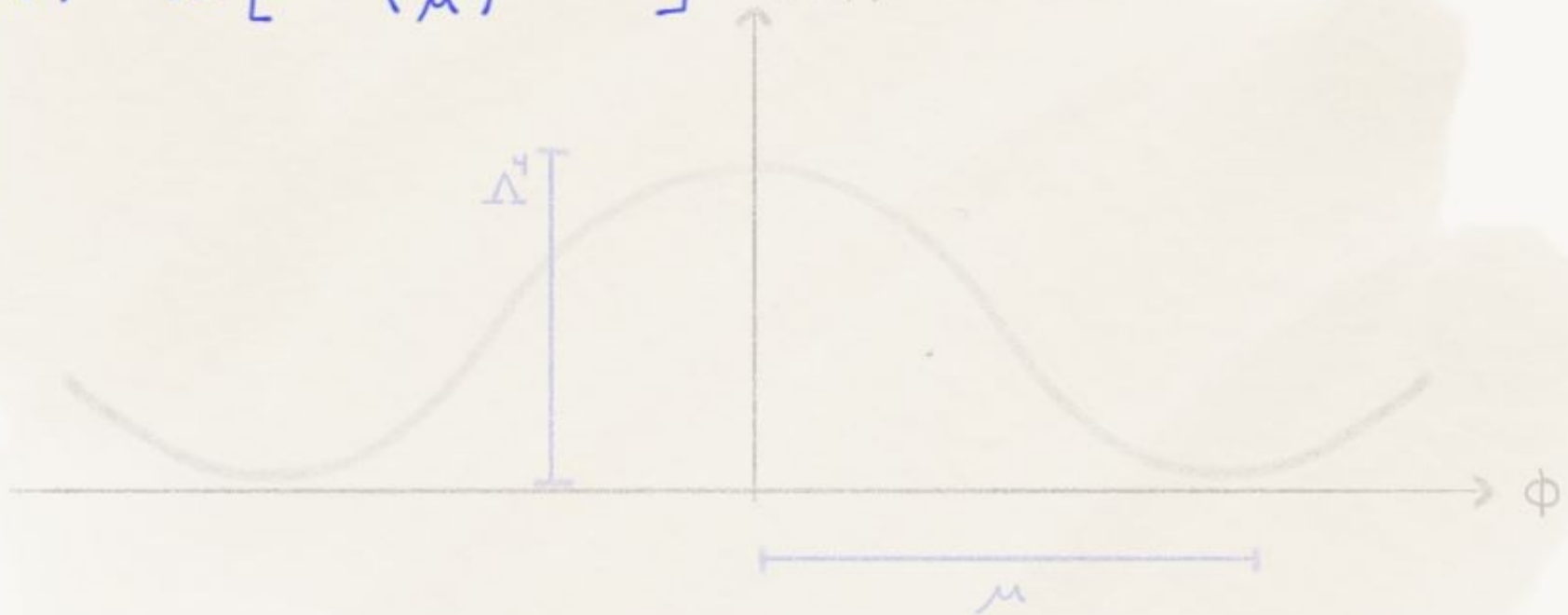
Hilltop Inflation



$$V(\phi) \sim \Lambda^4 \left[1 - \left(\frac{\phi}{\mu} \right)^p + \dots \right] \quad \underbrace{p = 2, 4, \dots}_{\text{Hilltop}}$$

Hilltop Inflation

$$V(\phi) \sim \Lambda^4 \left[1 - \left(\frac{\phi}{\mu} \right)^p + \dots \right] \quad p = 2, 4, \dots$$

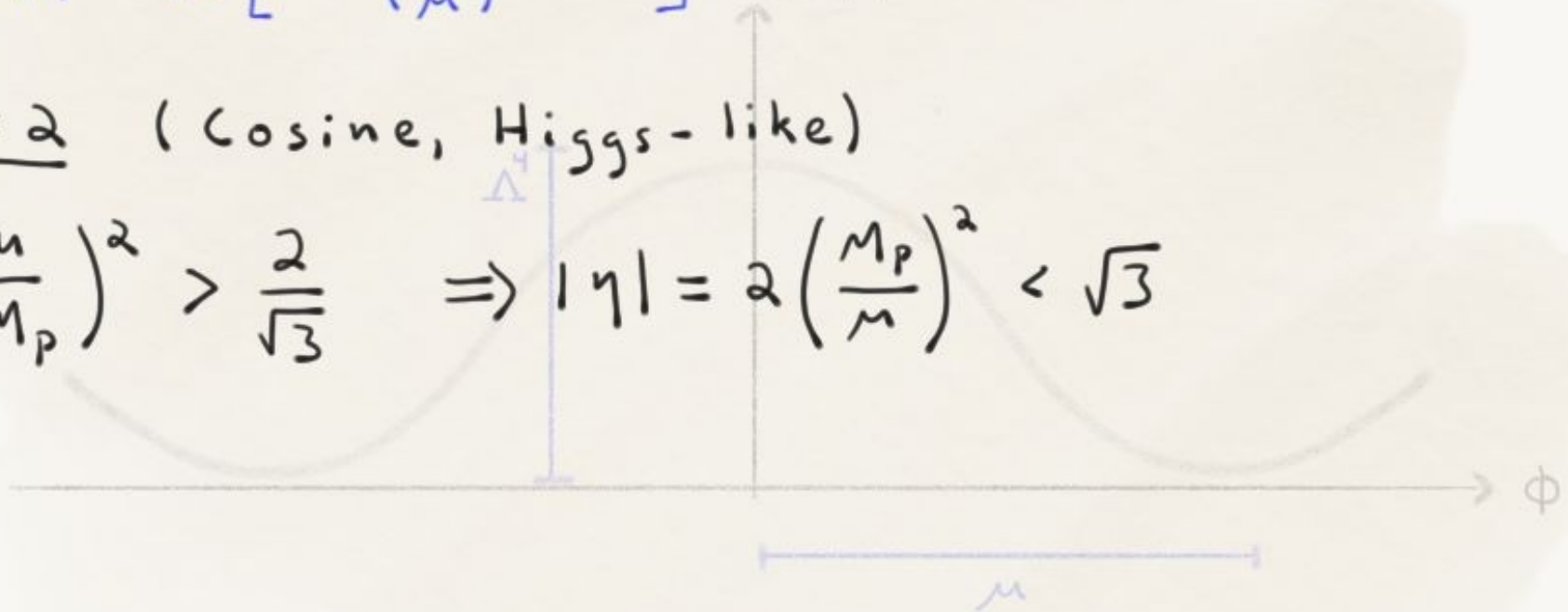


Hilltop Inflation

$$V(\phi) \sim \Lambda^4 \left[1 - \left(\frac{\phi}{\mu} \right)^p + \dots \right] \quad p=2, 4, \dots$$

$p=2$ (Cosine, Higgs-like)

$$\left(\frac{\mu}{M_P} \right)^2 > \frac{2}{\sqrt{3}} \Rightarrow |\eta| = 2 \left(\frac{M_P}{\mu} \right)^2 < \sqrt{3}$$



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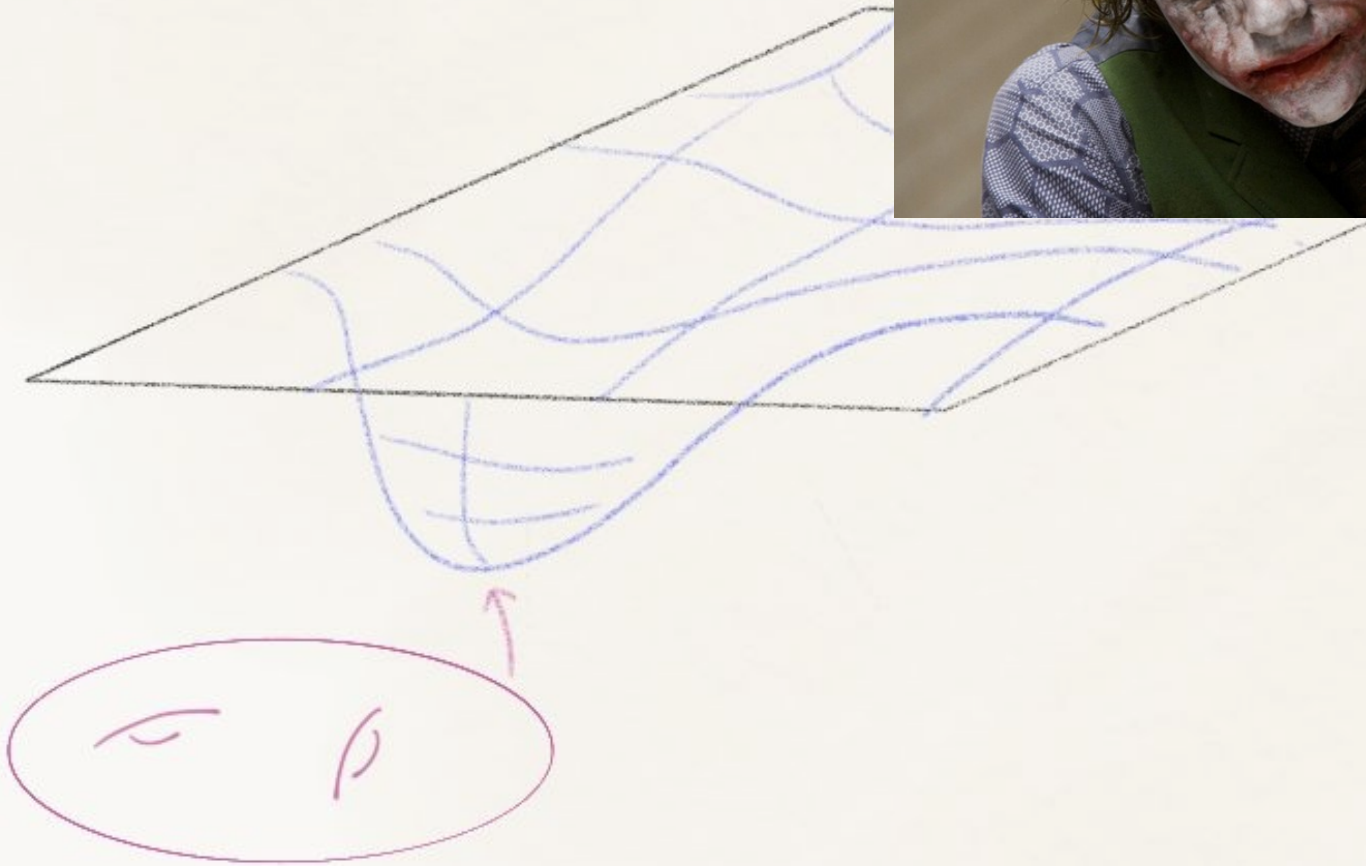
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$$\eta = M_P^2 \left(\frac{V''}{V} \right) \sim \mathcal{O}(1)$$

Conjecture, Smonjecture...

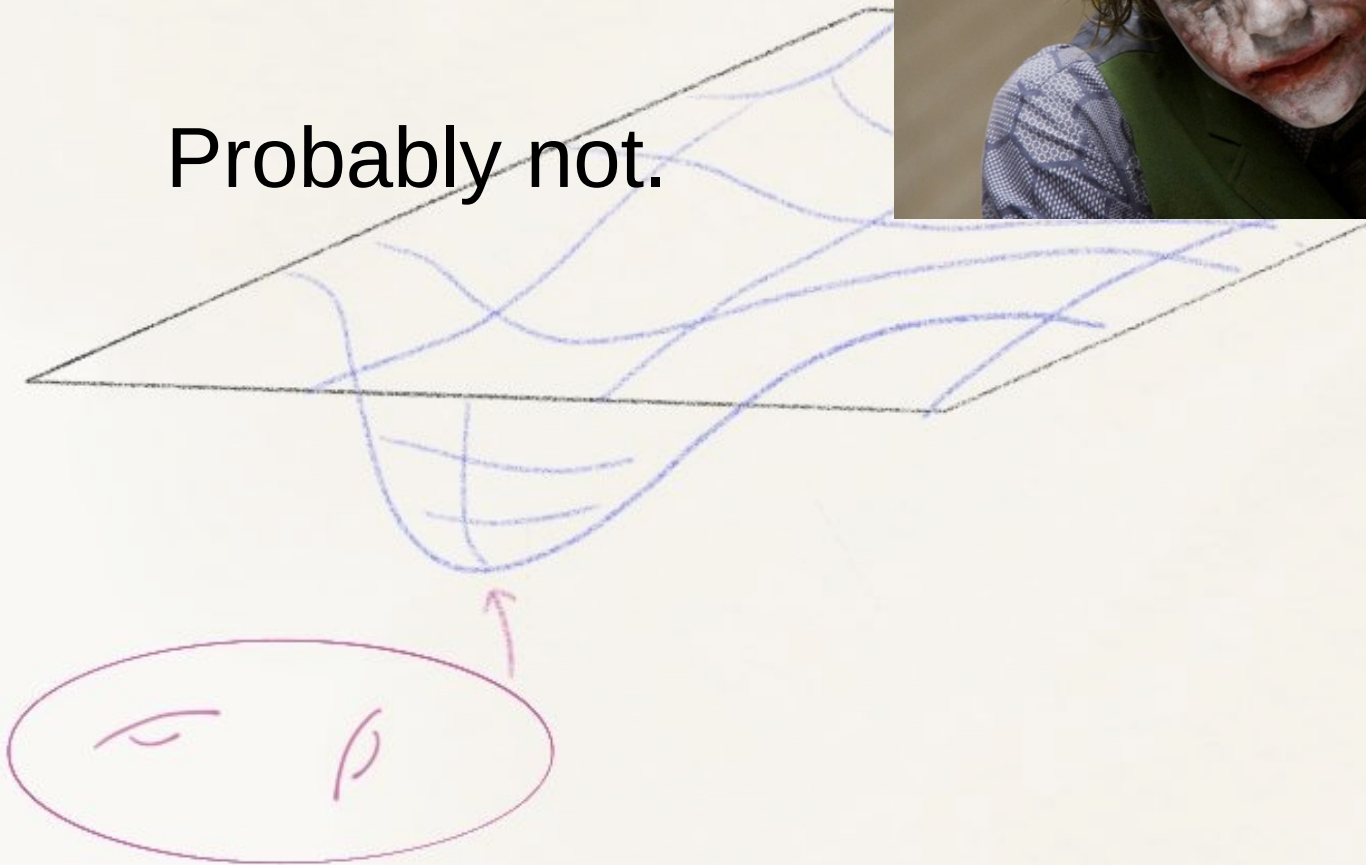
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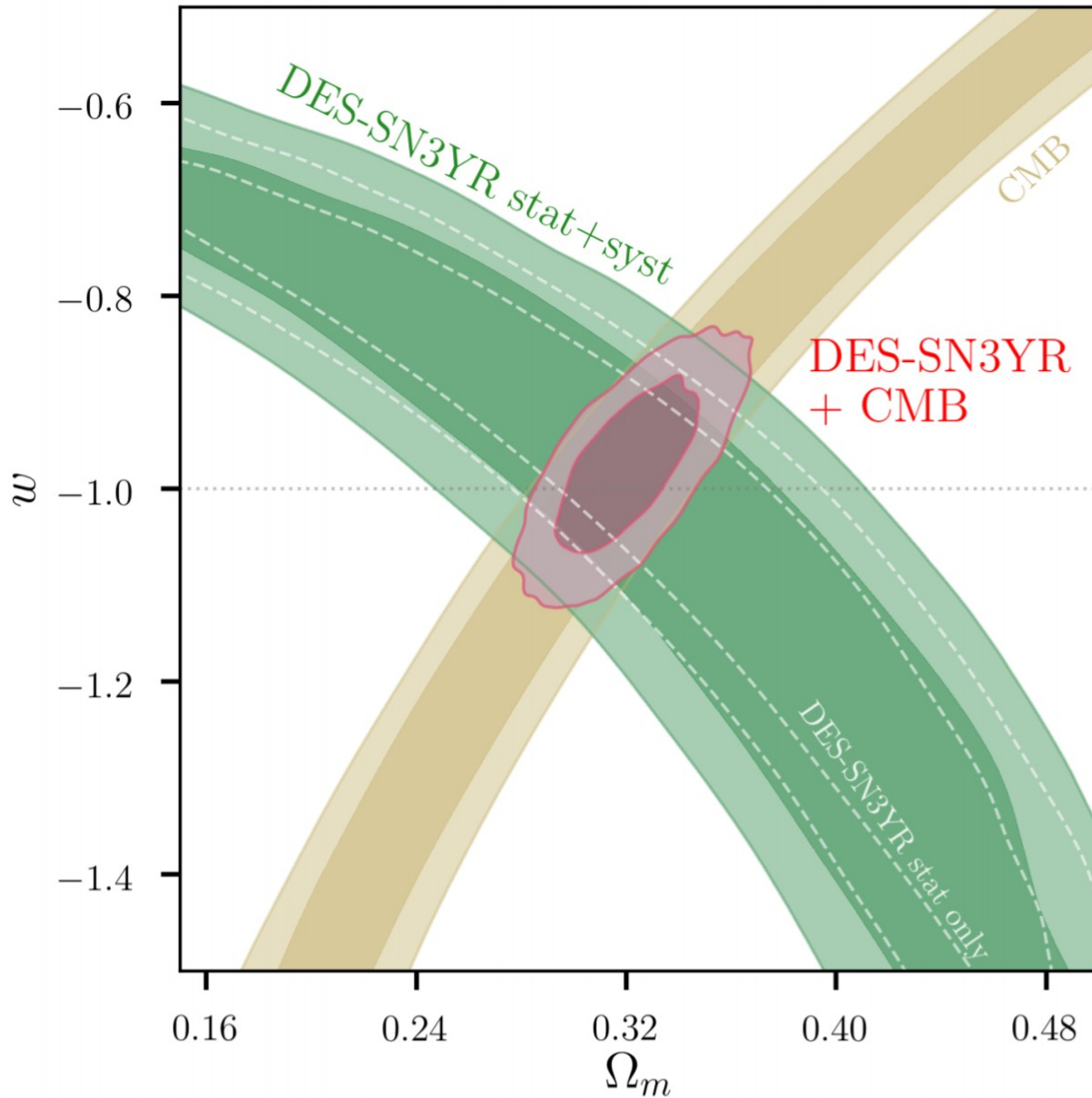
Conjecture, Smonjecture...

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Probably not.



DES-SN + CMB Constraints



Flat w CDM:

$$w = -0.978 \pm 0.059$$

Flat w_0/w_a CDM:

$$w_0 = -0.885 \pm 0.114$$

$$w_a = -0.387 \pm 0.430$$

[Abbott, et al. ArXiv:1811.02374]

Conjecture, Smonjecture...

So, should we take these conjectures ... *seriously?*



Probably not.

If string theory doesn't support de Sitter solutions, so what?